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# Design and Evaluation of the Hamal Parallel Computer

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# **Design and Evaluation of the Hamal Parallel Computer**

by

J.P. Grossman

Submitted to the Department of Electrical Engineering  
and Computer Science in partial fulfillment  
of the requirements for the degree of

Doctor of Philosophy

at the

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## Abstract

Parallel shared-memory machines with hundreds or thousands of processor-memory nodes have been built; in the future we will see machines with millions or even billions of nodes. Associated with such large systems is a new set of design challenges. Many problems must be addressed by an architecture in order for it to be successful; of these, we focus on three in particular. First, a scalable memory system is required. Second, the network messaging protocol must be fault-tolerant. Third, the overheads of thread creation, thread management and synchronization must be extremely low.

This thesis presents the complete system design for *Hamal*, a shared-memory architecture which addresses these concerns and is directly scalable to one million nodes. Virtual memory and distributed objects are implemented in a manner that requires neither inter-node synchronization nor the storage of globally coherent translations at each node. We develop a lightweight fault-tolerant messaging protocol that guarantees message delivery and idempotence across a discarding network. A number of hardware mechanisms provide efficient support for massive multithreading and fine-grained synchronization.

Experiments are conducted in simulation, using a trace-driven network simulator to investigate the messaging protocol and a cycle-accurate simulator to evaluate the Hamal architecture. We determine implementation parameters for the messaging protocol which optimize performance. A discarding network is easier to design and can be clocked at a higher rate, and we find that with this protocol its performance can approach that of a non-discarding network. Our simulations of Hamal demonstrate the effectiveness of its thread management and synchronization primitives. In particular, we find *register-based synchronization* to be an extremely efficient mechanism which can be used to implement a software barrier with a latency of only 523 cycles on a 512 node machine.

Thesis Supervisor: Thomas F. Knight, Jr.  
Title: Senior Research Scientist



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# Chapter 1

## Introduction

*The last thing one knows when writing a book is what to put first.*

– Blaise Pascal (1623-1662), “Pensées”

Over the years there has been an enormous amount of hardware research in parallel computation. It is a testament to the difficulty of the problem that despite the large number of wildly varying architectures which have been designed and evaluated, there are few agreed-upon techniques for constructing a good machine. Even basic questions such as whether or not remote data should be cached remain unanswered. This is in marked contrast to the situation in the scalar world, where many well-known hardware mechanisms are consistently used to improve performance (e.g. caches, branch prediction, speculative execution, out of order execution, superscalar issue, register renaming, etc.).

The primary reason that designing a parallel architecture is so difficult is that the parameters which define a “good” machine are extremely application-dependent. A simple physical simulation is ideal for a SIMD machine with a high processor to memory ratio and a fast 3D grid network, but will make poor utilization of silicon resources in a Beowulf cluster and will suffer due to increased communication latencies and reduced bandwidth. Conversely, a parallel database application will perform extremely well on the latter machine but will probably not even run on the former. Thus, it is important for the designer of a parallel machine to choose his or her battles early in the design process by identifying the target application space in advance.

There is an obvious tradeoff involved in choosing an application space. The smaller the space, the easier it is to match the hardware resources to those required by user programs, resulting in faster and more efficient program execution. Hardware design can also be simplified by omitting features which are unnecessary for the target applications. For example, the Blue Gene architecture [IBM01], which is being designed specifically to fold proteins, does not support virtual memory [Denneau00]. On the other hand, machines with a restricted set of supported applications are less use-

ful and not as interesting to end users. As a result, they are not cost effective because they are unlikely to be produced in volume. Since not everyone has \$100 million to spend on a fast computer, there is a need for commodity general-purpose parallel machines.

The term “general-purpose” is broad and can be further subdivided into three categories. A machine is general-purpose at the *application* level if it supports arbitrary applications via a restricted programming methodology; examples include Blue Gene [IBM01] and the J-Machine ([Dally92], [Dally98]). A machine is general-purpose at the *language* level if it supports arbitrary programming paradigms in a restricted run-time environment; examples include the RAW machine [Waingold97] and Smart Memories [Mai00]. Finally, a machine is general-purpose at the *environment* level if it supports arbitrary management of computation, including resource sharing between mutually non-trusting applications. This category represents the majority of parallel machines, such as Alewife [Agarwal95], Tera [Alverson90], The M-Machine ([Dally94b], [Fillo95]), DASH [Lenoski92], FLASH [Kuskin94], and Active Pages [Oskin98]. Note that each of these categories is not necessarily a sub-category of the next. For example, Active Pages are general-purpose at the environment level [Oskin99a], but not at the application level as only programs which exhibit regular, large-scale, fine-grained parallelism can benefit from the augmented memory pages.

The overall goal of this thesis is to investigate design principles for scalable parallel architectures which are general-purpose at the application, language and environment levels. Such architectures are inevitably less efficient than restricted-purpose hardware for any given application, but may still provide better performance at a fixed price due to the fact that they are more cost-effective. Focusing on general-purpose architectures, while difficult, is appealing from a research perspective as it forces one to consider mechanisms which support computation in a broad sense.

## 1.1 Designing for the Future

Parallel shared-memory machines with hundreds or thousands of processor-memory nodes have been built (e.g. [Dally98], [Laudon97], [Anderson97]); in the future we will see machines with millions [IBM01] and eventually billions of nodes. Associated with such large systems is a new set of design challenges; fundamental architectural changes are required to construct a machine with so many nodes and to efficiently support the resulting number of threads. Three problems in particular must be addressed. First, the memory system must be extremely scalable. In particular, it should be possible to both allocate and physically locate distributed objects without storing global information at each node. Second, the network messaging protocol must be fault-tolerant. With millions of discrete network components it becomes extremely difficult to prevent electrical or mechani-

cal failures from corrupting packets, regardless of the fault-tolerant routing strategy that is used. Instead, the focus will shift to end-to-end messaging protocols that ensure packet delivery across an unreliable network. Finally, the hardware must provide support for efficient thread management. Fine-grained parallelism is required to effectively utilize millions of nodes. The overheads of thread creation, context switching and synchronization should therefore be extremely low.

At the same time, new fabrication processes that allow CMOS logic and DRAM to be placed on the same die open the door for novel hardware mechanisms and a tighter coupling between processors and memory. The simplest application of this technology is to augment existing processor architectures with low-latency high-bandwidth memory [Patterson97]. A more exciting approach is to augment DRAM with small amounts of logic to extend its capabilities and/or perform simple computation directly at the memory. Several research projects have investigated various ways in which this can be done (e.g. [Oskin98], [Margolus00], [Mai00], [Gokhale95]). However, none of the proposed architectures are general-purpose at both the application and the environment level, due to restrictions placed on the application space and/or the need to associate a significant amount of application-specific state with large portions of physical memory.

Massive parallelism and RAM integration are central to the success of future parallel architectures. In this thesis we will explore these issues in the context of general-purpose computation.

## 1.2 The Hamal Parallel Computer

The primary vehicle of our presentation will be the complete system design of a shared memory machine: The Hamal<sup>1</sup> Parallel Computer. Hamal integrates many new and existing architectural ideas with the specific goal of providing a massively scalable and easily programmable platform. The principal tool used in our studies is a flexible cycle-accurate simulator for the Hamal architecture. While many of the novel features of Hamal could be presented and evaluated in isolation, there are a number of advantages to incorporating them into a complete system and assessing them in this context. First, a full simulation ensures that no details have been omitted, so the true cost of each feature can be determined. Second, it allows us to verify that the features are mutually compatible and do not interact in undesirable or unforeseen ways. Third, the cycle-accurate simulator provides a consistent framework within which we can conduct our evaluations. Fourth, our results are more realistic as they are derived from a cycle-accurate simulation of a complete system.

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<sup>1</sup> This research was conducted as part of Project Aries (<http://www.ai.mit.edu/projects/aries>). Hamal is the nickname for Alpha Arietis, one of the stars of the Aries constellation.



A fifth and final advantage to the full-system simulation methodology is that it forces us to pay careful attention to the layers of software that will be running on and cooperating with the hardware. In designing a general-purpose parallel machine, it is important to consider not only the processors, memory, and network that form the hardware substrate, but also the operating system that must somehow manage the hardware resources, the parallel libraries required to present an interface to the machine that is both efficient and transparent, and finally the parallel applications themselves which are built on these libraries (Figure 1-1). During the course of this thesis we will have occasion to discuss each of these important aspects of system design.

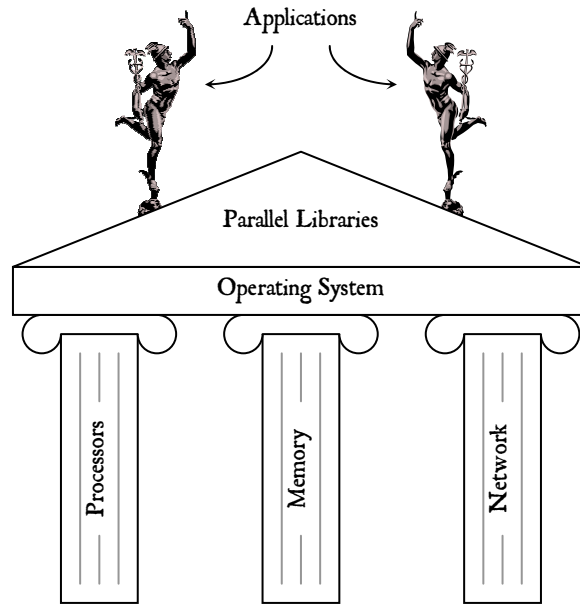


Figure 1-1: The components of a general purpose parallel computer

### 1.3 Contributions

The first major contribution of this thesis is the presentation of novel memory system features to support a scalable, efficient parallel system. A capability format is introduced which supports pointer arithmetic and nearly-tight object bounds without the use of capability or segment tables. We present an implementation of *sparsely faceted arrays* (SFAs) [Brown02a] which allow distributed objects to be allocated with minimal overhead. SFAs are contrasted with *extended address partitioning*, a technique that assigns a separate 64-bit address space to each node. We describe a flexible

scheme for synchronization within the memory system. A number of augmentations to DRAM are proposed to improve system efficiency including virtual address translation, hardware page management and memory events. Finally, we show how to implement forwarding pointers [Greenblatt74], which allow references to one memory location to be transparently forwarded to another, without suffering the high costs normally associated with aliasing problems.

The second contribution is the presentation of a lightweight end-to-end messaging protocol, based on a protocol presented in [Brown01], which guarantees message delivery and idempotence across a discarding network. We describe the protocol, outline the requirements for correctness, and perform simulations to determine optimal implementation parameters. A simple yet accurate analytical model for the protocol is developed that can be applied more broadly to any fault-tolerant messaging protocol.

Our third and final major contribution is the complete description and evaluation of a general-purpose shared-memory parallel computer. The space of possible parallel machines is vast; the Hamal architecture provides a design point against which other general-purpose architectures can be compared. Additionally, a discussion of the advantages and shortcomings of the Hamal architecture furthers our understanding of how to build a “good” parallel machine.

A number of minor contributions are made as we weave our way through the various aspects of hardware and software design. We develop an application-independent hash function with good collision avoidance properties that is easy to implement in hardware. Instruction cache *miss bits* are introduced which reduce miss rates in a set-associative instruction cache by allowing the controller to intelligently select entries for replacement. A systolic array is presented for maintaining least-recently-used information in a highly associative cache. We describe an efficient C++ framework for cycle-based hardware simulation. Finally, we introduce *dynamic sequence partitioning* for reproducibly generating good pseudo-random numbers in multithreaded applications where the number of threads is not known in advance.

## 1.4 Omissions

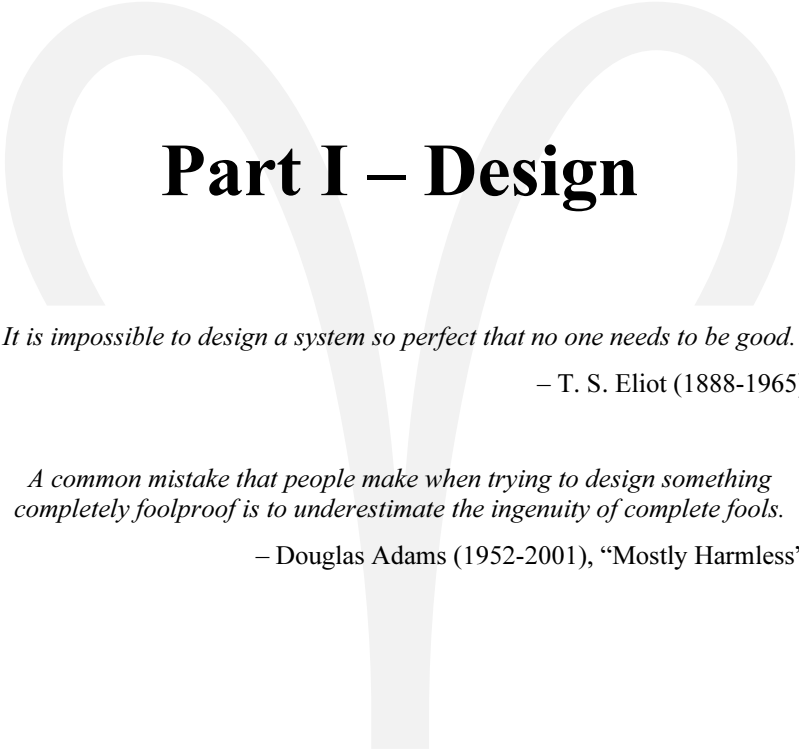
The focus of this work is on scalability and memory integration. A full treatise of general purpose parallel hardware is well beyond the scope of this thesis. Accordingly, there are a number of important areas of investigation that will not be addressed in the chapters that follow. The first of these is processor fault-tolerance. Built-in fault-tolerance is essential for any massively parallel machine which is to be of practical use (a million node computer is an excellent cosmic ray detector). However, the design issues involved in building a fault-tolerant system are for the most part orthogonal to the issues which are under study. We therefore restrict our discussion of

fault-tolerance to the network messaging protocol, and our simulations make the simplifying assumption of perfect hardware. The second area of research not covered by this work is power. While power consumption is certainly a critical element of system design, it is also largely unrelated to our specific areas of interest. Our architecture is therefore presented in absentia of power estimates. The third area of research that we explicitly disregard is network topology. A good network is of fundamental importance, and the choice of a particular network will have a first order effect on the performance of any parallel machine. However, there is already a massive body of research on network topologies, much of it theoretical, and we do not intend to make any contributions in this area. Finally, there will be no discussion of compilers or compilation issues. We will focus on low-level parallel library primitives, and place our faith in the possibility of developing a good compiler using existing technologies.

## 1.5 Organization

This thesis is divided into two parts. In the first part we present the complete system design of the Hamal Parallel Computer. Chapter 2 gives an overview of the design, including the principles that have guided us throughout the development of the architecture. Chapter 3 details the memory system which forms the cornerstone of the Hamal architecture. In Chapter 4 we discuss the key features of the processor design. In Chapter 5 we present the end-to-end messaging protocol used in Hamal to communicate across a discarding network. Chapter 6 describes the event-driven microkernel which was developed in conjunction with the processor-memory nodes. Finally, in Chapter 7 we show how a set of hardware mechanisms together with microkernel cooperation can ensure that the machine is provably deadlock-free. The chapters of Part I are more philosophical than scientific in nature; actual research is deferred to Part II.

In the second part we evaluate various aspects of the Hamal architecture. We begin by describing our simulation methodology in Chapter 8, where we present an efficient C++ framework for cycle-based simulation. In Chapter 9 we discuss the benchmark programs and we introduce *dynamic sequence partitioning* for generating pseudo-random numbers in a multi-threaded application. In Chapters 10, 11 and 12 we respectively evaluate Hamal's synchronization primitives, processor design, and forwarding pointer support. Chapters 13 and 14 depart briefly from the Hamal framework in order to study the fault-tolerant messaging protocol in a more general context: we develop an analytical model for the protocol, then evaluate it in simulation. In Chapter 15 we evaluate the system as a whole, identifying its strengths and weaknesses. Finally in Chapter 16 we conclude and suggest directions for future research.



# Part I – Design

*It is impossible to design a system so perfect that no one needs to be good.*

– T. S. Eliot (1888-1965)

*A common mistake that people make when trying to design something completely foolproof is to underestimate the ingenuity of complete fools.*

– Douglas Adams (1952-2001), “Mostly Harmless”



# Chapter 2

## Overview

*I have always hated machinery, and the only machine I ever understood was a wheelbarrow, and that but imperfectly.*

– Eric Temple Bell (1883-1960)

Traditional computer architecture makes a strong distinction between processors and memory. They are separate components with separate functions, communicating via a bus or network. The Hamal architecture was motivated by a desire to remove this distinction, leveraging new embedded DRAM technology in order to tightly integrate processor and memory. Separate components are replaced by processor-memory nodes which are replicated across the system. Processing power and DRAM coexist in a fixed ratio; increasing the amount of one necessarily implies increasing the amount of the other. In addition to reducing the number of distinct components in the system, this design improves the asymptotic behavior of many problems [Oskin98]. The high-level abstraction is a large number of identical fine-grained processing elements sprinkled throughout memory; we refer to this as the Sea Of Uniform Processors (SOUP) model. Previous examples of the SOUP model include the J-Machine [Dally92], and RAW [Waingold97].

### 2.1 Design Principles

A number of general principles have guided the design of the Hamal architecture. They are presented below in approximate order from most important to least important.

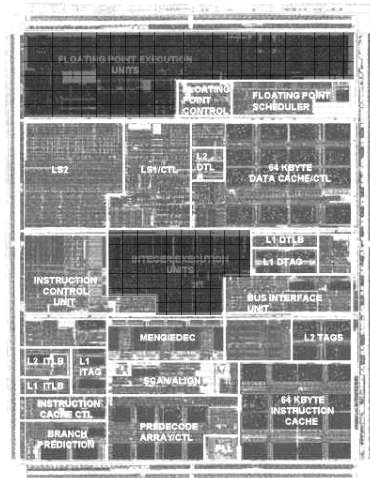
#### 2.1.1 Scalability

Implied in the SOUP architectural model is a very large number of processor-memory nodes. Traditional approaches to parallelism, however, do not scale very well beyond a few thousand nodes, in part due to the need to maintain globally coherent state at each node such as translation lookaside

buffers (TLBs). The Hamal architecture has been designed to overcome this barrier and scale to millions or even billions of nodes.

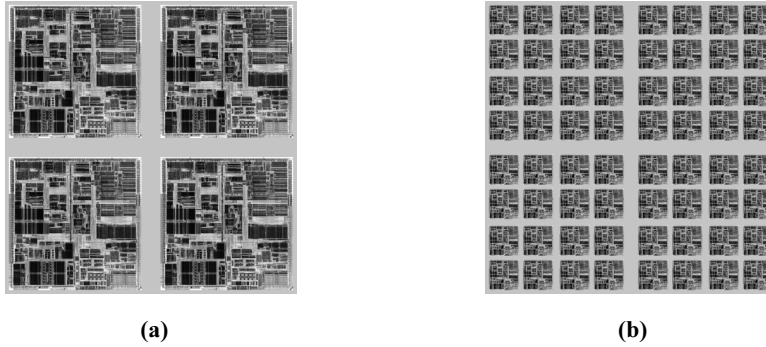
### 2.1.2 Silicon Efficiency

In current architectures there is an emphasis on executing a sequential stream of instructions as quickly as possible. As a result, massive amounts of silicon are devoted to incremental optimizations such as branch prediction, speculative execution, out of order execution, superscalar issue, and register renaming. While these optimizations improve performance, they may reduce the architecture's *silicon efficiency*, when can be roughly defined as performance per unit area. As a concrete example, in the AMD K7 less than 25% of the die is devoted to useful work; the remaining 75% is devoted to making this 25% run faster (Figure 2-1). In a scalar machine this is not a concern as the primary objective is single-threaded performance.



**Figure 2-1: K7 Die Photo. Shaded areas are devoted to useful work.**

Until recently the situation in parallel machines was similar. Machines were built with one processing node per die. Since, to first order, the overall cost of an  $N$  node system does not depend on the size of the processor die, there was no motivation to consider silicon efficiency. Now, however, designs are emerging which place several processing nodes on a single die ([Case99], [Diefen99], [IBM01]). As the number of transistors available to designers increases, this trend will continue with greater numbers of processors per die (Figure 2-2).



**Figure 2-2: (a) Today: 1-4 processors/die. (b) Tomorrow:  $N$  processors/die.**

When a large number of processors are placed on each die, overall silicon efficiency becomes more important than the raw speed of any individual processor. The Hamal architecture has been designed to maximize silicon efficiency. This design philosophy favours small changes in hardware which produce significant gains in performance, while eschewing complicated features with large area costs. It also favours general mechanisms over application- or programming language-specific enhancements.

As a metric, silicon efficiency is extremely application-dependent and correspondingly difficult to quantify. Applications differ wildly in terms of their computational intensity, memory usage, communication requirements, parallelism and scalability. It is not possible to maximize silicon efficiency in an absolute sense without reference to a specific set of applications, but one can often argue convincingly for or against specific architectural features based on this design principle.

### **2.1.3 Simplicity**

Simplicity is often a direct consequence of silicon efficiency, as many complicated mechanisms improve performance only at the cost of overall efficiency. Simplicity also has advantages that silicon efficiency on its own does not; simpler architectures are faster to design, easier to test, less prone to errors, and friendlier to compilers.

### **2.1.4 Programmability**

In order to be useful, an architecture must be easy to program. This means two things: it must be easy to *write* programs, and it must be easy to *debug* programs. To a large extent, the former requirement can be satisfied by the compiler as long as the underlying architecture is not so obscure as to defy compilation. The latter requirement can be partially addressed by the programming environment, but there are a number of hardware mechanisms



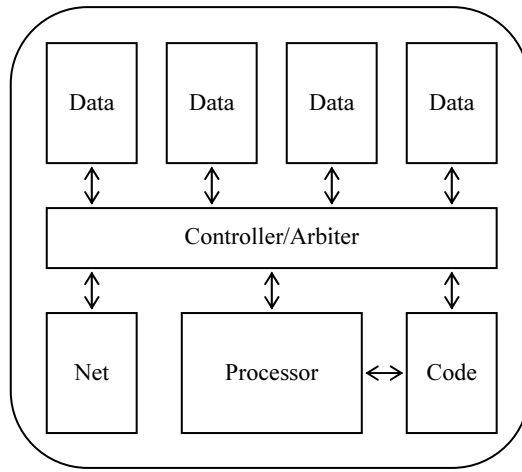
which can greatly ease and/or accelerate the process of debugging. It is perhaps more accurate to refer to this design principle as “debuggability” rather than “programmability”, but one can also argue that there is no difference between the two: it has been said that programming is “the art of debugging a blank sheet of paper” [Jargon01].

### **2.1.5 Performance**

Last and least of our design principles is performance. Along with simplicity, performance can to a large extent be considered a subheading of silicon efficiency. They are opposite subheadings; the goal of silicon efficiency gives rise to a constant struggle between simplicity and performance. By placing performance last among design principles we do not intend to imply that it is unimportant; indeed our interest in Hamal is above all else to design a terrifyingly fast machine. Rather, we are emphasizing that a fast machine is uninteresting unless it supports a variety of applications, it is economical in its use of silicon, it is practical to build and program, and it will scale gracefully over the years as the number of processors is increased by multiple orders of magnitude.

## **2.2 System Description**

The Hamal Architecture consists of a large number of identical processor-memory nodes connected by a fat tree network [Leiserson85]. The design is intended to support the placement of multiple nodes on a single die, which provides a natural path for scaling with future process generations (by placing more nodes on each die). Each node contains a 128 bit multi-threaded VLIW processor, four 128KB banks of data memory, one 512KB bank of code memory, and a network interface (Figure 2-3). Memory is divided into 1KB pages. Hamal is a capability architecture ([Dennis65], [Fabry74]); each 128 bit memory word and register in the system is tagged with a 129<sup>th</sup> bit to distinguish pointers from raw data. Shared memory is implemented transparently by the hardware, and remote memory requests are handled automatically without interrupting the processor.



**Figure 2-3: The Hamal Processor-Memory Node.**

There are no data caches in the system for a number of reasons. First, with on-die DRAM it is already possible to access local memory in only a few cycles. A small number of hardware contexts can therefore tolerate memory latency and keep the hardware busy at all times. Second, caches consume large amounts of silicon area which could instead be used to increase the number of processor-memory nodes. Third, designing a coherent cache for a massively parallel system is an extremely difficult and error-prone task.

System resources are managed by a concurrent event-driven microkernel that runs in the first thread context of every processor. Events, such as page faults and thread creation, are placed on a hardware event queue and serviced sequentially by the microkernel.

The following chapters describe the Hamal architecture in more detail. One aspect of the design that will *not* be discussed is secondary storage. We assume that some form of secondary storage exists which communicates with the nodes via the existing network. The sole purpose of this secondary storage is to store and retrieve pages of data and code, and we make the further assumption that the secondary storage maintains the mapping from virtual page addresses to physical locations within storage. Secondary storage is otherwise unspecified and may consist of DRAM, disks, or some combination thereof.



# Chapter 3

## The Memory System

*The two offices of memory are collection and distribution.*

– Samuel Johnson (1709-1784)

In a shared-memory parallel computer, the memory model and its implementation have a direct impact on system performance, programmability and scalability. In this chapter we describe the various aspects of the Hamal memory system, which has been designed to address the specific goals of massive scalability and processor-memory integration.

### 3.1 Capabilities

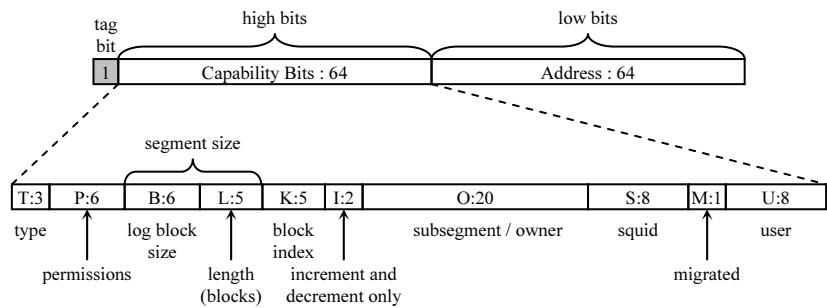
If a machine is to support environment-level general purpose computing, one of the first requirements of the memory system is that it provide a protection mechanism to prevent applications from reading or writing each other's data. In a conventional system, this is accomplished by providing each process with a separate virtual address space. While such an approach is functional, it has three significant drawbacks. First, a process-dependent address translation mechanism dramatically increases the amount of machine state associated with a given process (page tables, TLB entries, etc), which increases system overhead and is an impediment to fine-grained multithreading. Second, data can only be shared between processes at the page granularity, and doing so requires some trickery on the part of the operating system to ensure that the page tables of the various processes sharing the data are kept consistent. Finally, this mechanism does not provide security within a single context; a program is free to create and use invalid pointers.

These problems all stem from the fact that in most architectures there is no distinction at the hardware level between pointers and integers; in particular a user program can create a pointer to an arbitrary location in the virtual address space. An alternate approach which addresses these problems is the use of unforgeable *capabilities* ([Dennis65], [Fabry74]). Capabilities allow the hardware to guarantee that user programs will make no illegal memory references. It is therefore safe to use a single shared

illegal memory references. It is therefore safe to use a single shared virtual address space which greatly simplifies the memory model.

In the past capability machines have been implemented using some form of capability table ([Houdek81], [Tyner81]) and/or special capability registers ([Abramson86], [Herbert79]), or even in software ([Anderson86], [Chase94]). Such implementations have high overhead and are an obstacle to efficient computing with capabilities. However, in [Carter94] a capability format is proposed in which all relevant address, permission and segment size information is contained in a 64 bit word. This approach obviates the need to perform expensive table lookup operations for every memory reference and every pointer arithmetic operation. Additionally, the elimination of capability tables allows the use of an essentially unbounded number of segments (blocks of allocated memory); in particular object-based protection schemes become practical. The proposed format requires all segment sizes to be powers of two and uses six bits to store the base 2 logarithm of the segment size, allowing for segments as small as one byte or as large as the entire address space.

Hamal employs a capability format ([Grossman99], [Brown00]) which extends this idea. 128 bit capabilities are broken down into 64 bits of address and 64 bits of capability information (segment size, permissions, etc.). As in [Carter94], all words are tagged with a single bit to distinguish pointers from raw data, so capabilities and data may be mixed freely. Figure 3-1 shows how the 64 capability bits are broken down; the meaning of these fields will be explained in the following sections.



**Figure 3-1: The Hamal Capability Format.**

### 3.1.1 Segment Size and Block Index

Restricting segment sizes to powers of two as in [Carter94] causes three problems. First, since the size of many objects is not a power of two, there will be some amount of internal fragmentation within the segments. This wastes memory and reduces the likelihood of detecting pointer errors in programs as pointers can be incremented past the end of objects while re-

maining within the allocated segment. Second, this fragmentation causes the apparent amount of allocated memory to exceed the amount of in-use memory by as much as a factor of two. This can impact the performance of system memory management strategies such as garbage collection. Finally, the alignment restriction may cause a large amount of external fragmentation when objects of different size are allocated. As a result, a larger number of physical pages may be required to store a given set of objects.

To allow for more flexible segment sizes, we use an 11-bit floating point representation for segment size which was originally proposed by fellow Aries researcher Jeremy Brown [Brown99] and is similar to the format used in ORSLA [Bishop77]. Each segment is divided into *blocks* of size  $2^B$  bytes where  $0 \leq B \leq 63$ , so six bits are required to specify the block size. The remaining 5 bits specify the length  $1 \leq L \leq 32$  of the segment in blocks: the segment size is  $L \cdot 2^B$ . Note that the values  $1 \leq L \leq 16$  are only required when  $B = 0$ . If  $B > 0$  and  $L \leq 16$  we can use smaller blocks by doubling  $L$  and subtracting 1 from  $B$ . It follows that the worst-case internal fragmentation occurs when  $L = 17$  and only a single byte in the last block is used, so the fraction of wasted memory is less than  $1/17 < 5.9\%$ . As noted in [Carter94], this is the maximum amount of *virtual* memory which is wasted; the amount of physical memory wasted will in general be smaller.

In order to support pointer arithmetic and pointers to object interiors, we must be able to recover a segment's base address from a pointer to any location within the segment. To this end we include a five bit block index field  $K$  which gives the zero-based index of the block within the segment to which the capability points (Figure 3-2). The segment base address is computed from the current address by setting the low  $B$  address bits to zero, then subtracting  $K \cdot 2^B$ . Note that the capability format in [Carter94] can be viewed as a special case of this format in which  $L = 1$  and  $K = 0$  for all capabilities.

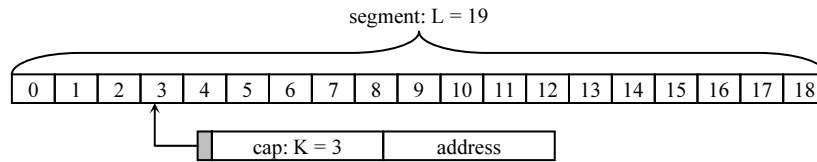
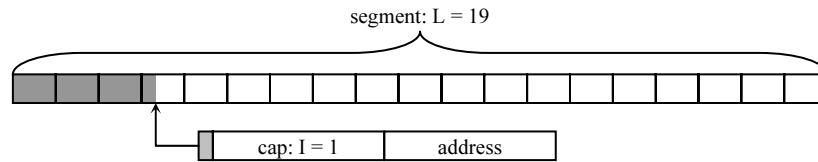


Figure 3-2: Pointer to segment interior with  $K = 3$ .

### 3.1.2 Increment and Decrement Only

Two bits  $I$  and  $D$  (grouped together in Figure 3-1) are used to specify a capability as increment-only and decrement-only respectively. It is an error to add a negative offset to a capability with  $I$  set, or a positive offset to a capability with  $D$  set. Setting these bits has the effect of trading unrestricted pointer arithmetic for the ability to exactly specify the start ( $I$  set) or end ( $D$

set) of the region of memory addressable by the capability. For example, if the capability in Figure 3-2 has I set then it cannot access the shaded region of the segment shown in Figure 3-3. This can be used to implement exact object bounds by aligning the object with the end of the (slightly larger) allocated segment instead of the start, then returning a capability with I set that points to the start of the object. It is also useful for sub-object security; if an object contains both private and public data, the private data can be placed at the start of the object (i.e. the shaded region of Figure 3-3), and clients can be given a pointer to the start of the public data with I set. Finally, setting I and D simultaneously prevents a capability from being modified at all.



**Figure 3-3: Using increment-only for sub-object security or exact bounds.**

### 3.1.3 Subsegments

It is a simple matter to restrict a capability to a subsegment of the original segment by appropriately modifying the B, L and K fields. In some cases it may also be desirable to recover the original segment from a restricted capability; a garbage collector, for example, would require this information. We can accomplish this by saving the values of (B, L, K) corresponding to the start of the subsegment within the original segment. Given an arbitrarily restricted capability, the original segment can then be recovered in two steps. First we compute the base address of the sub-segment as described in Section 3.1.1. Then we restore the saved (B, L, K) and again compute the base address, this time of the containing segment. Note that we must always store (B, L, K) for the largest containing segment, and if a capability is restricted several times then the intermediate sub-segments cannot be recovered. This scheme requires 16 bits of storage; these 16 bits are placed in the shared 20-bit subsegment / owner field. The other use for this field will be explained in Section 3.4 when we discuss distributed objects.

### 3.1.4 Other Capability Fields

The three bit type field (T) is used to specify one of seven hardware-recognized capability types. A *data* capability is a pointer to data memory. A *code* capability is used to read or execute code. Two types of *sparse* capabilities are used for distributed objects and will be described in Section 3.4. A *join* capability is used to write directly to one or more registers in a

thread and will be discussed in Section 4.4. An *IO* capability is used to communicate with the external host. Finally, a *user* capability has a software-specified meaning, and can be used to implement unforgeable certificates.

The permissions field (P) contains the following permission bits:

Bit	Permission
R	read
W	write
T	take
G	grant
DT	diminished take
DG	diminished grant
X	execute
P	execute privileged

**Table 3-1: Capability permission bits**

The read and write bits allow the capability to be used for reading/writing non-pointer data; take and grant are the corresponding permission bits for reading/writing pointers. The diminished take and diminished grant bits also allow capabilities to be read/written, however they are “diminished” by clearing all permission bits except for R and DT. These permission bits are based on those presented in [Karger88]. The X and P bits are exclusively for code capabilities which do not use the W, T, G, DT or DG bits (in particular, Hamal specifies that code is read-only). Hence, only 6 bits are required to encode the above permissions.

The eight bit user field (U) is ignored by the hardware and is available to the operating system for use. Finally, the eight bit squid field (S) and the migrated bit (M) are used to provide support for forwarding pointers as described in the next section.

## 3.2 Forwarding Pointer Support

Forwarding pointers are a conceptually simple mechanism that allow references to one memory location to be transparently forwarded to another. Known variously as “invisible pointers” [Greenblatt74], “forwarding addresses” [Baker78] and “memory forwarding” [Luk99], they are relatively easy to implement in hardware, and are a valuable tool for safe data compaction ([Moon84], [Luk99]) and object migration [Jul88]. Despite these advantages, however, forwarding pointers have to date been incorporated into few architectures.

One reason for this is that forwarding pointers have traditionally been perceived as having limited utility. Their original intent was fairly specific to LISP garbage collection, but many methods of garbage collection exist



which do not make use of or benefit from forwarding pointers [Plainfossé95], and consequently even some LISP-specific architectures do not implement forwarding pointers (such as SPUR [Taylor86]). Furthermore, the vast majority of processors developed in the past decade have been designed with C code in mind, so there has been little reason to support forwarding pointers.

More recently, the increasing prevalence of the Java programming language has prompted interest in mechanisms for accelerating the Java virtual machine, including direct silicon implementation [Tremblay99]. Since the Java specification includes a garbage collected memory model [Gosling96], architectures designed for Java can benefit from forwarding pointers which allow efficient incremental garbage collection ([Baker78], [Moon84]). Additionally, in [Luk99] it is shown that using forwarding pointers to perform safe data relocation can result in significant performance gains on arbitrary programs written in C, speeding up some applications by more than a factor of two. Finally, in a distributed shared memory machine, data migration can improve performance by collocating data with the threads that require it. Forwarding pointers provide a safe and efficient mechanism for object migration [Jul88]. Thus, there is growing motivation to include hardware support for forwarding pointers in novel architectures.

A second and perhaps more significant reason that forwarding pointers have received little attention from hardware designers is that they create a new set of aliasing problems. In an architecture that supports forwarding pointers, no longer can the hardware and programmer assume that different pointers point to different words in memory (Figure 3-4). In [Luk99] two specific problems are identified. First, direct pointer comparisons are not a safe operation; some mechanism must be provided for determining the final addresses of the pointers. Second, seemingly independent memory operations may no longer be reordered in out-of-order machines.

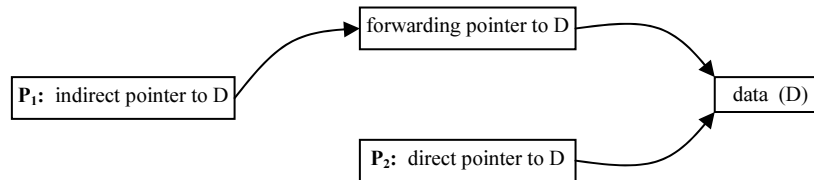


Figure 3-4: Aliasing resulting from forwarding pointer indirection.

### 3.2.1 Object Identification and Squids

Forwarding pointer aliasing is an instance of the more general challenge of determining object identity in the presence of multiple and/or changing names. This problem has been studied explicitly [Setrag86]. A natural solution which has appeared time and again is the use of system-wide unique

object ID's (e.g. [Dally85], [Setrag86], [Moss90], [Day93], [Plainfossé95]). UID's completely solve the aliasing problem, but have two disadvantages:

- i. The use of ID's to reference objects requires an expensive translation each time an object is referenced to obtain its virtual address.
- ii. Quite a few bits are required to ensure that there are enough ID's for all objects and that globally unique ID's can be easily generated in a distributed computing environment. In a large system, at least sixty-four bits would likely be required in order to avoid any expensive garbage collection of ID's and to allow each processor to allocate ID's independently.

Despite these disadvantages, the use of ID's remains appealing as a way of solving the aliasing problem, and it is tempting to try to find a practical and efficient mechanism based on ID's. We begin by noting that the expensive translations (i) are unnecessary if object ID's are included as part of the capability format. In this case we have the best of both worlds: object references make use of the address so that no translation is required, and pointer comparisons and memory operation reordering are based on ID's, eliminating aliasing problems. However, this still leaves us with disadvantage (ii), which implies that the pointer format must be quite large.

We can solve this problem by dropping the restriction that the ID's be unique. Instead of long unique ID's, we use short quasi-unique ID's (**squids**) [Grossman02]. At first this seems to defeat the purpose of having ID's, but we make the following observation: while squids cannot be used to determine that two pointers reference the same object, they *can* in most cases be used to determine that two pointers reference *different* objects. If we randomly generate an  $n$  bit squid every time an object is allocated, then the probability that pointers to distinct objects cannot be distinguished by their squids is  $2^{-n}$ .

### 3.2.2 Pointer Comparisons and Memory Operation Reordering

We can efficiently compare two pointers by comparing their base addresses, their segment offsets and their squids. If the base addresses are the same then the pointers point to the same object, and can be compared using their offsets. If the squids are different then they point to different objects. If the offsets are different then they either point to different objects or to different words of the same object. In the case that the base addresses are different but the squids and offsets are the same, we trap to a software routine which performs the expensive dereferences necessary to determine whether or not the final addresses are equal.

We can argue that this last case is rare by observing that it occurs in two circumstances: either the pointers reference different objects which

have the same squid, or the pointers reference the same object through different levels of indirection. The former occurs with probability  $2^{-n}$ . The latter is application dependent, but we note that (1) applications tend to compare pointers to different objects more frequently than they compare pointers to the same object, and (2) the results of the simulations in [Luk99] indicate that it may be reasonable to expect the majority of pointers to migrated data to be updated, so that two pointers to the same object will usually have the same level of indirection.

In a similar manner, the hardware can use squids to decide whether or not it is possible to reorder memory operations. If the squids are different, it is safe to reorder. If the squids are the same but the offsets are different, it is again safe to reorder. If the squids and offsets are the same but the addresses are different, the hardware assumes that the operations cannot be reordered. It is not necessary to explicitly check for aliasing since preserving order guarantees conservative but correct execution. Only simple comparisons are required, and the probability of failing to reorder references to different objects is  $2^{-n}$ .

### 3.2.3 Implementation

The Hamal capability contains an eight bit squid field (S) which is randomly generated every time memory is allocated. The probability that two objects cannot be distinguished by their squids is thus  $2^{-8} < 0.4\%$ . This reduces the overhead due to aliasing to a small but still non-zero amount. In order to eliminate overhead completely for applications that do not make use of forwarding pointers, we add a *migrated* bit (M) which indicates whether or not the capability points to the original segment of memory in which the object was allocated. When a new object is created, pointers to that object have  $M = 0$ . When the object is migrated, pointers to the new location (and all subsequent locations) have  $M = 1$ . If the hardware is comparing two pointers with  $M = 0$  (either as the result of a comparison instruction, or to check for a dependence between memory operations), it can ignore the squids and perform the comparison based on addresses alone. Hence, there is no runtime cost associated with support for forwarding pointers if an application does not use them.

## 3.3 Augmented Memory

One of the goals of this thesis is to explore ways in which embedded DRAM technology can be leveraged to migrate various features and computational tasks into memory. The following sections describe a number of augmentations to memory in the Hamal architecture.

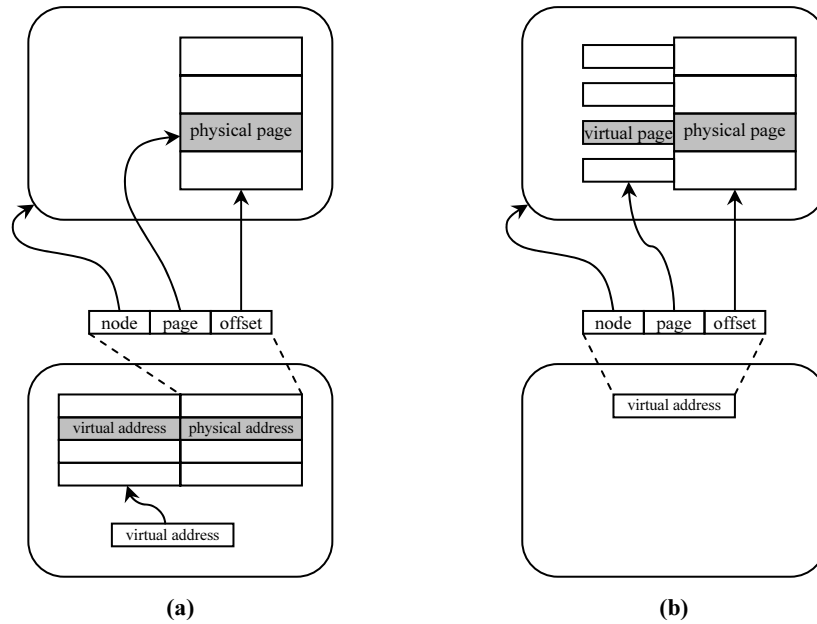
### 3.3.1 Virtual Memory

The memory model of early computers was simple: memory was external storage for data; data could be modified or retrieved by supplying the memory with an appropriate physical address. This model was directly implemented in hardware by discrete memory components. Such a simplified view of memory has long since been replaced by the abstraction of virtual memory, yet the underlying memory components have not changed. Instead, complexity has been added to processors in the form of logic which performs translations from sophisticated memory models to simple physical addresses.

There are a number of drawbacks to this approach. The overhead associated with each memory reference is large due to the need to look up page table entries. All modern processors make use of translation lookaside buffers (TLB's) to try to avoid the performance penalties associated with these lookups. A TLB is essentially a cache, and as such provides excellent performance for programs that use sufficiently few pages, but is of little use to programs whose working set of pages is large. Another problem common to any form of caching is the "pollution" that occurs in a multi-threaded environment: a single TLB must be shared by all threads which reduces its effectiveness and introduces a cold-start effect at every context switch. Finally, in a multiprocessor environment the TLB's must be kept globally consistent which places constraints on the scalability of the system [Teller90].

The Hamal architecture addresses these problems by performing virtual address translations at the memory rather than at the processor. Associated with each bank of DRAM is a hardware page table with one entry per physical page. These hardware page tables are similar in structure and function to the TLB's of conventional processors. They differ in that they are persistent (since there is a single shared virtual address space) and complete; they do not suffer from pollution or cold-starts. They are also slightly simpler from a hardware perspective due to the fact that a given entry will always translate to the same physical page. When no page table entry matches the virtual address of a memory request, a page fault event is generated which is handled in software by the microkernel.

A requirement of this approach is that there be a fixed mapping from virtual addresses to physical nodes. Accordingly, the upper bits of each virtual address are used to specify the node on which that address resides. This allows memory requests to be forwarded to the correct location without storing any sort of global address mapping information at each node (Figure 3-5).



**Figure 3-5: (a) Conventional approach: virtual address is translated at the source node using a TLB. Physical address specifies node and physical page. (b) Hardware page tables: virtual address specifies node and virtual page. Memory is accessed using virtual page address.**

The idea of hardware page tables is not new; they were first proposed for parallel computers in [Teller88], in which it was suggested that each memory module maintain a table of resident pages. These tables are accessed associatively by virtual address; a miss indicates a page fault. Subsequent work has verified the performance advantages of translating virtual addresses to physical addresses at the memory rather than at the processor ([Teller94], [Qui98], [Qui01]).

A related idea is *inverted page tables* ([Houdek81], [Chang88], [Lee89]) which also feature a one to one correspondence between page table entries and physical pages. However, the intention of inverted page tables is simply to support large address spaces without devoting massive amounts of memory to traditional forward-mapped page tables. The page tables still reside in memory, and translation is still performed at the processor. A hash table is used to locate page table entries from virtual addresses. In [Huck93], this hash table is combined with the inverted page table to form a *hashed page table*.

### **3.3.2 Automatic Page Allocation**

Hardware page tables allow the memory banks to detect which physical pages are in use at any given time. A small amount of additional logic makes it possible for them to select an unused page when one is required. In the Hamal architecture, when a virtual page is created or paged in, the targeted memory bank automatically selects a free physical page and creates the page table entry. Additionally, pages that are created are initialized with zeros. The combination of hardware page tables and automatic page allocation obviates the need for the kernel to ever deal with physical page numbers, and there are no instructions that allow it to do so.

### **3.3.3 Hardware LRU**

Most operating systems employ a Least Recently Used (LRU) page replacement policy. Typically the implementation is approximate LRU rather than exact LRU, and some amount of work is required by the operating system to keep track of LRU information and determine the LRU page. In the Hamal architecture, each DRAM bank automatically maintains exact LRU information. This simplifies the operating system and improves performance; a lengthy sequence of status bit polling to determine LRU information is replaced by a single query which immediately returns an exact result. To provide some additional flexibility, each page may be assigned a weight in the range 0-127; an LRU query returns the LRU page of least weight.

### **3.3.4 Atomic Memory Operations**

The ability to place logic and memory on the same die produces a strong temptation to engineer “intelligent” memory by adding some amount of processing power. However, in systems with tight processor/memory integration there is already a reasonably powerful processor next to the memory; adding an additional processor would do little more than waste silicon and confuse the compiler. The processing performed by the memory in the Hamal architecture is therefore limited to simple single-cycle atomic memory operations such as addition, maximum and boolean logic. These operations are useful for efficient synchronization and are similar to those of the Tera [Alverson90] and CrayT3E [Scott96] memory systems.

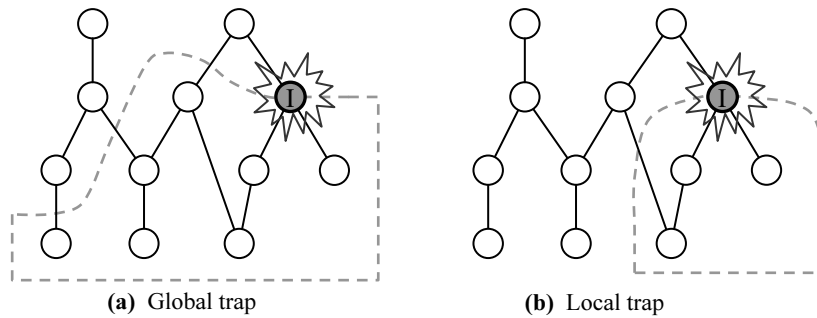
### **3.3.5 Memory Traps and Forwarding Pointers**

Three trap bits (T, U, V) are associated with every 128 bit data memory word. The meaning of the T bit depends on the contents of the memory word. If the word contains a valid data pointer, the pointer is interpreted as a forwarding pointer and the memory request is automatically forwarded.

Otherwise, references to the memory location will cause a trap. This can be used by the operating system to implement mechanisms such as data breakpoints. The U and V bits are available to user programs to enrich the semantics of memory accesses via customized trapping behaviour. Each instruction that accesses memory specifies how U and V are interpreted and/or modified. For each of U and V, the possible behaviours are to ignore the trap bit, trap on set, and trap on clear. Each trap bit may be left unchanged, set, or cleared, and the U bit may also be toggled. When a memory request causes a trap the contents of the memory word and its trap bits are left unchanged and an event is generated which is handled by the microkernel. The T trap bit is also associated with the words of code memory (each 128 bit code memory word contains one VLIW instruction) and can be used in this context to implement breakpoints.

The U and V bits are a generalization of the trapping mechanisms implemented in HEP [Smith81], Tera [Alverson90], and Alewife [Kranz92]. They are also similar to the pre- and post-condition mechanism of the M-Machine [Keckler98], which differs from the others in that instead of causing a trap, a failure sets a predicate register which must be explicitly tested by the user program.

Handling traps on the node containing the memory location rather than on the node containing the offending thread changes the trapping semantics somewhat. Historically, traps have been viewed as events which occur at a well-defined point in program execution. The active thread is suspended, and computation is not allowed to proceed until the event has been atomically serviced. This is a *global* model in that whatever part of the system generates the trap, the effects are immediately visible everywhere. An alternate model is to treat traps as *local* phenomena which affect, and are visible to, only those instructions and hardware components which directly depend on the hardware or software operation that caused the trap. As an example of the difference between the global and local models, consider the program flow graph shown in Figure 3-6, and suppose that the highlighted instruction I generates an trap. In the global model, there is a strict division of instructions into two sets: those that precede I in program order, and those that do not (Figure 3-6a). The hardware must support the semantics that at the time the exception handler begins execution, all instructions in the first set have completed and none of the instructions in the second set have been initiated. In the local model, only those instructions which have true data dependencies on I are guaranteed to be uninitiated (Figure 3-6b). All other instructions are unaffected by the exception, and the handler cannot make any assumptions about their states.



**Figure 3-6: Global vs. local traps.**

The local model is better suited to parallel and distributed computing, in which the execution of a single thread may be physically distributed across the machine; it is the model used in the Hamal architecture. With a global trapping model, a thread would have to stall on every remote memory reference. Memory references causing a trap would be returned to the processor where the thread would be preempted by a trap handler. With a local exception model, a thread may continue processing while waiting for a remote memory reference to complete. If the reference causes a trap, the trap is serviced on the *remote* node, independent of the thread that caused it, and the trap handler completes the memory request manually. This is transparent to the thread; the entire sequence is indistinguishable from an unusually long-latency memory operation.

To allow for application-dependent trapping behaviour, each memory request which can potentially trap on the U and V bits is accompanied by the requesting thread's *trap vector*, a code capability giving the entry point to a trap handler. The microkernel responds to U and V trap events by creating a new thread to run the trap handler.

### 3.4 Distributed Objects

In large-scale shared-memory systems, the layout of data in physical memory is crucial to achieving the best possible performance. In particular, for many algorithms it is important to be able to allocate single objects in memory which are distributed across multiple nodes in the system. The challenge is to allow arbitrary single nodes to perform such allocations without any global communication or synchronization. A straightforward approach is to give each node ownership of parts of the virtual address space that exist on all other nodes, but this makes poor use of the virtual address bits: an  $N$  node system would require  $2\log N$  bits of virtual address to specify both location and ownership.

In this section we describe two different approaches to distributed object allocation: *Extended Address Partitioning* and *Sparsely Faceted Arrays*



[Brown02a]. These techniques share the characteristic that a node atomically and without communication allocates a portion of the virtual address space - a *facet* - on each node in the system, but actual physical memory is lazily allocated only on those nodes which make use of the object. Both of these mechanisms have been incorporated into the Hamal architecture.

### 3.4.1 Extended Address Partitioning

Consider a simple system which gives each node ownership of a portion of the virtual address space on all other nodes, using  $\log N$  virtual address bits to specify ownership (Figure 3-7a). When a distributed object is allocated, these  $\log N$  bits are set to the ID of the node on which the allocation was performed. Thereafter, the owner bits are immutable. Pointer arithmetic on capabilities for the object may alter the node and address fields, but not the owner field. We can therefore move the owner field from the address bits to the capability bits (Figure 3-7b). This has the effect of *extending* the virtual address space by  $\log N$  bits, then *partitioning* it so that each node has ownership of, and may allocate segments within, an equal portion of the address space.

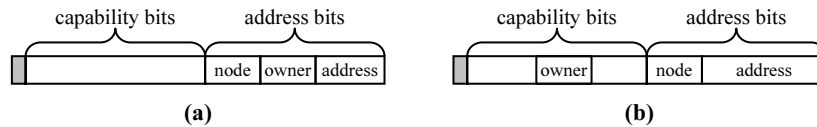


Figure 3-7: (a) Simple address partitioning. (b) Extended address partitioning.

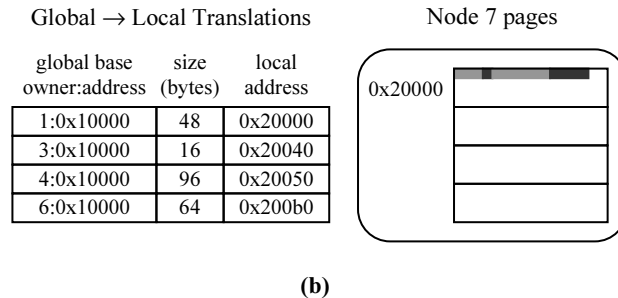
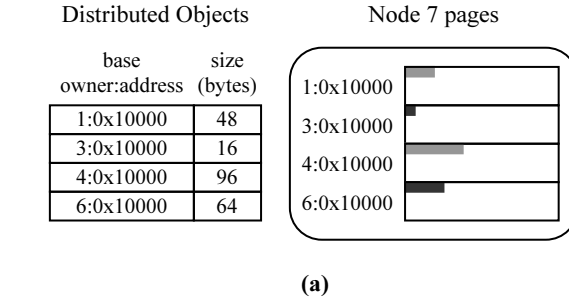
Distributed objects are allocated using extended address partitioning by reserving the same address range on all nodes. Capabilities for these objects are of type *sparse*; the term “sparse” reflects the fact that while an object is conceptually allocated on all nodes, its facets may physically exist only on a small subset of nodes. There are two differences between sparse capabilities and data capabilities. First, when a sparse capability is created the owner field is automatically set (recall that the owner field is used for subsegments in data capabilities; subsegmenting of a sparse capability is not allowed). Second, the node field of the address may be altered freely using pointer arithmetic or indexing. The remaining capability fields have the same meaning in both capability types. In particular B, L and K have the same values that they would if the specified address range had been allocated on a single node only.

In a capability architecture such as Hamal, no special hardware mechanism is required to implement lazy allocation of physical memory; it suffices to make use of page faults. This is because capabilities guarantee that all pointers are valid, so a page fault on a non-existent page always represents a page that needs to be created and initialized, and never represents an

application error. As a result, no communication needs to take place between the allocating node and the nodes on which the object is stored other than the capability itself, which is included in memory requests involving the object.

### 3.4.2 Sparsely Faceted Arrays

A problem with extended address partitioning is that the facets of distributed objects allocated by different nodes must reside in different physical pages, which can result in significant fragmentation and wasted physical memory. This is illustrated by Figure 3-8a, which shows how the facets of four distributed objects allocated by four different nodes are stored in memory on a fifth node. Four pages are required to store the facets, and most of the space in these pages is unused.



**Figure 3-8: (a) Extended address partitioning results in fragmentation. (b) Address translation allows facets to be allocated contiguously.**

Sparsely faceted arrays (SFAs) are a solution to this problem described in [Brown02a]. The central idea is to perform a translation from global array names (which consist of the owner node and the base address on that node) to local addresses. This extra layer of translation allows facets to be

allocated contiguously, even intermingled with local data, regardless of the nodes on which the SFAs were allocated (Figure 3-8b).

SFAs require a translation table to exist at the boundary of each processing node in order to translate local addresses to/from global array names. When a SFA pointer moves from a node to the network, it is first decomposed into a base address and an offset. The base address is used to look up the array's global name in the translation table. Similarly, when a SFA pointer arrives at a node, the owner and base address are used to look up the local facet base address in the translation table. If no entry exists in the table, which occurs the first time a node sees a pointer to a given SFA, then a local facet is allocated and the base address is entered into the table. Note that no translation is required at the boundary of the owner node.

SFA capabilities in the Hamal architecture have type *translated sparse*, or *xsparse*. They are exactly the same as sparse capabilities, and are only treated differently by the network interface which recognizes them and automatically performs translations. In particular, the owner field is still set automatically when an xsparse capability is created. While this is not strictly necessary for a SFA implementation, it has two advantages. First, it allows the network interface to detect xsparse capabilities that are locally owned, so the null local  $\leftrightarrow$  global translation for this case can be omitted from the translation table. Second, it avoids the need to expand xsparse capabilities from 128 to  $128 + \log N$  bits to include the owner node when they are transmitted across the network. Each network interface has a 256-entry translation cache and can perform a single translation on each cycle. In the case of a cache miss, an event is generated which must be handled by the microkernel.

### 3.4.3 Comparison of the Two Approaches

Each of these approaches has benefits and disadvantages. Extended address partitioning has very low overhead and is inherently scalable. It has the additional advantage of enlarging the virtual address space. However, it can suffer from significant fragmentation problems. Sparsely faceted arrays eliminate fragmentation, but require translation tables to be stored at individual nodes which can potentially affect the scalability of the system. These tables do not store global information as translations are locally generated and managed, but it is not clear how quickly they will grow over time or with machine size, and some sort of translation garbage collection would be required to prevent the tables from becoming arbitrarily large. Another issue is the performance degradation which occurs if the working set of SFAs on some node exceeds the size of the hardware translation table. It is impossible to determine *a priori* which approach is to be preferred; most likely this is application-dependent. We have therefore chosen to implement both mechanisms in the Hamal architecture.

#### 3.4.4 Data Placement

If an application programmer has specific knowledge concerning the physical layout of the processor nodes and the topology of the network that connects them, it may be desirable to specify not only that an object is to be distributed, but also the exact mapping of facets to physical nodes. The ability to do so has been integrated into the High Performance Fortran language [Koelbel94], and some parallel architectures provide direct hardware support. The M-Machine has a global translation mechanism which allows large portions of the virtual address space to be mapped over rectilinear subsets of the system's three dimensional array of nodes [Dally94b]. In the Tera Computer System, consecutive virtual addresses in a segment may be distributed among any power of two number of memory units [Alverson90]. The Cray T3E features an *address centrifuge* which can extract user-specified bits from a virtual address and use them to form the ID for the node on which the data resides [Scott96].

The Hamal processor contains no global segment or translation tables; virtual addresses are routed to physical nodes based exclusively on the upper address bits. To compensate for this somewhat rigid mapping and to allow applications to lay out an object in a flexible manner without performing excessive computation on indices, a hardware *swizzle* instruction is provided. This instruction combines a 64 bit operand with a 64 bit mask to produce a 64 bit result by right-compacting the operand bits corresponding to 1's in the mask, and left-compacting the operand bits corresponding to 0's in the mask. *swizzle* is a powerful bit-manipulation primitive with a number of potential uses. In particular, it allows an address centrifuge to be implemented in software using a single instruction.

### 3.5 Memory Semantics

Sequential consistency presents a natural and intuitive shared memory model to the programmer. Unfortunately, it also severely restricts the performance of many parallel applications ([Gharach91], [Zucker92], [Chong95]). This is due to the fact that no memory operation from a given thread may proceed until the effect of every previous memory operation from that thread is globally visible in the machine. This problem becomes worse as machine size scales up and the average round trip time for a remote memory reference increases.

In order to maximize program efficiency, Hamal makes no guarantees concerning the order in which references to different memory locations complete. Memory operations are explicitly split-phase; a thread continues to execute after a request is injected into the system, and at some unknown time in the future a reply will be received. The hardware will only force a thread to stall in three circumstances:

1. The result of a read is needed before a reply containing the value is received
2. There is a RAW, WAR or WAW hazard with a previous memory operation
3. The hardware table used to keep track of incomplete memory operations is full

A *wait* instruction is provided to force a thread to stall until all outstanding memory operations have completed. This allows release consistency [Gharach90] to be efficiently implemented in software.

# Chapter 4

## Processor Design

*Everything should be made as simple as possible, but not simpler.*

– Albert Einstein (1879-1955)

The Hamal architecture features 128 bit multithreaded Very Long Instruction Word (VLIW) processors. There are eight hardware contexts; of these, context 0 is reserved for the event-driven microkernel, and contexts 1-7 are available for running user programs. Instructions may be issued from a different context on each cycle, and instructions from multiple contexts may complete in a given cycle. Each context consists of an instruction cache, a trace controller (which fetches instructions from the instruction cache and executes control flow instructions), issue logic, 32 128-bit tagged general purpose registers, 15 single-bit predicate registers, and a small number of special-purpose registers.

Each VLIW instruction group consists of three instructions and an immediate. One instruction is an arithmetic instruction which specifies up to two source operands and a destination register. One instruction is a memory instruction which specifies up to three source operands (address, index, data) and a destination register; this can also be a second arithmetic instruction for certain simple single-cycle operations. The last instruction is a control flow instruction which specifies zero or one operands. Predicated execution is supported; each instruction within an instruction group can be independently predicated on the value (true or false) of any one the 15 predicates.

This chapter gives an overview of, and provides motivation for, the key features of the Hamal processor. These features represent various tradeoffs involving the five design principles outlined in Section 2.1: scalability, silicon efficiency, simplicity, programmability, and performance. A more detailed description of the processor can be found in [Grossman01a] and [Grossman01b].

## 4.1 Datapath Width and Multigranular Registers

The choice of 128 bits as the basic datapath and register width was motivated by two factors:

1. Capabilities are 128 bits, so at least some datapaths must be this wide
2. Wide datapaths make effective use of the available embedded DRAM bandwidth

A criticism of wide datapaths is that large portions of the register file and/or functional units will be unused for applications which deal primarily with 32 or 64 bit data, significantly reducing the area efficiency of the processor. This issue is addressed in two ways. First, each register is addressable as a single 128 bit register, two 64 bit registers, or four 32 bit registers (Figure 4-1). This requires a small amount of shifting logic to implement in hardware, and increases both the register file utilization and the number of registers available to user programs. Second, many of the instructions can operate in parallel on two sets of 64 bit inputs or four sets of 32 bit inputs packed into 128 bits. This provides the opportunity to increase both performance and functional unit usage via fine-grained SIMD parallelism. Note that, for the purpose of scoreboarding, busy bits must be maintained for the finest register granularity; a register is marked as busy by setting the busy bits of all of its sub-registers.

r3	r2y	r2x	r1y	r1b	r1a	r0d	r0c	r0b	r0a
r7	r6		r5			r4			
r11	r10		r9			r8			
r15	r14		r13			r12			
⋮									

Figure 4-1: Multigranular general purpose registers.

## 4.2 Multithreading and Event Handling

Multithreading is a very well known technique. In [Agarwal92] and [Thekath94] it is shown that hardware multithreading can significantly improve processor utilization. A large number of designs have been proposed and/or implemented which incorporate hardware multithreading; examples include HEP [Smith81], Horizon [Thistle88], MASA [Halstead88], Tera [Alverson90], April [Agarwal95], and the M-Machine [Dally94b]. Most of these designs are capable of executing instructions from a different thread on every cycle, allowing even single-cycle pipeline bubbles in one thread to be filled by instructions from another. An extreme model of multithreading, variously proposed as processor coupling [Keckler92], parallel multithread-

ing [Hirata92] and simultaneous multithreading [Tullsen95], allows multiple threads to issue instructions during the *same* cycle in a superscalar architecture. This has been implemented in the Intel Pentium 4 Xeon architecture [Marr02].

The idea of using multithreading to handle events is also not new. It is described in both [Keckler99] and [Zilles99], and has been implemented in the M-Machine [Dally94b]. Using a separate thread to handle events has been found to provide significant speedups. In [Keckler99] these speedups are attributed to three primary factors:

1. No instructions need to be squashed
2. No contexts need to be saved and subsequently restored
3. Threads may continue to execute concurrently with the event handler

In the Hamal architecture, events are placed in a hardware event queue. Events may be generated by memory (e.g. page faults), the network interface (e.g. xsparse translation cache misses) or by the processor itself (e.g. thread termination). The size of the event queue is monitored in hardware; if it grows beyond a high-water mark, certain processor activities are throttled to prevent new events from being generated, thus avoiding event queue overflow and/or deadlock. A special *poll* instruction allows context 0 to remove an event from the queue; information concerning the event is placed in read-only event registers. The Hamal event-handling model is illustrated in Figure 4-2.

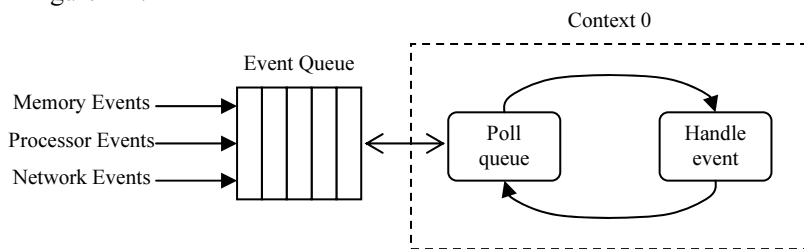


Figure 4-2: Event queue and event handler context.

### 4.3 Thread Management

One of the requirements for efficient fine-grained parallelism is a set of lightweight mechanisms for thread management. This is made possible in the Hamal architecture via hardware support for thread *swap pages*. Each thread is explicitly assigned to a page in memory; the virtual address of this page is used to identify the thread. All major thread management operations are performed by single instructions, issued from context 0, which specify a thread swap address as their argument. Context loading and



unloading is performed in the background while the processor continues to execute instructions, as described in [Soundarar92].

#### 4.3.1 Thread Creation

Threads are created in the Hamal architecture using a *fork* instruction which specifies a code starting address for the new thread and a subset of the 32 general purpose registers to copy into the thread. The upper bits of the starting address indicate the node on which the new thread should be created (code capabilities, like sparse capabilities, allow the node field of the address to be changed via pointer arithmetic and indexing). When a fork request has arrived at the destination node (which may be the same node that issued the *fork* instruction), it is placed in a hardware fork queue. Each node has an eight-entry FIFO queue for storing fork requests; when the queue fills fork instructions on that node are not allowed to issue, and fork packets received from the network cannot be processed. Each time a fork is placed in the queue a fork event is generated. The microkernel can handle this event in one of two ways: it can issue an *fload* instruction to immediately load the new thread into a free context and activate it, or it can issue an *fstore* instruction to write the new thread to memory. Both of these instructions specify as their single operand a swap address for the new thread.

#### 4.3.2 Register Dribbling and Thread Suspension

One of the challenges of fine-grained parallelism is deciding when a thread should be suspended; it is not even clear whether this decision should be made by hardware or software. The problem is that it is difficult or impossible to predict how long a blocked thread will remain inactive, particularly in a shared-memory system with no bounds on the amount of time required for a remote access to complete. In order to minimize the likelihood of suspending a thread that would have become unblocked a short time in the future while at the same time attempting to keep the processor active, the Hamal processor waits until no forward progress is being made by *any* context. If there less than two free contexts, it then generates a *stall* event without actually suspending any threads, informing the microkernel of the least-recently-issued (LRI) thread and allowing it to make the final decision as to whether or not this thread should be suspended. Hamal uses dribbling registers [Soundarar92] to minimize the cost of a context switch; the processor is always dribbling the LRI context to memory. This dribbling is included in the determination of forward progress, hence a stall event is not generated until the LRI context is clean *and* no context can issue.

## 4.4 Register-Based Synchronization

Hamal supports register-based synchronization through the use of *join* capabilities. A join capability allows one thread to write directly to the register file of another. Three instructions are provided to support this type of synchronization: *jcap*, *busy*, and *join*. *jcap* creates a join capability and specifies the intended destination register as its argument. *busy* sets the scoreboard busy bit(s) associated with a register, simulating the effect of a high-latency memory request. Finally, *join* takes as arguments a join capability and data and writes the data directly to the destination register specified by the capability. When a join is received, the appropriate busy bit(s) are cleared.

gives a simple example of how these instructions can be used: a parent thread creates a child thread and supplies it with a join capability; the child thread uses this capability to inform the parent thread that it has finished its computation.

parent thread	child thread
<pre>r0 = jcap r1a r1a = busy fork _child_thread, {r0} r1a = and r1a, r1a</pre>	<pre>_child_thread: &lt;computation&gt; join r0, 0</pre>

Figure 4-3: Register-based synchronization example.

## 4.5 Shared Registers

Eight 128-bit shared registers are visible to all contexts. They may be read by any thread, but may be modified only by programs running in privileged mode. Their purpose is to hold shared kernel data, such as allocation counters and code capabilities for commonly-called kernel routines.

## 4.6 Hardware Hashing

Hashing is a fundamental technique in computer science which deterministically maps large data objects to short bit-strings. The ubiquitous use of hashing provides motivation for hardware support in novel processor architectures. The challenge of doing so is to design a single hash function with good characteristics across a wide range of applications.

The most important measure of a hash function's quality is its ability to minimize *collisions*, instances of two different inputs which map to the same output. In particular, similar inputs should have different outputs, as many applications must work with clusters of related objects (e.g. similar variable names in a compiler, or sequences of board positions in a chess program). While the meaning of "similar inputs" is application-dependent,

one simple metric that can be applied in any circumstance is *hamming distance*; the number of bits in which two inputs differ. We define the *minimum collision distance* of a hash function to be the smallest positive integer  $d$  such that there exist two inputs separated by hamming distance  $d$  that map to the same output.

For an  $n$  bit input,  $m$  bit output hash function, the goal is to maximize the minimum collision distance. The problem is that the number of required input and output bits varies greatly from application to application. A hardware hash function must therefore choose  $n$  and  $m$  large enough so that applications can simply use as many of the least significant input and output bits as they need. It is therefore not enough to ensure that this  $n \rightarrow m$  hash function has a good minimum collision distance, for if the outputs of two similar inputs differ only in their upper bits, then these two inputs will collide in applications that discard the upper output bits.

In this section we will show how to construct a single  $n \rightarrow m$  hash function which is easy to implement in hardware and has the property that the  $n \rightarrow m'$  *subhashes* obtained by discarding the upper  $m - m'$  output bits all have good minimum collision distances. Our approach is to construct a nested sequence of linear codes; we will begin with a brief review of these codes and their properties. Note that it suffices to consider the size of the outputs, as any  $n' \rightarrow m$  subhash obtained by forcing a set of  $n - n'$  input bits to zero will have a minimum collision distance at least as large as that of the original  $n \rightarrow m$  hash.

#### 4.6.1 A Review of Linear Codes

An  $(n, k)$  binary linear code  $C$  is a  $k$ -dimensional subspace of  $\text{GF}(2)^n$ . A *generator matrix* is any  $k \times n$  matrix whose rows form a basis of  $C$ . A generator matrix  $\mathbf{G}$  defines a mapping from  $k$ -dimensional input vectors to code words; given a  $k$ -dimensional row vector  $\mathbf{v}$ , the corresponding code word is  $\mathbf{v}\mathbf{G}$ . A *parity check matrix* is any  $(n - k) \times n$  matrix whose rows form a basis of  $C^\perp$ , the subspace of  $\text{GF}(2)^n$  orthogonal to  $C$ . A parity check matrix  $\mathbf{H}$  has the property that an  $n$ -dimensional vector  $\mathbf{w}$  is a code word if and only if  $\mathbf{w}\mathbf{H}^\top = 0$ .

The *minimum distance* of a code is the smallest hamming distance  $d$  between two different code words. For a binary linear code, this is also equal to the smallest weight (number of 1's) of any non-zero code word. The quality of a code is determined by its minimum distance, as this dictates the number of single-bit errors that can be tolerated when code words are communicated over a noisy channel. Maximizing  $d$  for a particular  $n$  and  $k$  is an open problem, with upper limits given by the non-constructive Johnson bound [Johnson62]. The best known codes tend to come from the Bose-Chaudhury-Hocquenghem (BCH) [Kasami69] or Extended BCH [Edel97] constructions.

A BCH code with minimum distance  $d$  is constructed as follows. Choose  $n$  odd, and choose  $q$  such that  $n$  divides  $2^q - 1$ . Let  $\beta$  be an order  $n$  element of  $\text{GF}(2^q)$ , and let  $j$  be an integer relatively prime to  $n$ . Finally, let  $g$  be the least common multiple of the minimal polynomials of  $\beta^j, \beta^{j+1}, \beta^{j+2}, \dots, \beta^{j+d-2}$  over  $\text{GF}(2)$ . The code words are then the coefficients of the polynomials over  $\text{GF}(2)$  with degree  $< n$  which are divisible by  $g$ . If  $g$  has degree  $m$ , this defines an  $(n, n - m)$  linear code with minimum distance  $\geq d$ .

#### 4.6.2 Constructing Hash Functions from Linear Codes

Let  $\mathbf{H}$  be a parity check matrix for an  $(n, k, d)$  linear code (the third parameter in this notation is the minimum distance). Let  $H()$  be the linear  $n \rightarrow k$  hash function defined by  $H(\mathbf{v}) = \mathbf{v}\mathbf{H}^T$ . For any two input vectors  $\mathbf{x}$  and  $\mathbf{y}$ , we have  $H(\mathbf{x}) = H(\mathbf{y}) \Leftrightarrow \mathbf{x}\mathbf{H}^T = \mathbf{y}\mathbf{H}^T \Leftrightarrow (\mathbf{x} - \mathbf{y})\mathbf{H}^T \Leftrightarrow \mathbf{x} - \mathbf{y}$  is a code word. It follows that the minimum collision distance of  $H()$  is the smallest weight of any non-zero code word, which is equal to  $d$ . We can therefore apply the theory of error-correcting codes to the construction of good hash functions.

Next, suppose that  $C_1$  is an  $(n, k_1, d_1)$  linear code and  $C_2$  is an  $(n, k_2, d_2)$  subcode of  $C_1$  (so  $k_2 < k_1$  and  $d_2 \geq d_1$ ). Let  $\mathbf{H}_1$  be a parity check matrix for  $C_1$ . Since  $C_2 \subset C_1$ , we have  $C_1^\perp \subset C_2^\perp$ , so the rows of  $\mathbf{H}_1$ , which form a basis of  $C_1^\perp$ , can be extended to a basis of  $C_2^\perp$ . Let  $\mathbf{H}_2$  be the matrix whose rows are the vectors of this extended basis, ordered so that the bottom  $n - k_1$  rows of  $\mathbf{H}_2$  are the same as the rows of  $\mathbf{H}_1$ . Then  $\mathbf{H}_2$  is a parity check matrix for  $C_2$ , and the hash function  $H_1()$  is the subhash of  $H_2()$  obtained by discarding the  $k_1 - k_2$  leftmost output bits. It follows that we can construct an  $n \rightarrow m$  hash function whose subhashes have good minimum collision distances by constructing a nested sequence  $C_{n-m} \subset C_{n-m+1} \subset C_{n-m+2} \subset \dots$  of linear codes where  $C_k$  is an  $(n, k, d_k)$  code with  $d_k$  as large as possible.

#### 4.6.3 Nested BCH Codes

Assume for now that  $n$  is odd; we construct a nested sequence of BCH codes as follows. Choose  $q, \beta$ , and  $j$  as described in Section 4.6.1. For  $d \geq 2$ , let  $g_d$  be the least common multiple of the minimal polynomials of  $\beta^j, \beta^{j+1}, \dots, \beta^{j+d-2}$ , let  $m_d = \deg(g_d)$ , and let  $B_d$  be the resulting  $(n, n - m_d)$  BCH code with minimum distance  $\geq d$ . Since  $g_d$  divides  $g_{d+1}$ , it follows from the BCH construction that all the code words of  $B_{d+1}$  are also code words of  $B_d$ , hence  $B_2 \supset B_3 \supset B_4 \supset \dots$

We can use this nested sequence of BCH codes to construct the desired sequence  $C_{n-m} \subset C_{n-m+1} \subset C_{n-m+2} \subset \dots$  of linear codes, assuming still that  $n$  is odd. Start by choosing  $D$  large enough so that  $m_D \geq m$ . Construct a basis  $\{b_i\}$  of  $B_2$  by choosing the first  $n - m_D$  vectors to be a basis of  $B_D$ ,

choosing the next  $m_D - m_{D-1}$  vectors to extend this basis to a basis of  $B_{D-1}$ , and so on, choosing the last  $m_3 - m_2$  vectors to extend the basis of  $B_3$  to a basis of  $B_2$ . Finally, for  $n - m \leq k \leq n - m_2$  let  $C_k = \text{span}\{b_1, b_2, \dots, b_k\}$ . Then  $\{C_k\}$  is an increasing sequence of nested codes. When  $k = n - m_d$  for some  $d$ ,  $C_k = B_d$  and therefore  $C_k$  has minimum distance  $\geq d$ . At this point we note that we can construct the  $\{C_k\}$  with  $n$  even by first using  $n - 1$  to construct the  $\{b_i\}$ , then adding a random bit to the end of each  $b_i$ . This has the effect of simultaneously extending the  $\{C_k\}$  from  $(n - 1, k)$  codes to  $(n, k)$  codes, and does not decrease their minimum distances. Note that in this case  $k$  ranges from  $n - m$  to  $n - 1 - m_2$ .

#### 4.6.4 Implementation Issues

Assume for the remainder that  $n$  is even (we are, after all, interested in a hardware implementation, and in computer architecture all numbers are even). Using the technique described in Section 4.6.2 we can construct a parity check matrix  $\mathbf{H}_k$  for each code  $C_k$  such that for  $n - m \leq k \leq n - 1 - m_2$ ,  $\mathbf{H}_k$  consists of the bottom  $n - k$  rows of  $\mathbf{H}_{n-m}$ . This gives us an  $n \rightarrow m$  hash function  $H_{n-m}()$  whose subhashes, obtained by discarding up to  $m - m_2 - 1$  of the leftmost output bits, all have provably good minimum collision distances.

We can manipulate the rows and columns of  $\mathbf{H}_{n-m}$  to improve the properties of the hash function. Permissible operations are to permute the columns or the bottom  $m_2 + 1$  rows, or to add two rows together and replace the upper row with the sum (not the lower row, as this would destroy the properties of the subhashes). There are three ways in which it is desirable to improve the hash function. First, the weights of the rows and columns should be as uniform as possible so that each input bit affects the same number of output bits and each output bit is affected by the same number of input bits. Additionally, the maximum row weight should be as small as possible as this determines the circuit delay of a hardware implementation. Second, as many as possible of the  $m' \times m'$  square submatrices in the lower right-hand corner should have determinant 1, so that the  $m' \rightarrow m'$  subhashes are permutations. Finally, the BCH construction provides poor or no lower bounds for the minimum collision distance of the  $n' \rightarrow m'$  subhashes with  $n' < n$  and  $m' < m_4 + 1$ . We can attempt to improve these small subhashes using the following general observations. If the hash function corresponding to a matrix  $\mathbf{H}$  has minimum collision distance  $d$ , then:

1.  $d > 1$  if the columns of  $\mathbf{H}$  are all non-zero
2.  $d > 2$  if in addition the columns of  $\mathbf{H}$  are distinct
3.  $d > 3$  if in addition the columns of  $\mathbf{H}$  all have odd weight

The proofs of (1) and (2) are trivial; the proof of (3) is the observation that vector addition over  $\text{GF}(2)$  preserves parity, so three columns of odd

weight cannot sum to zero. As a final note, linear hash functions are straightforward to implement in hardware as each output bit is simply the XOR of a number of input bits.

#### 4.6.5 The Hamal *hash* Instruction

The Hamal architecture implements a  $256 \rightarrow 128$  hash function constructed as described in the previous sections; the *hash* instruction takes two 128 bit inputs and produces a 128 bit output. Figure 4-4 plots the minimum collision distance  $d$  of the  $256 \rightarrow m$  subhashes against the best known  $d$  for independently constructed linear hash functions of the same size. We see that for many values of  $m$  the minimum collision distance of the subhash is optimal.

The hash matrix was manipulated as described in Section 4.6.4. The weight of all rows in the resulting matrix is 127 with one exception of weight 128. All  $128 \rightarrow m$  subhashes are permutations. For small  $n' \rightarrow m'$  hashes, we chose to optimize the particular common case  $m' = 8$ . The  $256 \rightarrow 8$  subhash has  $d = 2$ . The  $128 \rightarrow 8$  subhash has  $d = 3$ . For  $n_1 \leq 64$  and  $n_2 \leq 32$ , the  $(n_1, n_2) \rightarrow 8$  subhashes, obtained by supplying  $n_1$  bits to the first operand and  $n_2$  bits to the second operand of the *hash* instruction, all have  $d \geq 4$ .

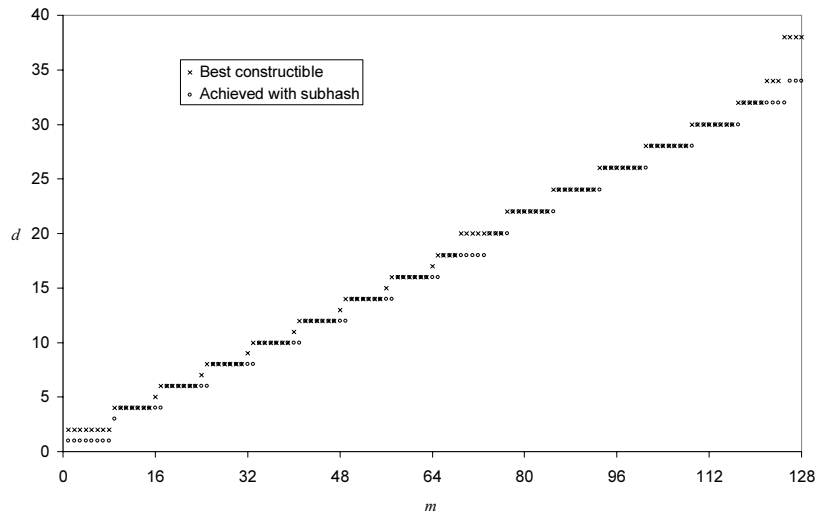


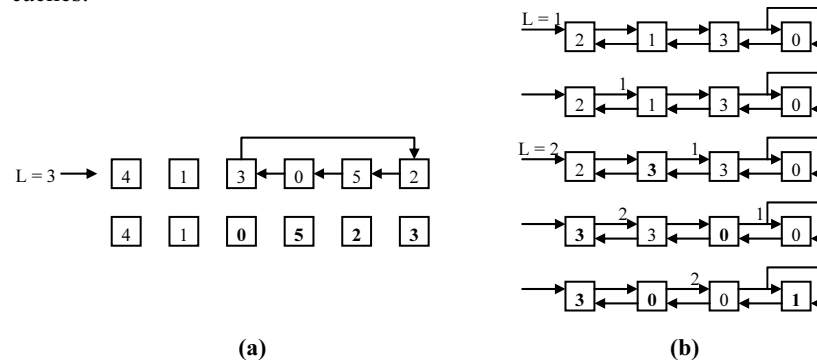
Figure 4-4: Best constructible vs. achieved minimum collision distance  $d$  for  $256 \rightarrow m$  hashes.

## 4.7 Instruction Cache

Each context in the Hamal processor contains a 64 entry, single cycle access, fully associative instruction cache. Each of the 64 cache lines is 1024 bits long and holds 8 consecutive VLIW instruction groups. When a cache line is accessed, the next 8 instruction groups are prefetched from instruction memory if they are not already present in the cache. In this section we present two mechanisms used to optimize cache line replacement.

### 4.7.1 Hardware LRU

Implementing a least recently used (LRU) policy is difficult in caches with high degrees of associativity. As a result, hardware designers generally opt for simpler replacement strategies such as round-robin [Clark01], even though the LRU policy is known to provide better performance [Smith82]. The Hamal instruction cache uses a systolic array to maintain exact LRU information for the cache lines. Since the length of the critical path in a systolic array is constant, this approach is suitable for arbitrarily associative caches.

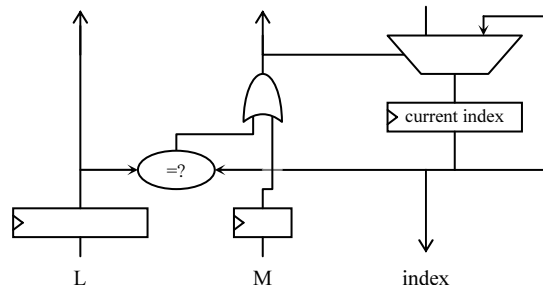


**Figure 4-5: Maintaining LRU information using (a) an atomically updated list (b) a systolic array.**

The central idea is to maintain a list of cache line indices sorted from LRU to MRU (most recently used). When a cache line is accessed its line index  $L$  is presented to the list, and that index is rotated to the MRU position at the end (Figure 4-5a). We can implement this list as a systolic array by advancing  $L$  one node per clock cycle, along with a single-bit “matched” signal  $M$ , indicating whether or not the index has found a match within the array. Until a match is found,  $L$  is advanced without any changes being made. Once a match is found, nodes begin copying values from their neighbours to the right. Finally,  $L$  is deposited in the last node. This is illustrated in Figure 4-5b. We can use the same design for all nodes by wiring together the last node’s inputs, as shown in Figure 4-5b. This ensures

that  $L$  will be deposited because by the end of the array we are guaranteed that  $M = 1$ , so the last node will attempt to copy a value from the right, and with the inputs wired together this value is  $L$ . Note that we can only present indices to the array on every other cycle. For example, if in Figure 4-5b '2' were presented on the cycle immediately following '1', then the value '1' would erroneously be copied into the first node instead of the correct '3'.

Figure 4-6 shows a hardware implementation of the systolic array node. The forward signals are the line index  $L$  and the match bit  $M$ ; the backward signal is the current index which is used to shift values when  $M = 1$ . The node contains two  $\log N$  bit registers (where  $N$  is the degree of associativity), one single-bit register, a  $\log N$  bit multiplexer, a  $\log N$  bit comparator, and an OR gate. No extra hardware is required to set up the array as it can be initialized simply by setting  $M = 1$  and presenting all  $N$  line indices in  $N$  consecutive cycles followed by  $N$  copies of the last index ( $N - 1$ ) in the next  $N$  consecutive cycles.



**Figure 4-6: Systolic array node.**

In normal operation the input  $M$  to the first node is always 0. On a cache hit, the line index  $L$  is presented to the array. On a cache miss, the output of the first node gives the LRU line index; this line is replaced and the index is fed back into the array. On a cycle with no cache activity, the index of the most recently accessed line is presented, which does not change the state of the array (this technique avoids the need for a separate "valid" bit).

We can modify the systolic array to accommodate one cache line access per cycle simply by removing every other set of forward registers and altering the backward 'index' signal slightly to obtain the new node implementation shown in Figure 4-7. The index signal is taken from the input rather than the output of the bottom register to ensure that when the previous node attempts to copy the index value, it obtains the value that would be stored in this register *after* the node has finished processing its current inputs. This new systolic array, which contains  $N/2$  nodes, can be initialized by presenting all  $N$  line indices in  $N$  consecutive cycles with  $M = 1$ .



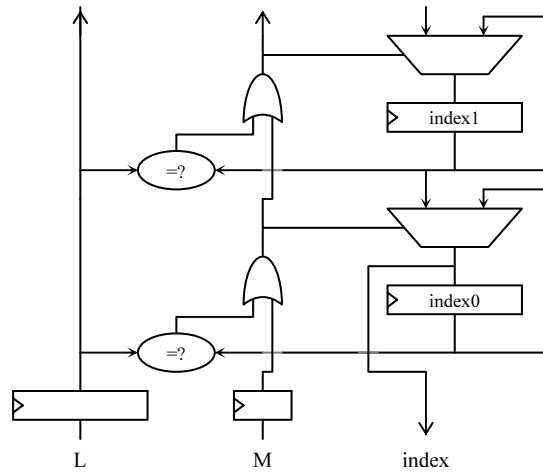


Figure 4-7: Modified systolic array node.

#### 4.7.2 Miss Bits

Simple prefetching can be used to avoid cache misses in straight-line code. This leads to the observation that there is no need to maintain such code in the instruction cache. It suffices to keep one cache line containing the first instruction group in the basic block; the rest of the instructions will be automatically prefetched when the code is executed. The Hamal instruction cache takes advantage of this observation by adding a *miss bit* to each cache line. The bit is set for lines that were loaded in response to a cache miss, and clear for lines that were prefetched. The instruction cache is then able to preferentially replace those lines which are likely to be successfully prefetched the next time they are required. This scheme requires a slight modification to the LRU systolic array so that the line indices are sorted first by miss bits and then by LRU.

Making use of miss bits is similar to the use of a *branch target buffer* [Kronstadt87], but differs in that it more precisely identifies those lines which cannot be successfully prefetched. In particular, the branch targets of short forward or backward branches may be successfully prefetched, whereas the cache line following a branch target may *not* be successfully prefetched if, for example, the branch target is the last instruction group in its cache line.

# Chapter 5

## Messaging Protocol

*What I tell you three times is true.*

– Lewis Carroll (1832-1898), “The Hunting of the Snark”

In large parallel machines, the implementation of the network has a first order effect on the performance characteristics of the system. Both the network topology and the messaging protocol must be carefully chosen to suit the needs of the architecture and its target applications. One of the first decisions that designers must face is whether the responsibility for successful packet delivery should be placed on the network or the processing nodes.

If it is the network’s responsibility, then packets injected into the network are precious and must not be corrupted or lost under any circumstances. Network nodes must contain adequate storage to buffer packets during congestion, and some strategy is required to prevent or recover from deadlock. The mechanical design of the network must afford an extremely low failure rate, as a single bad component or connection can result in system failure. Many fault-tolerant routing strategies alleviate this problem somewhat by allowing the system to tolerate static detectable faults at the cost of increased network complexity and often reduced performance. Dynamic or undetected faults remain a challenge, although techniques have been described to handle the dynamic failure of a *single* link or component ([Dennison91], [Dally94a], [Galles96]).

If, on the other hand, responsibility for message delivery is placed on the processing nodes, network design is simplified enormously. Packets may be dropped if the network becomes congested. Components are allowed to fail arbitrarily, and may even be repaired online so long as at least one routing path always exists between each pair of nodes. Simpler control logic allows the network to be clocked at a higher speed than would otherwise be possible ([DeHon94], [Chien98]).

The cost, of course, is a more complicated messaging protocol which requires additional logic and storage at each node, and reduces the performance of the system. Thus, with few nodes (hundreds or thousands), it is

likely a good tradeoff to place extra design effort into the network and reap the performance benefits of guaranteed packet delivery. However, as the scale of the machine increases to hundreds of thousands or even millions [IBM01] of nodes and the number of discrete network components is similarly increased, it becomes extremely difficult to prevent electrical or mechanical failures from corrupting packets within the network. There is therefore a growing motivation to accept the possibility of network failure and to develop efficient end-to-end messaging protocols.

Any fault-tolerant messaging protocol must have the following two properties:

- i. **delivery:** All messages must be successfully delivered at least once.
- ii. **idempotence:** Only one action must be taken in response to a given message even if duplicates are received.

Additionally, for a protocol to be scalable to large systems, it should exhibit these properties without storing global information at each node (e.g. sequence numbers for packets received from every other node). In light of this restriction, the idempotence property becomes more of a challenge.

In this chapter we develop a lightweight fault-tolerant idempotent messaging protocol that is easy to implement in hardware and has been incorporated into the Hamal architecture. Each communication is broken down into three parts: the *message*, sent from sender to receiver, the *acknowledgement*, sent from receiver to sender to indicate message reception, and the *confirmation*, sent from sender to receiver to indicate that the message will not be re-sent. For the most part the protocol arises fairly naturally from the *delivery* and *idempotence* requirements as well as the restriction that global information may not be stored at each node. There are some subtleties, however, that must be addressed in order to ensure correctness. We begin with the assumption that the network does not reorder packets; in Section 5.3 we will see how this restriction can be relaxed.

## 5.1 Previous Work

The vast majority of theoretical and applied work in interconnection networks has focused on fault-tolerant routing strategies for non-discarding networks. While specific types of operations may be transformed into idempotent forms for repeated transmission over unreliable networks [Elick94], no general mechanism providing lightweight end-to-end idempotence has previously been reported. As a result, most previous and existing parallel architectures have implemented non-discarding networks ([Hwang93], [Ni93], [Culler99]).

The practice of discarding packets is common among WAN networking technologies such as Ethernet [Metcalfe83] and ATM [Rooholamini]; end-to-end protocols such as TCP [Postel81] are required to ensure reliable message delivery over these networks. However, WAN-oriented protocols generally require total table storage proportional to  $N^2$  for  $N$  intercommunicating nodes ([Dennison91], [Dally93]), and are therefore poorly suited to large distributed shared-memory machines.

Only a few parallel architectures feature networks which may discard packets; among these exceptional cases are the BBN Butterfly [Rettburg86], the BBN Monarch [Rettburg90], and the Metro router architecture [DeHon94]. Each of these implements a circuit-switched network which discards packets in response to collisions or network faults.

The protocol presented in this chapter was first described in [Brown01] and was implemented as part of a faulty network simulation in [Woods01].

## 5.2 Basic Requirements

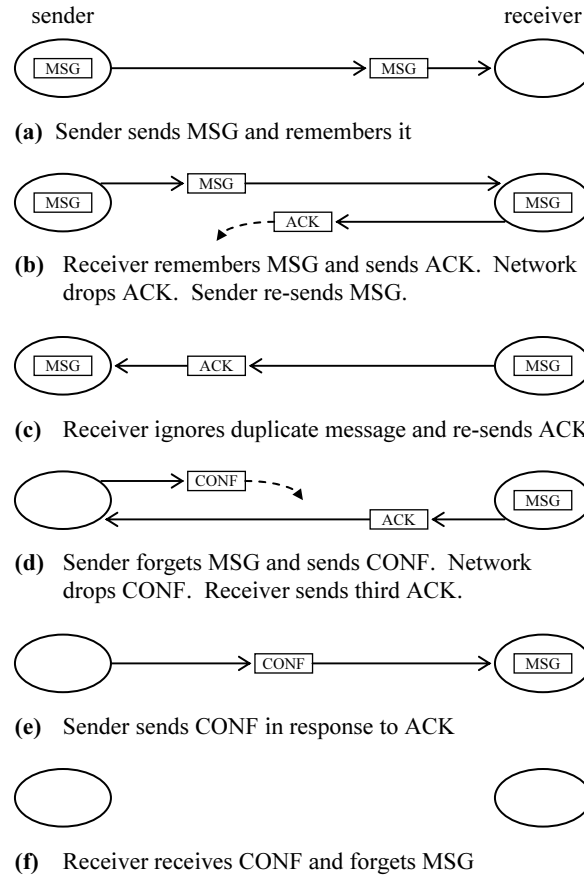
The message-acknowledge pair is fundamental to any end-to-end messaging protocol. The sender has no way of knowing whether or not a message was successfully delivered, so it must remember and periodically re-send the message until an acknowledgement (ACK) is received at which point it can forget the message.

Because a message can be sent (and therefore received) multiple times, the receiver must somehow remember that it has already acted on a given message in order to preserve message idempotence. One approach, used in the TCP protocol [Postel81], is to sequentially generate packet numbers for every sender-receiver pair; each node then remembers the last packet number that it received from every other node. This approach is feasible with thousands of nodes, but the memory requirements are likely to be prohibitive in machines with millions of nodes.

Without maintaining this type of global information at each node, the only way to ensure message idempotence is to remember individual messages that have been received. To ensure correctness, each message must be remembered until a guarantee can be made that no more duplicates will be received. This, however, depends on a remote event, specifically the successful delivery of an ACK to the sender. Only the sender knows when no more copies of the message will be sent, and so we require a third confirmation (CONF) packet to communicate this information to the receiver.

We thus have our three-part idempotent messaging protocol. The sender periodically sends a message (MSG) until an ACK is received, at which point it can drop the message. Once a message is received, the receiver ignores duplicates and periodically sends back an ACK until a CONF is received, at which point it can forget about the message. Finally, each time that a sender receives an ACK it responds with a CONF to indicate

that the message will not be resent. This is illustrated in Figure 5-1, which shows how the protocol is able to deal with arbitrary packets being lost.



**Figure 5-1: Idempotent messaging example.**

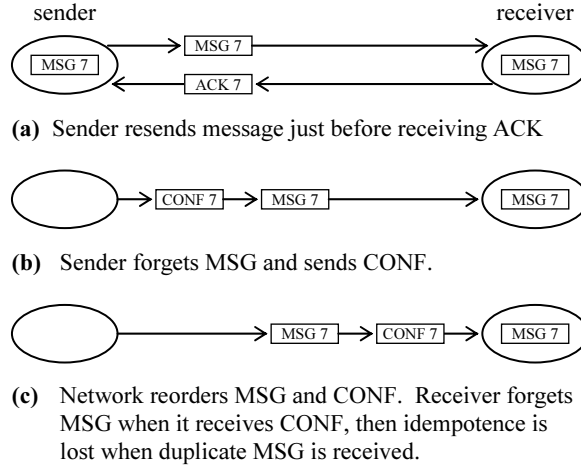
### 5.3 Out of Order Messages

The assumption that no more duplicate messages will be delivered once a CONF has been received is true only if packets sent from one node to another are received in the order that they were sent. If the network is permitted to reorder packets then the messaging protocol can fail as shown in Figure 5-2.

This problem can be fixed as long as the amount of time allowed for a packet to traverse the network is bounded. Suppose that all packets are either delivered or discarded at most  $T$  cycles after they are sent. We modify the protocol by having the receiver remember a message for  $T$  cycles

after the CONF is received. Since any duplicate message would have been sent before the CONF, by choice of  $T$  it is safe to forget the message after  $T$  cycles have elapsed.

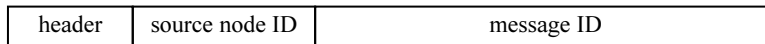
We can ensure that the bound  $T$  exists either by assigning packets a time to live as in TCP [Postel81], or by limiting both the number of cycles that a packet may be buffered by a single network node and the length of the possible routing paths. The former approach places a tighter bound on  $T$ , while latter is simpler as it does not require transmitting a time to live with each packet.



**Figure 5-2: Failure resulting from packet reordering.**

## 5.4 Message Identification

Each message must be assigned an identifier (ID) that can be placed in the ACK and CONF packets relating to that message. On the sending node the ID is sufficient to identify the message; on the receiving node the message is uniquely identified by the pair (source node ID, message ID). Figure 5-3 shows the structure of an ACK/CONF packet.

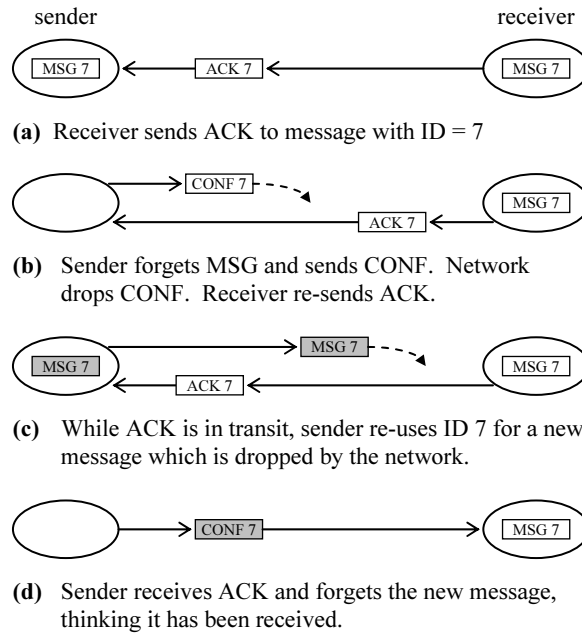


**Figure 5-3: ACK/CONF packet structure.**

A header field is present in all packets and contains the packet type and routing information. The source node ID field identifies the node which sent the packet; for a CONF this is combined with the message ID field at the receiving node to uniquely identify the message, and for an ACK it pro-

vides the destination for the CONF response (note that this information *must* be stored in the ACK and cannot simply be remembered with the original message since the message is discarded when the first ACK is received, but multiple ACKs may be received).

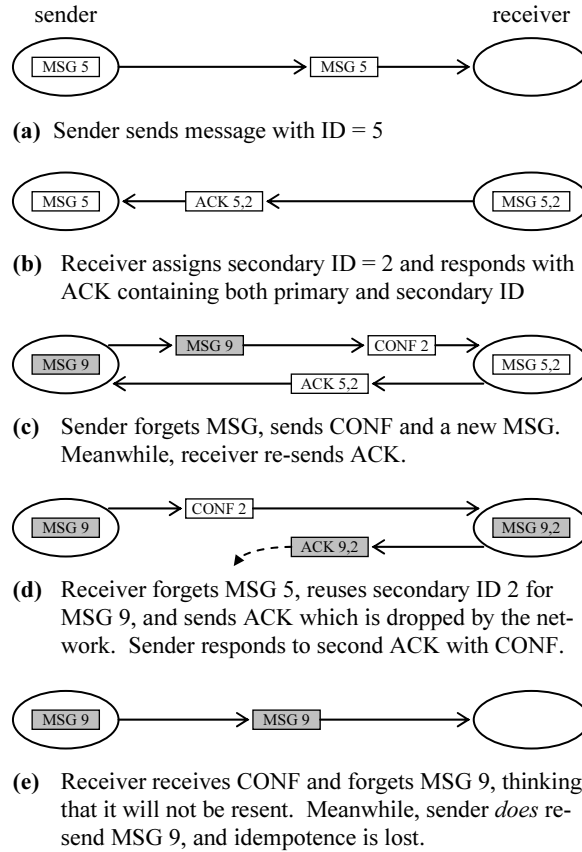
The ACK and CONF packets represent the overhead of the idempotent messaging protocol, and as such it is desirable to make them as small as possible. It is tempting to try to use short (say 4-8 bit) message ID's and simply ensure that, on a given sending node, no two active messages have the same ID. Unfortunately, this approach fails because a message is "active" until the CONF is received, and there is no way for the sending node to know when this occurs (short of adding a fourth message to the protocol). Figure 5-4 shows how a message can be erroneously forgotten if message ID's are reused too quickly.



**Figure 5-4: Failure resulting from message ID reuse.**

It is therefore necessary to use long message ID's so that there is a sufficiently long period between ID reuse. It is difficult to quantify "sufficiently long" since a message can, in theory, be active for an arbitrarily long time if the network continually drops its CONF packets. One possible strategy is to use reasonably long ID's, say 48 bits, then drain the network by suppressing new messages once every 4-12 months of operation.

The next temptation is to eliminate the source node ID field and shorten the message ID field in CONF packets only. This can be achieved by assigning to messages short secondary ID's on the receiving node so that CONF packets consist of only a header field and this secondary ID (the source node ID is no longer necessary since the secondary ID's are generated by the receiving node). Secondary ID's can be direct indices into the receive table. However, the straightforward implementation of this idea also fails when secondary ID's are reused prematurely. Figure 5-5 shows how a message can lose its idempotence when this occurs.



**Figure 5-5: Failure resulting from secondary ID reuse.**

Fortunately, a more careful implementation of secondary ID's does, in fact, work. The key observation is that because the sending node forgets CONF packets as soon as they are sent, we *can* place a bound on the amount of time that a secondary ID remains active after a CONF has been



received. If an ACK was sent before the CONF was received, then the secondary ID will be active as long as the ACK is traveling to the sender, or the sender is processing the ACK, or the CONF response is traveling back to the receiver. We have already seen how to place a bound  $T$  on packet travel time. If in addition we place a bound  $R$  on the time taken to process an ACK (dropping the packet if it cannot be serviced in time), then a secondary ID can remain active for at most  $2T + R$  cycles after the first CONF is received. We can therefore avoid secondary ID reuse by remembering a message for  $2T + R$  cycles after the CONF is received.

## 5.5 Hardware Requirements

In addition to the control logic needed to implement the protocol, the primary hardware requirements are two content addressable memories (CAMs) used for remembering messages. The first of these remembers messages sent, stores {message ID, message index} on each line, and is addressed by message ID. “message index” locates the actual message and is used to free resources when an ACK is received. The processor is prohibited from generating new messages if this send table fills, and must stall if it attempts to do so until an entry becomes available. The second CAM remembers messages received, stores {source node ID, message ID} on each line and is addressed by (source node ID, message ID). No additional information is required in this CAM since the receiver simply needs to know whether or not a particular message has already been received. If this table is full, new messages received over the network are dropped.

# Chapter 6

## The Hamal Microkernel

*I claim not to have controlled events, but confess  
plainly that events have controlled me.*

– Abraham Lincoln (1809-1865), in a letter to Albert G. Hodges

The resources of the Hamal processor-memory node are managed by a lightweight event-driven microkernel that runs concurrently in context 0. This approach has the effect of blurring the distinction between hardware and software, and necessitates an integrated design methodology. Indeed, throughout the course of the design process, many hardware mechanisms have been replaced by software alternatives, and many basic kernel tasks have been migrated into hardware. The resulting design reflects an effort to maximize system efficiency and flexibility while keeping both the hardware and the kernel as simple as possible. In this chapter we describe the various aspects of the Hamal microkernel, including both its event handling strategies and the interface it presents to user applications.

### 6.1 Page Management

The Hamal instruction set contains privileged instructions that allow the kernel to create, destroy, page in and page out pages of memory. All page management instructions take a virtual page address as their operand. The kernel is never required (or able) to manipulate physical page numbers; it is simply required to keep track of the number of free pages in each bank.

The use of capabilities guarantees that a page fault is always caused by an attempt to access a page which is not resident in memory and is never due to a program error. This fact, together with the use of virtual addresses to reference pages both in memory and in secondary storage, means that there is no need for the kernel to maintain any sort of page tables.

There are two types of page fault events: *data* page faults, caused by memory references, and *code* page faults, caused by instruction fetching. The kernel handles both types of events by issuing a page-in request and writing the event information to a page-in table in memory, so that the

faulting operation may be resumed when the page arrives. For a data page fault, this information consists of the memory operation, the memory address, the reply address, up to 128 bits of data, and a trap vector. For a code page fault, the information consists of the instruction address and the swap address of the faulting thread. In the case of a code page fault the kernel also suspends the offending thread.

Secondary storage responds to page-in requests by using the virtual address to physically locate the page; it then fetches the page and sends it to the requesting node. If the page does not exist, which occurs the first time a new data page is accessed, it is created and initialized with zeros. When a code or data page-in completes, a *page-in* event is generated which supplies the kernel with the virtual address of the newly arrived page. The kernel searches the page-in table for matching data page fault entries, and uses a special privileged instruction to reissue memory requests (this must be done even for code memory page-ins because code is readable). If the new page is a code page, the kernel also searches the table for matching code page fault entries, reactivating the corresponding threads.

## 6.2 Thread Management

Privileged mode instructions allow the kernel to suspend, resume, and terminate threads. As with the page management instructions, these instructions all take the virtual swap address of a thread as their operand. The kernel is neither required nor able to manipulate physical context numbers, but must keep track of the number of free contexts.

The kernel maintains threads in four doubly linked lists according to their state. *active* threads are those currently executing in one of the hardware contexts. *new* threads have been created to handle a trap or in response to a fork event but have not yet been activated. *ready* threads have been swapped out to allow other threads to run, and are ready to continue execution at any time. *suspended* threads are blocked, and are waiting for a memory reply, a code page, or a join operation.

When a fork is added to a node's hardware fork queue a *fork* event is generated. When the kernel handles this event, it allocates a new swap page by advancing a counter and creating the page. If there is a free context, the kernel loads the new thread immediately and places it in the 'active' list. Otherwise, it writes the thread to the swap page and adds it to the 'new' list. To improve the efficiency of micro-threads that perform a very simple task and then exit, the kernel attempts to reserve a context for new threads. This allows these threads to run immediately without having to wait for a longer-running thread to relinquish a context.

When a stall event occurs (Section 4.3.2), the kernel checks to see if there are any new or ready threads waiting to execute. If so, the stalled thread is suspended. Otherwise, the stall event is ignored. If the thread is suspended, it is *not* immediately added to the 'suspend' list; the kernel sim-

ply issues the *suspend* instruction and returns to the head of the event loop. This allows other events to be processed while the thread state dribbles back to its swap page. Once the thread has been completely unloaded, a *suspend* event is generated to inform the kernel that the contents of the swap page are valid and that the context is available. At this point the kernel adds the thread to the ‘suspend’ list and checks to see if it can activate any new or ready threads.

In addition to the suspend event which is generated after a thread has been manually suspended, there are four other events which indicate to the kernel that a thread is unable to continue execution. A *code page fault* event occurs when a thread tries to execute an instruction group located in a non-resident page, and was described in the previous section. A *code T trap* event occurs when a thread tries to execute an instruction group with the T trap bit set. A *break* event occurs when a thread issues a *break* instruction; this is the normal mechanism for thread termination. The kernel responds to a break event by removing the thread from the ‘active’ list and checking to see if it can activate any new or ready threads. A *trap* event occurs when a thread encounters an error condition and its trap vector is invalid. Each of these events is placed in the event queue *after* the faulting thread has been dribbled to memory, so the kernel can assume that the contents of the swap page are valid and the thread’s context is available.

When a reply to a memory request is received, the processor checks to see if the requesting thread is still active in one of the contexts. If so, the reply is processed by that context. Otherwise a *reply* event is generated. The kernel handles this event by directly modifying the contents of the thread’s swap page. If the thread was suspended and the kernel determines that the reply will allow the thread to continue executing, then the thread is reactivated if there is more than one free context (recall that one context is reserved for new threads), otherwise it is moved to the ‘ready’ list.

Thread scheduling is performed using a special purpose count-down register which is decremented every cycle when positive and which generates a *timer* event when it reaches zero. If there are no threads waiting to be scheduled, then the timer event is simply ignored. Otherwise the least recently activated thread (i.e. the thread at the head of the ‘active’ list) is suspended using the *suspend* instruction.

### 6.3 Sparsely Faceted Arrays

In order to support sparsely faceted arrays, the kernel must supply the network interface with translations when translation cache misses occur. Two events notify the kernel of cache misses: *translate-in* events, generated by failed global→local translations, and *translate-out* events, generated by failed local→global translations. The kernel maintains a full translation table, and responds to translation events by looking up the appropriate translation and communicating it to the network interface using the privi-

leged *xlate* instruction. If no translation is found, which can only occur for a translate-in event the first time a node encounters an xsparse capability for a SFA, the kernel uses the segment size information embedded in the xsparse capability to allocate a local facet, and the base address of this facet is entered into the translation table.

## 6.4 Kernel Calls

The kernel exposes a set of privileged subroutines to user applications by creating a *kernel table* of entry points in memory, then placing a read-only capability for this table in one of the shared registers. The entry points are all code capabilities with the P (execute privileged), I (increment only) and D (decrement only) bits set, allowing applications to call these subroutines in privileged mode. Table 6-1 lists some examples of kernel subroutines.

Subroutine	Description
trap	Default trap handler
malloc	Allocate a data capability
smlloc	Allocate a sparse capability
xmalloc	Allocate an xsparse capability
fopen	Open an existing file
fnew	Create a file

**Table 6-1: Kernel subroutines examples.**

Because the trap and malloc entry points are used so frequently (threads typically copy *trap* into the trap vector when they initialize, and malloc is called to allocate memory), they are stored in shared registers so that they may be accessed directly. The *fopen* and *fnew* routines return IO capabilities that allow applications to communicate with the external host.

The *malloc* routine allocates memory simply by advancing an allocation counter. The allocation counter is stored in a shared register. Spin-wait synchronization is used to obtain the counter; *malloc* begins by atomically reading and resetting the shared register (using two instructions in a single instruction group) until a non-zero value is read. After the memory is allocated the counter is advanced and written back into the shared register. Both *malloc* and *xmalloc* use the same counter; *smlloc* uses a separate counter so that multiple sparse objects allocated by the same node will be stored contiguously on all nodes.

## 6.5 Forwarding Pointers

Hamal implements forwarding pointers by setting the T trap bit of a 128-bit memory word and storing the forwarding pointer in that word. When a memory request attempts to access a forwarding pointer, the memory sys-

tem attempts to automatically forward the request. In some cases, however, it may not be possible for the request to be forwarded in hardware (see Chapter 7: Deadlock Avoidance). In these cases a *data T trap* event is generated. The kernel spawns a new thread to handle the trap and forward the memory request. When this thread runs, it uses the *loadw* instruction, a privileged non-trapping load, to read the forwarding pointer from memory, and then reissues the memory request using the new address.

The default trap handler supplied by the kernel contains code to handle squid traps, caused by pointer comparison instructions that cannot be completed in hardware, as described in Section 3.2.2. The handler uses *loadt*, a privileged instruction to inspect a T trap bit, in conjunction with *loadw* to determine the final addresses of the pointers being compared. It then performs the comparison and manually updates the predicate register specified as the destination of the trapping instruction.

## 6.6 UV Traps

When a memory reference causes a U/V trap (Section 3.3.5), a *UV trap* event is generated. The kernel responds to this event by creating a new thread to handle the event. The starting address for this thread is the user-supplied trap vector which accompanies every potentially-trapping memory request. The thread is created in memory, and is initialized with the UV trap information. It is activated immediately if a context is available, otherwise it is added to the ‘new’ list. The kernel *must* create this thread manually and cannot simply issue a *fork* as this is a potentially blocking instruction (see Chapter 7).

## 6.7 Boot Sequence

The boot sequence on a processing node is initiated by the arrival of a page of code whose virtual address is zero, at which point context 0 starts executing the code from the beginning. This page contains the start of the kernel loader which performs the following tasks in order:

1. Root code and data capabilities are created.
2. The rest of the kernel code pages are paged in from secondary storage.
3. Kernel data pages are created and initialized
4. The kernel table is created and the shared registers are initialized.
5. The code pages containing the kernel loader are destroyed.
6. The kernel loader branches to the head of the event loop.

At this point the event queue will be empty and the kernel will stall waiting for an event. The external host can then initiate user applications by injecting one or more *fork* messages into the machine.



# Chapter 7

## Deadlock Avoidance

*Advance, and never halt, for advancing is perfection.*

– Kahlil Gibran (1883-1931), “The Visit of Wisdom”

One of the most important considerations in designing a large parallel system is ensuring that it is deadlock-free. Much of the literature regarding deadlock avoidance deals exclusively with the network, which is the most obvious potential source of deadlocking problems. In a non-discarding network, one must rely on either topological routing constraints [Dally87] or virtual channels [Dally93] to prevent network deadlock. In addition, it is necessary to guarantee that nodes can always sink packets that arrive over the network. A discarding network, by contrast, finesses the problem by simply dropping packets that cannot make forward progress. As a result, cyclic routing dependencies are transient at worst and will never bring the machine to a halt. There are, however, two other potential sources of deadlock in the system. The first of these is *inter-node* deadlock, caused by a group of nodes that exhaust their network resources while trying to send each other packets. Consider the simple case in which programs running on two different nodes issue a large number of remote read requests to each other’s memory (Figure 7-1). If the send and receive tables on each node should fill up with these requests, then no more forward progress will be made. No packets can be delivered because the receive tables are full, and no packets can be processed because the send tables are full so there is no room for the read replies. The second possible type of deadlock is *intra-node* deadlock, which occurs when the event-handling microkernel becomes wedged. This can happen, for example, if the kernel issues a read request which causes a page fault. A page fault event will be placed on the event queue but will never be serviced; the kernel thread will stall indefinitely waiting for the read operation to complete.

Eliminating these potential sources of deadlock requires cooperation between the hardware design and the software microkernel. In this chapter we outline the strategies used in the Hamal architecture and microkernel to ensure that the entire system is provably deadlock-free.



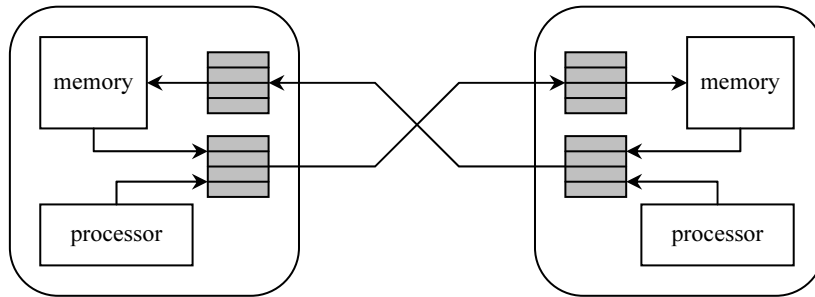


Figure 7-1: Inter-node deadlock can occur if the network tables fill up.

## 7.1 Hardware Queues and Tables

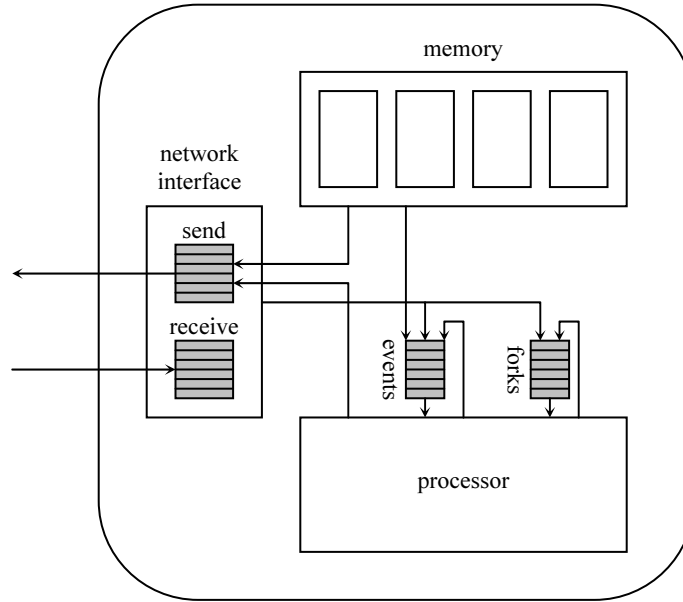
To first order approximation, the possibility of deadlock emerges directly from the presence of hardware queues and tables. A hardware queue/table has a fixed size and can potentially fill up; when it does backpressure must be exerted to suppress various other events and operations. We therefore begin our discussion of deadlock avoidance by reviewing the hardware queues and tables of the Hamal processor-memory nodes and the various types of backpressure used to ensure that they do not overflow.

As shown in Figure 7-2, there are two queues and two tables that need to be considered. First and foremost is the hardware event queue. Events can be generated by the processor (e.g. thread termination, memory replies), the memory banks (e.g. page faults, memory traps), or the network interface (e.g. translation cache miss, forks). The second queue is the fork queue which is fed by both the network interface and the local processor. Finally, the network interface contains two tables: a send table, fed by the processor and the memory banks (for replies to remote memory operations or forwarded addresses), and a receive table, which is fed by the network.

If the receive table fills, no packets will be accepted from the network. If the fork queue fills, fork packets in the receive table will not be processed, and any context that tries to issue a *fork* instruction will stall. Having the send table or event queue fill is a much more serious problem as in this case a memory bank could stall if it needs to generate an event or service a remote memory request. This in turn can deadlock the node if the kernel needs to access the stalled memory bank to make forward progress. Mechanisms are therefore required to ensure that memory banks are always able to finish processing requests.

The node controller guarantees space in the send table by reserving entries in advance. Before accepting a remote memory request from the network or a local request from the processor with a remote return address, the controller attempts to reserve a spot in the send table. If it is unable to do so then the memory request is blocked. If a remote memory request is al-

lowed to proceed to the appropriate memory bank but causes a trap, an event is added to the event queue and the send table reservation for that request is cancelled.



**Figure 7-2: Hardware queues and tables in the Hamal processor-memory node.**

The event queue is prevented from overflowing using a high water level mechanism. If the event queue fills beyond the high water level, all operations which can potentially give rise to new events are throttled. Other potentially event-causing operations may already be in progress; the high water level mark is chosen so that there are enough free entries to accept these events. Network events are suppressed, and no forks, joins or memory requests are accepted from the network. Processor events (such as thread termination) are suppressed. All memory requests are blocked except for those generated by context 0. Once the kernel has processed enough events to bring the event queue below the high water level, normal operation resumes.

## 7.2 Intra-Node Deadlock Avoidance

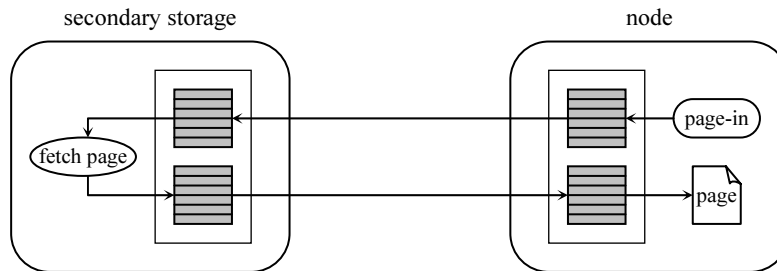
We begin by describing a set of requirements to prevent an individual node from deadlocking. In the following section we show how to use the assumption that individual nodes are deadlock-free to avoid inter-node deadlocks. For now, however, we can make no assumptions about the system as a whole, and in particular we must allow for the possibility that packets

destined to other nodes remain in the send table for arbitrarily long periods of time.

To avoid intra-node deadlock, we must be able to guarantee that the microkernel's event handling routines do not block and finish executing in a finite amount of time. This ensures that forward progress can always be made, independent of the pattern of events which occur. For the most part this is easy to do; software exceptions can be avoided through careful programming, and instructions requiring machine resources that may not be available (e.g. *fork*) can be avoided altogether. The difficulty lies in performing memory operations, since every memory reference can potentially generate a page fault or a trap.

The solution to this problem requires cooperation between the kernel and the hardware. The kernel must not issue a potentially trapping memory request, a remote memory request, or a memory request with a remote return address. When the kernel accesses local memory it must ensure that the page being referenced is present in memory. If a page is not present, then the kernel must first page it in and spin-wait for it to arrive, possibly first paging out another page to make room. Thus, the hardware must guarantee that page-ins and page-outs can always complete without blocking.

Figure 7-3 shows the complete path taken by a page-in request; page-outs follow the first half of this path. We can ensure that secondary storage requests do not block by working backwards along this path. First, the processor-memory node must be able to process the page-in packet. Processing a page-in usually involves storing the page to memory and generating a page-in event. However, this can cause problems if the kernel needs to page-in and spin-wait for several pages; the resulting page-in events could overwhelm the event queue. We avoid this situation with a special version of the *pagein* instruction that does not generate an event when the page is loaded. By using this instruction to load pages that are needed immediately, the kernel guarantees that the node will be able to process the page when it arrives.



**Figure 7-3: Life cycle of a page-in request.**

Next, the network interface must be able to receive the page-in packet sent from secondary storage. This is guaranteed by reserving an entry in

the network receive table for secondary storage packets. If a packet arrives from some other source and there is only one available receive table entry, that packet is dropped. Moving backwards along the path, secondary storage simply handles requests in the order that they are received and will never block. Although its send table can potentially fill up, the fact that nodes can always eventually receive secondary storage packets implies that a send table entry will become available in a finite amount of time. Finally, a node must always be able send page-in and page-out packets to secondary storage. We again make this guarantee by reserving a table entry for secondary storage packets, this time in the send table. The combination of an event-free *pagein* instruction and reserved entries in the send and receive tables ensures that page-in and page-out operations can always proceed to completion. This in turn implies that the event-handling microkernel can always make forward progress, so the nodes are deadlock-free.

There is still one subtlety that must be addressed with regard to page-ins. While the above mechanisms are sufficient to ensure that event-free page-ins will never become blocked, we must also consider those page-ins which are issued in response to a page fault and which must be allowed to generate an event when they arrive at the node. Furthermore, at any given time there could be many active page-in requests at various points in the path of Figure 7-3. The event queue must be able to absorb their events when they arrive at the node: the page-ins cannot stall in the receive table until an event queue slot becomes available as this could block a page-in for which the kernel is spin-waiting, nor can the reserved receive table entry be designated for event-free page-ins only as then the secondary storage send table could fill with event-generating page-ins that cannot be sent. One solution is to lower the event-queue high water mark to allow for some specified number of in-flight page-ins, requiring that the kernel cooperate by never requesting more than that number of page-ins simultaneously. A slightly more efficient solution, implemented in the Hamal architecture, is to maintain a separate event queue specifically for page-in events. This avoids wasting large event-queue entries (512 bits each) for small page-in events (each page-in event simply consists of the virtual base address of the newly arrived page). Again, the kernel cooperates by restricting the number of simultaneously requested pages.

### 7.3 Inter-Node Deadlock Avoidance

We can now use the fact that individual nodes are deadlock-free to eliminate the possibility of inter-node deadlocks. A sufficient condition for the system to be deadlock free is for every request in a node's network receive table entry to be processed in a finite amount of time. The difficulty is that some of these requests cannot be processed unless there is space in the send table; it is this dependency that leads to the deadlock situation illustrated in Figure 7-1. We will refer to these as *non-terminal* requests. A *terminal*

request is one that can be processed by the node without generating a new remotely destined request. Terminal requests consist of forks, joins (Section 4.4) and replies to remote memory references. Non-terminal requests consist of all memory operations. We can leverage the fact that, because a given node is deadlock-free, all terminal requests in the receive table will eventually be processed by the node.

The network send and receive tables already have an entry reserved for secondary storage packets. Our approach to inter-node deadlock avoidance is to reserve an additional entry in each table for terminal requests. We claim that with this simple hardware modification, the system as a whole is deadlock-free. To see this, suppose that a node is unable to process one of the packets in its receive table. This implies both that the packet is a non-terminal request (i.e. a remote memory request) and that a reservation cannot be made in the send table for the reply to this request. Since a memory reply is a terminal request, this means that the terminal request entry in the send table is occupied. But this terminal request will eventually be delivered to its destination, because the destination node has a receive entry reserved for terminal requests. It doesn't matter if this entry is occupied or if there are other nodes competing for it; because the destination node can always service terminal requests, with probability 1 the terminal request will eventually be successfully delivered. Thus, the terminal request entry in the send table will eventually be unoccupied, allowing the remote memory request to be processed. Again, it doesn't matter if other non-terminal requests, existing in the receive table or locally generated, are competing for the send table; as long as the node's arbitration policy is starvation-free, with probability 1 the memory request will eventually be processed by the node.

What makes this approach possible is the fact that when a non-terminal request is serviced, a terminal request is generated. There is, however, one exception to this rule: if a request encounters a forwarding pointer, it is automatically forwarded, possibly generating a new non-terminal request if the forwarding destination is remote. This is not a problem, and does not affect the above proof, so long as the send table reservation for that request was not made using the entry set aside for terminal requests. If it was, then the request cannot be automatically forwarded. Instead, the node controller cancels the send table reservation and generates a data T trap event to be handled by the microkernel.



## Part II – Evaluation

*There is nothing either good or bad, but thinking makes it so.*

– William Shakespeare (1564-1616), “Hamlet”, Act 2 scene 2

*It is a capital mistake to theorize before one has data.*

– Sir Arthur Conan Doyle (1859-1930), “Scandal in Bohemia”



# Chapter 8

## Simulation

*I just bought a Mac to help me design the next Cray.*

– Seymour Cray (1925-1996)

Our evaluations of the Hamal parallel architecture are based on a cycle accurate simulator of the entire system. In this chapter we describe our simulation methodology. We begin by presenting *Sim*, a C++ framework for cycle-based simulation that was developed to facilitate the construction of the Hamal simulator. We then give an overview of the Hamal simulator, and we describe the development environment used to edit, assemble, run and debug both the kernel and benchmark applications.

### 8.1 An Efficient C++ Framework for Cycle-Based Simulation

Software simulation is a critical step in the hardware design process. Hardware description languages such as Verilog and VHDL allow designers to accurately model and test the target hardware, and they provide a design path from simulation to fabrication. However, they are also notoriously slow, and as such are not ideal for simulating long runs of a large, complex system. Instead, a high-level language (usually C or C++) is generally used for initial functional simulations. Inevitably, the transition from this high-level simulation to a low-level hardware description language is a source of errors and increased design time.

Recently there have been a number of efforts to develop simulation frameworks that enable the accurate description of hardware systems using existing or modified general-purpose languages ([Ku90], [Liao97], [Gajski00], [Ramanathan00], [Cyn01], [SC01]). This bridges the gap between high-level and register transfer level simulations, allowing designers to progressively refine various components within a single code base. The approach has been successful: one group reported using such a framework to



design a 100 million transistor 3D graphics processor from start to finish in two months [Kogel01].

There are four important criteria to consider when choosing or developing a framework:

**Speed:** The simulator must be fast. Complex simulations can take hours or days; a faster simulator translates directly into reduced design time.

**Modularity:** There should be a clean separation and a well-defined interface between the various components of the system.

**Ease of Use:** The framework should not be a burden to the programmer. The programming interface should be intuitive, and the framework should be transparent wherever possible.

**Debugging:** The framework must contain mechanisms to aid the programmer in detecting errors within the component hierarchy.

These criteria were used to create *Sim*, a cycle-based C++ simulation framework used to simulate the Hamal architecture. Through experience we found that *Sim* met all four criteria with a great deal of success. In the following sections we describe the *Sim* framework and we report on what we observed to be its most useful features. We also contrast *Sim* with SystemC [SC01], an open-source C++ simulation framework supported by a number of companies.

### 8.1.1 The *Sim* Framework

To a large extent, the goals of speed and modularity can be met simply by choosing an efficient object-oriented language, i.e. C++. What distinguishes a framework is its simulation model, programming interface and debugging features. *Sim* implements a pure cycle-based model; time is measured in clock ticks, and the entire system exists within a single clock domain. The programmer is provided with three abstractions: components, nodes and registers. A component is a C++ class which is used to model a hardware component. In debug builds, *Sim* automatically generates hierarchical names for the components so that error messages can give the precise location of faults in the simulated hardware. A node is a container for a value which supports connections and, in debug builds, timestamping. Nodes are used for all component inputs and outputs. Registers are essentially D flip-flops. They contain two nodes, D and Q; on the rising clock edge D is copied to Q.

Simulation proceeds in three phases. In the construction phase, all components are constructed and all connections between inputs and outputs

are established. When an input/output node in one component is connected to an input/output node in another component, the two nodes become synonyms, and writes to one are immediately visible to reads from the other. In the initialization phase, Sim prepares internal state for the simulation and initial values may be assigned to component outputs. Finally, the simulation phase consists of alternating calls to the top-level component's Update function (to simulate combinational evaluation) and a global Tick function (which simulates a rising clock edge).

Figure 8-1 gives an example of a simple piece of hardware that computes Fibonacci numbers and its equivalent description using Sim. The example shows how components can contain sub-components (Fibonacci contains a ClockedAdder), how nodes and registers are connected during the construction phase (using the overloaded left shift operator), and how the simulation is run at the top level via alternating calls to fib.Update() and Sim::Tick(). The component functions Construct() and Init() are called automatically by the framework; Update() is called explicitly by the programmer.

### 8.1.2 Timestamps

In a cycle-based simulator, there are three common sources of error:

**Invalid Outputs:** The update routine(s) for a component may neglect to set one or more outputs, resulting in garbage or stale values being propagated to other components.

**Missing Connections:** One or more of a component's inputs may never be set.

**Bad Update Order:** When the simulation involves components with combinational paths from inputs to one or more outputs, the order in which components are updated becomes important. An incorrect ordering can have the effect of adding or deleting registers at various locations.

While careful coding can avoid these errors in many cases, experience has shown that it is generally impossible to write a large piece of software without introducing bugs. In addition, these errors are particularly difficult to track down as in most cases they produce silent failures which go unnoticed until some unrelated output value is observed to be incorrect. The programmer is often required to spend enormous amounts of time finding the exact location and nature of the problem.

```

class ClockedAdder : public CComponent
{
    DECLARE_COMPONENT(ClockedAdder)
public:
    Input<int> a;
    Input<int> b;
    Output<int> sum;

    Register<int> reg;

    void Construct (void) {sum << reg;}
    void Init (void) {reg.Init(0);}
    void Update (void) {reg = a + b;}
};

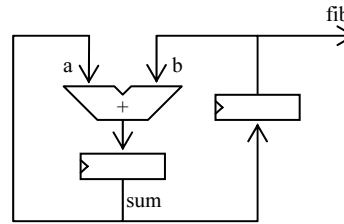
class Fibonacci : public CComponent
{
    DECLARE_COMPONENT(Fibonacci)
public:
    Output<int> fib;

    Register<int> reg;
    ClockedAdder adder;

    void Construct (void)
    {
        adder.a << adder.sum;
        adder.b << reg;
        reg << adder.sum;
        fib << reg;
    }
    void Init (void)
    {
        adder.sum.Init(1);
        reg.Init(0);
    }
    void Update (void)
    {
        adder.Update();
    }
};

void main (void)
{
    Fibonacci fib; // Construction
    Sim::Init(); // Initialization
    while (1) // Simulation
    {
        fib.Update();
        Sim::Tick();
    }
}

```



**Figure 8-1: Sim code and schematic for a Fibonacci number generator.**

The Sim framework helps the programmer to eliminate all three sources of error by timestamping inputs and outputs. In debug builds, each time a node is written to it is timestamped, and each time a node is read the timestamp is checked to ensure that the node contains valid data. When an invalid timestamp is encountered, a warning message is printed which includes the automatically generated name of the input/output, pinpointing the error within the component hierarchy.

Timestamped nodes have proven to be by far the most useful feature of the Sim framework. They can speed up the debugging process by an order of magnitude, allowing the programmer to detect and correct errors in minutes that would otherwise require hours of tedious work. Figure 8-2 shows the exact warning message that would be generated if the connection “adder.b << reg” were omitted from the function Fibonacci::Construct() in Figure 8-1.

```
Warning: Fibonacci0::Adder0::Input1
        Invalid timestamp
        c:\projects\sim\sim.h, line 527, simTime = 1
```

**Figure 8-2: Warning message generated if the programmer forgets the connection adder.b << reg.**

### 8.1.3 Other Debugging Features

The Sim framework provides a number of Assert macros which generate warnings and errors. As is the case with standard assert macros, they give the file and line number at which the error condition was detected. In addition, the error message contains the simulation time and a precise location within the component hierarchy (as shown in Figure 8-2). Again, this allows the programmer to quickly determine which instance of a given component was the source of the error.

When one node A is connected to another node B, the intention is usually to read from A and write to B (note that order is important; connecting A to B is not the same as connecting B to A). Timestamps can be used to detect reads from B, but not writes to A. To detect this type of error, in debug builds a node connected to another node is marked as read-only<sup>1</sup>; assignment to a read-only node generates a warning message. In practice this feature did not turn out to be very useful as the simple naming convention of prefixing inputs with in\_ and outputs with out\_ tended to prevent these errors. The feature does, however, provide a safety net, and it does not affect release builds of the simulator.

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<sup>1</sup> Unless the node has been declared as a bi-directional Input/Output.

### 8.1.4 Performance Evaluation

Making use of a simulation framework comes at a cost, both in terms of execution time and memory requirements. We can quantify these costs for the Sim framework by implementing four low-level benchmark circuits in both Sim and straight C++. The most important difference between the implementations is that inputs and outputs in the C++ versions are ordinary class member variables; data is propagated between components by explicitly copying outputs to inputs each cycle according to the connections in the hardware being modeled. The following benchmark circuits are used in our evaluation:

- LFSR:** 4-tap 128-bit linear feedback shift register. Simulated for  $2^{24}$  cycles.
- LRU:** 1024 node systolic array used to keep track of least recently used information for a fully associative cache (see Chapter 4, Section 4.7.1). Simulated for  $2^{17}$  cycles.
- NET:** 32x32 2D grid network with wormhole routing. Simulated for  $2^{13}$  cycles.
- FPGA:** 12 bit pipelined population count implemented on a simple FPGA. The FPGA contains 64 logic blocks in an 8x8 array; each block consists of a 4-LUT and a D flip-flop. Simulated for  $2^{21}$  cycles.

In the Sim version of FPGA, the FPGA configuration is read from a file during the construction phase and used to make the appropriate node connections. In the C++ version, which does not have the advantage of being able to directly connect inputs and outputs, the configuration is used on every cycle to manually route data between logic blocks.

The benchmarks were compiled in both debug and release modes and run on a 1.2GHz Pentium III processor. Table 8-1 shows the resulting execution times in seconds, and Table 8-2 lists the memory requirements in bytes.

	Debug			Release		
	C++	Sim	Ratio	C++	Sim	Ratio
LFSR	17.56	500.40	<b>28.50</b>	5.77	20.56	<b>3.56</b>
LRU	15.78	106.54	<b>6.75</b>	3.15	5.14	<b>1.63</b>
NET	11.34	126.54	<b>11.16</b>	2.86	5.38	<b>1.88</b>
FPGA	12.29	6.42	<b>0.52</b>	3.44	0.36	<b>0.10</b>

**Table 8-1: Benchmark execution time in seconds.**

	Debug			Release		
	C++	Sim	Ratio	C++	Sim	Ratio
LFSR	129	7229	<b>56.04</b>	129	1673	<b>12.97</b>
LRU	28672	233484	<b>8.14</b>	28672	61448	<b>2.14</b>
NET	118784	806936	<b>6.79</b>	118784	249860	<b>2.10</b>
FPGA	9396	74656	<b>7.95</b>	7084	14598	<b>2.06</b>

**Table 8-2: Benchmark memory requirements in bytes.**

The time and space overheads of the Sim framework are largest for the LFSR benchmark; the release build runs 3.56 times slower and requires 12.97 times more memory than the corresponding C++ version. This is because the C++ version is implemented as a 128-element byte array which is manually shifted, whereas the Sim version is implemented using 128 actual registers which are chained together. In release builds, each register contains three pointers: one for the input (D) node, one for the output (Q) node, and one to maintain a linked list of registers so that they can be automatically updated by the framework when Sim::Tick() is called. This, together with the 129 bytes of storage required for the actual node values, accounts for the factor of 13 increase in memory usage. Clearly the register abstraction, while more faithful to the hardware being modeled, is a source of inefficiency when used excessively.

The execution time and memory requirements for the release builds of the other three Sim benchmarks compare more favorably to their plain C++ counterparts. In all cases the memory requirements are roughly doubled, and the worst slowdown is by a factor of 1.88 in NET. In the FPGA benchmark the Sim implementation is actually faster by an order of magnitude. This is due to the fact that the framework is able to directly connect nodes at construction time as directed by the configuration file.

Not surprisingly, the Sim framework overhead in the debug builds is quite significant. The debug versions run roughly 20-25 times slower than their release counterparts, and require four times as much memory. This is largely a result of the node timestamping that is implemented in debug builds.

### 8.1.5 Comparison with SystemC

SystemC is an open source C++ simulation framework originally developed by Synopsys, CoWare and Frontier Design. It has received significant industry support; in September 1999 the Open SystemC Initiative was endorsed by over 55 system, semiconductor, IP, embedded software and EDA companies [Arnout00].

The most important difference between Sim and SystemC is that, like Verilog and VHDL, SystemC is event driven. This means that instead of being called once on every cycle, component update functions are activated as a result of changing input signals. Event driven simulators are strictly

more powerful than cycle-based simulators; they can be used to model asynchronous designs or systems with multiple clock domains.

Event driven simulation does, of course, come at a price. A minor cost is the increased programmer effort required to register all update methods and specify their sensitivities (i.e. which inputs will trigger execution). More significant are the large speed and memory overheads of an event driven simulation kernel. For example, we implemented the LRU benchmark using SystemC, and found that the release version was over 36 times slower and required more than 8 times as much memory as the Sim release build.

While event driven simulation is more powerful in terms of the hardware it can simulate, it also presents a more restrictive programming model. In particular, the programmer has no control over when component update functions are called. Hiding this functionality ensures that updates always occur when needed and in the correct order, but it also prevents certain techniques such as inlining a combinational component within an update function. Figure 8-3 gives an example of such inlining in the Sim framework; it is simply not possible using SystemC.

```
class BlackBox : public CComponent
{
    DECLARE_COMPONENT(BlackBox)
public:
    Input<int> a;
    Input<int> b;
    Output<int> out;

    void Update (void);
};

class GreyBox : public CComponent
{
    DECLARE_COMPONENT(GreyBox)
public:
    Input<int> in;
    Output<int> out;

    BlackBox    m_box;
    int         m_key;

    void Update (void)
    {
        m_box.a = in;
        m_box.b = m_key;
        m_box.Update();
        out = in + m_box.out;
    }
};
```

**Figure 8-3: Inlining a combinational component (BlackBox) within the Grey-Box Update() function.**

Another important difference between Sim and SystemC is the manner in which inputs and outputs are connected. Sim allows input/output nodes to be directly connected; in release builds a node is simply a pointer, and connected nodes point to the same piece of data. SystemC, by contrast, requires that inputs and outputs be connected by explicitly declared signals. This approach is familiar to hardware designers from hardware description languages such as Verilog and VHDL. However, it is less efficient in terms of programmer effort (more work is required to define connections between components), memory requirements, and execution time.

A minor difference between the frameworks is that SystemC requires component names to be supplied as part of the constructor, whereas Sim generates them automatically. In particular, components in SystemC have no default constructor, so one cannot create arrays of components in the straightforward manner, nor can components be member variables of other components. The programmer must explicitly create all components at run time using the *new* operator. Clearly this is not a fundamental difference and it would be easy to fix in future versions of SystemC. It does, however, illustrate that the details of a framework's implementation can noticeably affect the amount of programmer effort that is required to use it. A crude measure of programmer effort is lines of code; the SystemC implementation of LRU uses 160 lines of code, compared to 130 lines for Sim and 110 lines for straight C++.

### 8.1.6 Discussion

Our experience with Sim has taught us the following five lessons regarding simulation frameworks:

#### 1. Use C++

For a number of reasons, C++ has “The Right Stuff” for developing a simulation framework. First, it is fast. Second, it is object-oriented, and objects are without question the appropriate model for hardware components. Furthermore, well defined construction orders (e.g. base objects before derived objects) allow the framework to automatically deduce the component hierarchy. Third, templated classes allow abstractions such as inputs and outputs to be implemented for arbitrary data types in a clear and intuitive manner. Fourth, macros hide the heavy machinery of the framework behind short, easy to use declarations. Fifth, the preprocessor permits different versions of the same code to be compiled. In particular, debugging mechanisms such as timestamps can be removed in the release build, resulting in an executable whose speed rivals that of straight C++. Sixth, operator overloading allows common constructs to be expressed concisely, and typecast overloading allows the framework's abstractions to be implemented trans-



parently. Finally, C++ is broadly supported and can be compiled on virtually any platform.

## **2. Use timestamps**

Silent failures are the arch-nemesis of computer programmers. Using timestamped nodes in conjunction with automatically generated hierarchical component names, the Sim framework was able to essentially eliminate all three of the common errors described in Section 8.1.2 by replacing silent failures with meaningful warning messages.

## **3. Allow inputs/outputs to be directly connected**

Using explicitly declared signals to connect component inputs and outputs is familiar to users of existing hardware description languages. However, directly connecting inputs and outputs does not change the underlying hardware model or make the simulator framework any less powerful. Direct connections reduce the amount of programmer effort required to produce a hardware model, and they lead to an extremely efficient implementation of the input/output abstraction.

## **4. Don't make excessive use of abstractions**

The most useful abstractions provided by a simulation framework are components and their interfaces. Within a component, however, further use of abstractions may not add to the modularity of the design or make the transition to silicon any easier. Thus, when simulation speed is a concern, programmers are well-advised to use straight C++ wherever possible. A good example of this principle is the LFSR benchmark. The Sim implementation could just as easily have implemented the shift register internals using a 128-element byte array, as in the C++ implementation. Using the register abstraction slowed down execution significantly, especially in the debug build. In general, we found the register abstraction to be most useful for implementing clocked outputs, as in the Adder of Figure 8-1.

## **5. Pay attention to the details**

While the speed and modeling power of a framework are primarily determined by its high-level design, it is the implementation details that programmers need to work with. How easy is it for the programmer to declare and connect components? Can components be inherited? Can they be templated? The answers to questions such as these will determine which programmers will want to use the framework, and how much effort they must expend in order to do so.

## 8.2 The Hamal Simulator

The Sim framework was used to construct a cycle accurate simulator of the Hamal architecture. We made use of the framework to define a component hierarchy and to establish connections between components. Component internals were coded in straight C++. The top level Hamal component contains four major component types. A *Root node* component emulates an external host and provides the interface between the simulator and the simulation environment. *Secondary Storage* components serve the sole purpose of storing and retrieving code and data pages. *Processor-Memory nodes* implement the actual architecture. Finally, a *network* component simulates the fat tree interconnect between the various other components. The following sections provide additional details for the processor-memory and network components.

### 8.2.1 Processor-Memory Nodes

Processor-memory nodes are divided into components exactly as shown in Figure 2-3, reproduced below as Figure 8-4 for convenience. Four data memory components and one code memory component implement the augmented embedded DRAM. A processor component simulates the Hamal processor described in Chapter 4. A network interface component allows the processor-memory node to communicate with the rest of the system via the idempotent messaging protocol presented in Chapter 5. Finally, a controller component arbitrates the various requests and replies and directs the flow of data within the node.

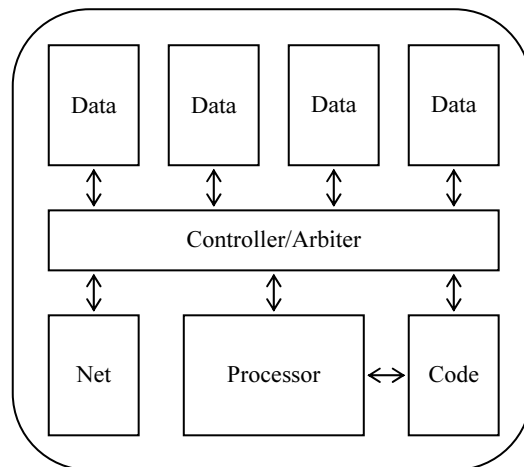
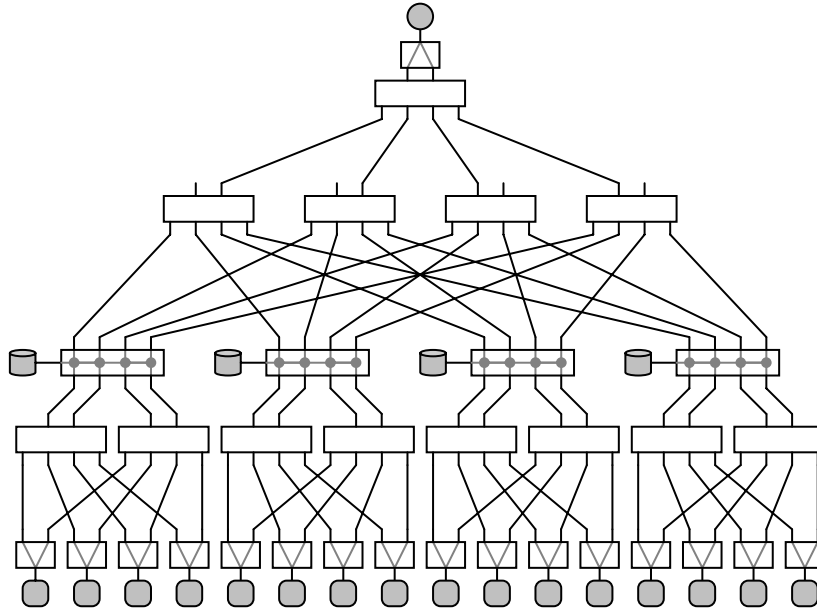


Figure 8-4: Component hierarchy of the processor-memory node.

### 8.2.2 Network

A single network component is broken down into three different types of sub-components which are connected together to form the fat tree interconnect. *Fat nodes* are radix 4 (down) dilation 2 (up) fat tree routers with two upward connections and four downward connections. *Storage nodes* connect  $k$  network connections to a single secondary storage unit; the value of  $k$  and the placement of secondary storage nodes within the network depends on the ratio of processor-memory nodes to secondary storage units. Finally, leaf nodes are connected to the root node and all processor-memory nodes; they dilate one network port into two. Each connection in the network is a 64 bit bidirectional link.

The exact configuration of the network depends on the number of processor-memory nodes and the number of secondary-storage units, both of which must be powers of two. Figure 8-5 shows an example with 16 nodes and 4 storage units.



**Figure 8-5:** Fat tree network with 16 processor-memory nodes and 4 secondary storage units.

Each network port is implemented by a *network link* sub-component which contains a four-flit FIFO queue in the input direction, and a single flit buffer in the output direction (Figure 8-6). Whenever possible, input flits are routed directly to a destination port where they are buffered and then

forwarded on the rising clock edge. In case of contention, input flits are queued for up to four cycles, after which they are discarded.

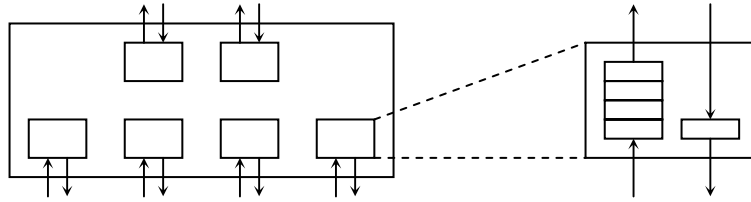


Figure 8-6: Network link sub-components implement buffering in the network nodes.

### 8.3 Development Environment

The Hamal simulator was integrated into *ramdev*, a fully featured development environment containing both an assembler and a debugger. The debugger allows the user to run code, step through code, set conditional breakpoints, save/restore the state of the entire machine, single step the entire machine, and view the contents of contexts, event queues and memory. Figure 8-7 shows a screenshot from a *ramdev* debugging session.

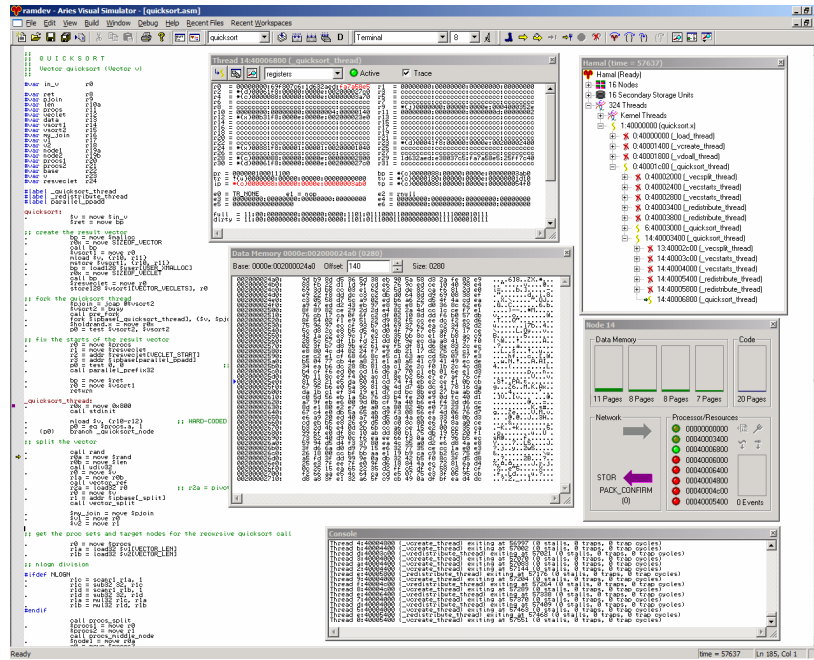


Figure 8-7: ramdev development environment for the Hamal architecture.

Ramdev was modeled after Microsoft Visual C++ and contains most of the features found in conventional debuggers. In addition, it contains a number of features to facilitate the debugging of multithreaded programs:

**Thread Hierarchy:** The debugger automatically detects the hierarchy of threads and displays it as an expanding tree (top right of Figure 8-7). Different icons indicate whether or not a thread has already terminated.

**Trace Thread:** The debugger identifies a single thread as the *trace* thread. Single stepping the trace thread causes the simulation to run until the thread's instruction pointer is advanced. When any thread encounters a breakpoint which causes the simulation to halt, that thread becomes the trace thread.

**One Thread/All Thread Breakpoints:** Two different types of breakpoints may be set by the user. Single thread breakpoints only cause the simulation to halt if they are encountered by the current trace thread. Multiple thread breakpoints halt the simulation when they are encountered by *any* thread.

**Step Into Child:** In addition to the standard Step Over, Step Into and Step Out single stepping mechanisms, ramdev contains a Step Into Child mechanism. This causes the simulation to run until a new thread is created which is a child thread of the current trace thread. The simulation is then halted, and the child thread becomes the new trace thread.

The microkernel, parallel libraries and benchmark applications were all coded in assembly using the ramdev development environment.

# Chapter 9

## Parallel Programming

*The process of preparing programs for a digital computer is especially attractive, not only because it can be economically and scientifically rewarding, but also because it can be an aesthetic experience much like composing poetry or music.*

– Donald E. Knuth (1938- ), “The Art of Computer Programming”

Our evaluation of Hamal’s support for parallel computation, most notably thread management and synchronization, are based on four parallel benchmark programs. In this chapter we describe the benchmark programs and the underlying parallel primitives used to create them.

### 9.1 Processor Sets

The basic primitive that we use to construct parallel libraries and benchmarks is the *processor set*. A processor set is an opaque data structure that specifies an arbitrary subset of the available processor nodes. Processor sets can be passed as arguments to parallel library functions to specify the set of nodes on which a computation should run. They can also be included as members of parallel data structures, indicating the nodes across which structures are distributed and implicitly specifying the processor nodes which should be used to operate on these structures. The permissible operations on processor sets are *union*, *intersection*, and *split* (split the set into two smaller sets according to a supplied ratio).

Processor sets are nearly identical to *processor teams* in [Hardwick97] and *spans* in [Brown02a]; the only difference is that both teams and spans are restricted to processor sets of the form  $[a, b]$  (where the processors are numbered from 0 to  $N - 1$ ). Removing this restriction allows one to take the union of two processor sets and also provides the opportunity to allocate processor sets which reflect the physical layout of the nodes (e.g. create a processor set for a sub-cube of the nodes in a 3D mesh). In [Hardwick97] it is shown that the processor team abstraction provides simple and efficient support for divide-and-conquer algorithms.

```

struct Vector
{
    int32  len;      // number of elements
    int32  elsize;  // size of elements
    ProcSet procs;
    Veclet *veclets; // sparse pointer
};

struct Veclet
{
    int32 len;      // number of elements
    int32 elsize;  // size of each element
    int32 start;   // index of first element
    void *data;
};

```

**Figure 9-1: Parallel vector data structures.**

Processor sets were used in conjunction with sparsely faceted arrays to create a parallel vector library. A parallel vector is simply a vector distributed across some subset of the processor-memory nodes. Figure 9-1 shows the two data structures used to implement parallel vectors. The primary Vector data structure, which exists on a single node, specifies the total number of elements in the vector, the size in bytes of each element, the set of processors across which the vector is distributed, and a sparse pointer to the vector's *veclets*. One Veclet data structure exists on each node which contains a portion of the vector. A veclet specifies the number of elements on that node, the size in bytes of each element (this is the same for all veclets), the index of the first element on that node, and a pointer to the actual vector data. The routines in the parallel vector library all operate on vectors by spawning a thread on each node within the vector's processor set; these threads then operate on individual veclets.

## 9.2 Parallel Random Number Generation

Random number generation is one of the fundamental numerical tasks in computer science, used in applications such as physical simulations, Monte Carlo integration, simulated annealing, and of course all randomized algorithms. While work has been done on "true" random number generators based on some form of physical noise, the majority of software makes use of pseudo-random numbers generated by some deterministic algorithm. A good pseudo-random number generator should satisfy several properties. Ideally, the stream of numbers that is generated should be:

1. uniformly distributed
2. completely uncorrelated
3. non-repeating

4. reproducible (for debugging)
5. easy to generate

Conditions 2 and 3 are not theoretically possible to satisfy since a pseudo-random stream is generated by a deterministic algorithm, and any generator which uses a finite amount of storage will eventually repeat itself. In practice, however, many generation algorithms are known with good statistical properties and extremely long periods. The three most commonly used generators are linear congruential generators, lagged Fibonacci generators, and combined generators which somehow combine the values from two different generators ([Coddington97], [Knuth98]).

### 9.2.1 Generating Multiple Streams

Parallel random number generation is more difficult because it becomes necessary to produce multiple streams of pseudo-random numbers. Each stream should satisfy the five properties listed above; in addition there should be no correlation between the various streams. Three main techniques are used to produce multiple streams of pseudo-random data from sequential generators [Coddington97]:

**Leapfrog:** A single sequence  $\{x_i\}$  is cyclically partitioned among  $N$  processors so that the sequence generated by the  $k^{\text{th}}$  processor is  $\{x_{k+iN}\}$ .

**Sequence Splitting:** A single sequence  $\{x_i\}$  with large period  $D$  is partitioned in a block fashion among  $N$  processors so that the sequence generated by the  $k^{\text{th}}$  processor is  $\{x_{k(D/N)+i}\}$ .

**Independent Sequences:** The same random number generator is used by all processors with different seeds to generate completely different sequences.

These techniques are effective in the restricted setting where there is exactly one thread per processor, but they are unsatisfactory for a more general multithreaded model of parallel computation. By associating random number generators with physical processors rather than threads of execution, the random number generators becomes shared resources and thus much more difficult to use. Furthermore, different runs of the same deterministic multithreaded program can produce different results if the threads on a given node access the generator in a different order. It may still be possible to use one of these techniques if the exact number of threads is known in advance, but in general this is not the case.



### 9.2.2 Dynamic Sequence Partitioning

An alternative to setting up a fixed number of pseudo-random streams *a-priori* is to use *dynamic sequence partitioning* to dynamically partition a single sequence on demand in a multithreaded application. This technique is based on the observation that parallel applications start as a single thread; new threads are created one at a time whenever a parent thread spawns a child thread. The idea is simply to perform a leapfrog partition each time a new thread is created. Thus, if the pseudo-random number sequence associated with a thread is  $\{x_i\}$  (where  $x_0$  is the next value that would be generated), then after creating a child thread the parent thread uses the sequence  $\{x_{2i}\}$  and the child thread uses the sequence  $\{x_{2i+1}\}$ . This partitioning is applied recursively as new threads are created.

Figure 9-2 shows an example of dynamic sequence partitioning. Initially, the single thread A has sequence  $\{x_0, x_1, x_2, \dots\}$ . When thread B is created it inherits the subsequence  $\{x_1, x_3, x_5, \dots\}$  while A retains  $\{x_0, x_2, x_4, \dots\}$ . Then A calls `rand()`, generating  $x_0$  and leaving  $\{x_2, x_4, x_6, \dots\}$ . When thread C is created it is given the subsequence  $\{x_4, x_8, x_{12}, \dots\}$  and A is left with  $\{x_6, x_{10}, x_{14}, \dots\}$ . Finally, thread C creates thread D which is initialized with the sequence  $\{x_8, x_{16}, \dots\}$ .

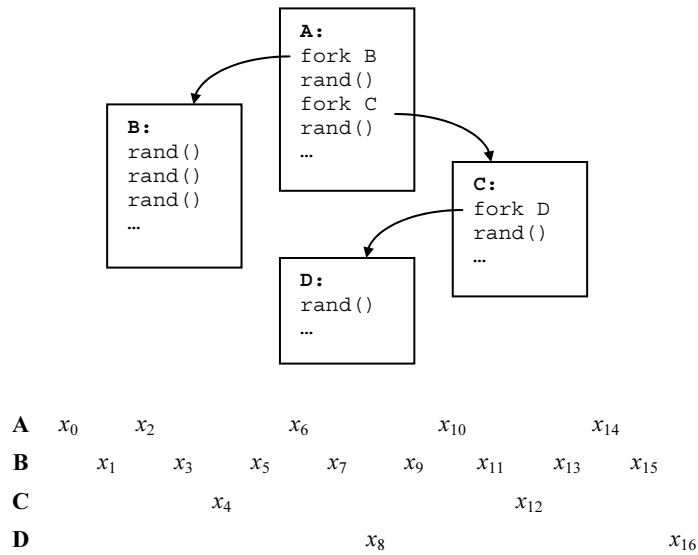


Figure 9-2: Dynamic sequence partitioning example.

Given an infinite initial pseudo-random sequence  $\{x_i\}$ , dynamic sequence partitioning would assign to each thread a disjoint pseudo-random sub-sequence. In practice, of course, pseudo-random sequences are peri-

odic, not infinite. Furthermore, since leapfrog partitioning has the effect of halving the sequence period, creating threads in an adversarial manner can cause the sequence to wrap around in logarithmic time. It is therefore desirable to choose an initial sequence with an extremely long period.

### 9.2.3 Random Number Generation in Hamal

For the Hamal benchmarks, we have implemented a multiplicative linear congruential generator with modulus  $2^{61} - 1$  (this is the next Mersenne prime beyond  $2^{31} - 1$ , a common modulus for existing applications). Given a multiplier  $a$ , the sequence  $\{x_i\}$  is defined by

$$x_{i+1} \equiv ax_i \pmod{2^{61} - 1} \quad (1)$$

This generator provides a balance between quality and simplicity of random number generation. The period is of medium length – if  $a$  is a primitive root then the period is  $2^{61} - 2$ . Only 128 bits of state are required to store  $a$  and  $x_i$ . Because Hamal supports 64→128 bit integer multiplication, computing  $x_{i+1}$  is very efficient. Figure 9-3 shows assembly code for `rand()`, which consists of 7 arithmetic instructions arranged in 5 VLIW instruction groups. `$holdrand` (r29) is a 128 bit register whose upper 64 bits (`$holdrand.y`) are used to store  $a$  and whose lower 64 bits (`$holdrand.x`) are used to store  $x_i$  shifted left by 3 bits ( $8x_i$ ).

```
#var holdrand    r29
#var rand        r29b

rand:
.               r0x = move $holdrand.y  ;; r0x = multiplier 'a'
.               $holdrand = mul64 $holdrand.x, $holdrand.y
.               $holdrand.y = shl64 $holdrand.y, 3
.               $holdrand.x = add64 $holdrand.x, $holdrand.y
.               $holdrand.y = move r0x
.   (p13)      $holdrand.x = add64 $holdrand.x, 8
.               r0a = move $rand
.               return
```

**Figure 9-3: Hamal assembly code for `rand()`.**

The multiplication in the first instruction group computes  $8ax_i = 8x_{i+1}$  as a 128 bit number. If the upper 64 bits of the product are  $u$  and the lower 64 bits are  $8v$ , then

$$8x_{i+1} = 2^{64}u + 8v \equiv 8u + 8v \pmod{2^{61} - 1} \quad (2)$$

To reduce the product modulo  $2^{61} - 1$  we therefore left shift the upper bits by 3 then add them to the lower bits. In case of a carry beyond the last bit (indicated by the *integer inexact* flag p13), we must add an additional 8,

since  $2^{64} \equiv 8 \pmod{2^{61} - 1}$ . Finally, `rand()` returns a 32 bit random number taken from the upper 32 bits of  $x_{i+1}$ .

Another advantage of this generator is that dynamic sequence partitioning is easy. If the state of a thread's random number generator is  $(a, x)$ , then when a child thread is created the state is changed to  $(a^2, x)$ , and the state of the child thread's generator is  $(a^2, ax)$ . Note that if  $a$  is a primitive root then  $a^2$  is *not* a primitive root and has order  $2^{60} - 1$ . Since  $2^{60} - 1$  is odd, successive squarings do not change this order. Thus, all pseudo-random number sequences created by dynamically partitioning this generator will have period  $2^{60} - 1$  and will cycle through all the squares modulo  $2^{61} - 1$ .

### 9.3 Benchmarks

Four benchmark applications were chosen to test Hamal's support for parallel programming: a simple parallel-prefix addition, quicksort, an  $N$ -body simulation, and a frequency count of words from a large body of text. The following sections describe each of these benchmarks in detail.

#### 9.3.1 Parallel Prefix Addition

Parallel prefix operations (also known as *scans*) are important data-parallel primitives supported by high-level parallel languages such as NESL [Bleloch95]. The **ppadd** benchmark performs parallel prefix addition on a vector of 32 bit integers, replacing the entry  $x_k$  with the sum  $x_0 + x_1 + \dots + x_k$ . `ppadd` stores the vector as a single sparsely faceted array and sets up a binary tree of threads with one leaf thread on each node, using register-based synchronization to pass values between parent and child threads (Figure 9-4). Each leaf computes the sum of the values on its node and passes this sum to its parent. The tree of threads is then used to compute partial sums in logarithmic time. Finally, each leaf receives from its parent the sum of all values on all previous nodes, and uses this sum to perform the local parallel prefix computation.

The running time of parallel prefix on  $N$  nodes for a vector of length  $m$  can be modeled as  $C_0 + C_1m/N + C_2\log(N)$ . The constant  $C_2$  represents the overhead of creating a binary tree of threads and communicating within this tree and it limits the overall speedup that can be achieved. Setting the derivative of this expression to zero, we find that optimal speedup is expected with  $N = C_1m/C_2$ . Plotting execution time of `ppadd` against the number of nodes  $N$  therefore allows us to evaluate the efficiency of thread creation and communication in a parallel architecture.

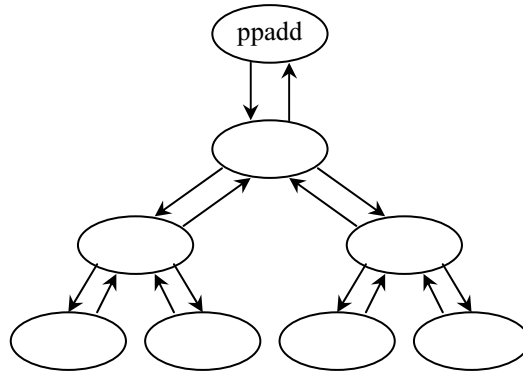


Figure 9-4: Parallel prefix addition thread structure.

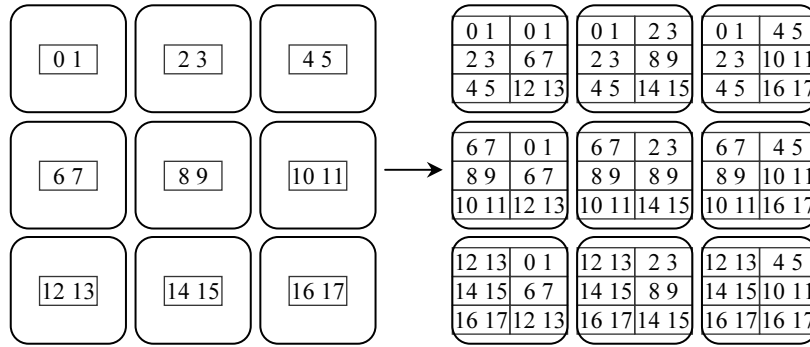
### 9.3.2 Quicksort

Quicksort is the archetypal randomized divide-and-conquer algorithm. The **quicksort** benchmark uses parallel vectors to perform quicksort on an array of integers. The top level quicksort function chooses a random pivot element, splits the vector into less-than and greater-than vectors, subdivides the processor set according to the  $M \log N$  ratio of expected work, redistributes the less-than and greater-than vectors to the two smaller processor sets, then recurses by creating two child threads. When the processor set consists of a single node, a fast sequential in-place quicksort is used.

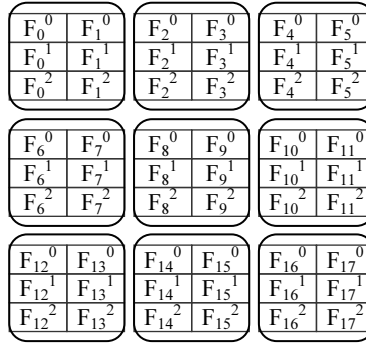
### 9.3.3 *N*-Body Simulation

The **nbody** benchmark performs 8 iterations of a 256 body simulation. Exact force calculations are performed, i.e. on each iteration the force between every pair of bodies is computed. Computation is structured for  $O(\sqrt{N})$  communication by conceptually organizing the processors into a square array; each processor communicates only with the other processors in the same row or column. An iteration consists of three phases. In the first phase, each processor broadcasts the mass and position of its bodies to the other processors in the same row and column. In the second phase, the processor in row  $i$  and column  $j$  computes, for each body in row  $i$ , the net force from all bodies in column  $j$ ; these partial forces are then forwarded to the appropriate processor in that row. Finally in the third phase the partial forces for each body are added up, and all velocities and positions are updated. This is illustrated in Figure 9-5 for 18 bodies on 9 processors. The key aspect of this benchmark is the inter-node synchronization that is required between the phases of an iteration when bodies and forces are passed from node to node.

phase 1



phase 2



**Figure 9-5:  $N$ -Body example with 18 bodies on 9 processors. In phase 1 bodies are broadcast to rows and columns. In phase 2 partial forces  $F_m^j$  of column  $j$  acting on body  $m$  are computed. In phase 3 (not shown) these forces are accumulated and the bodies are updated.**

### 9.3.4 Counting Words

In the final benchmark, **wordcount**, the number of occurrences of each word in [Brown02a] is computed. In the initial configuration, the text of this thesis is distributed across the machine. A distributed hash table is used to keep track of the words. A thread is created on each node to process the local portion of the text and isolate words. For each word, the distributed hash table node and index are computed, then the count for the word is incremented (creating a new entry in the hash table if necessary). Each location in the hash table contains a pointer to a linked list of words with the same hash value; these pointers must be locked and unlocked to ensure consistency when two or more threads attempt to access the same hash table location.

# Chapter 10

## Synchronization

*The days of the digital watch are numbered.*

– Tom Stoppard (1937- )

One of the most important aspects of a parallel computer is its support for synchronization. Inter-thread synchronization is required in parallel programs to ensure correctness by enforcing read-after-write data dependencies and protecting the integrity of shared data. All shared-memory multiprocessors provide, at minimum, atomic read-and-modify memory operations (e.g. *swap*, *test-and-set*). These operations are sufficient to implement higher-level synchronization primitives such as locks, semaphores, {I, J, L, M}-structures ([Arvind86], [Barth91], [Kranz92]), producer-consumer queues, and barriers. However, the overhead of synchronization primitives implemented with atomic memory operations alone can be quite high, so it becomes desirable to provide additional hardware support for efficient synchronization. In this chapter we discuss four synchronization primitives in the Hamal architecture: atomic memory operations, shared registers, register-based synchronization, and user trap bits.

### 10.1 Atomic Memory Operations

Hamal supports eight atomic read-and-modify memory operations, shown in Table 10-1. Each of these operations returns the original contents of the memory word. The operations can be performed on 8, 16, 32 or 64 bit words. Additionally, the three boolean operations can be performed on 128 bit words. The utility of atomic memory operations has been well established; we list those supported by Hamal for completeness only and focus our evaluation efforts on other synchronization primitives.

Instruction	Width (bits)	Operation
memadd	8, 16, 32, 64	word = word + data
memsub	8, 16, 32, 64	word = word - data
memrsub	8, 16, 32, 64	word = data - word
memand	8, 16, 32, 64, 128	word = word & data
memor	8, 16, 32, 64, 128	word = word   data
memxor	8, 16, 32, 64, 128	word = word ^ data
memmax	8, 16, 32, 64	word = max(word, data)
memmin	8, 16, 32, 64	word = min(word, data)

Table 10-1: Atomic memory operations.

## 10.2 Shared Registers

The Hamal processor contains eight shared registers g0-g7 which can be read by any context and written by contexts running in privileged mode. The primary purpose of these registers is to allow the kernel to export data to user programs, such as a pointer to the table of kernel calls and the instruction pointer for the frequently-called *malloc* routine. In addition, they allow shared data to be atomically read and modified by privileged-mode subroutines. Atomicity can be implemented by making use of both arithmetic data paths in a VLIW instruction group to simultaneously read and write a shared register. For example, the current implementation of the Hamal microkernel uses g0 as a malloc counter; it stores the 64 bit local address at which the next segment should be allocated. Figure 10-1 gives assembly code for the privileged *malloc* routine. The first instruction group (instruction groups are demarcated by periods) attempts to obtain the counter by simultaneously reading and resetting g0. If it is successful, the capability formed in r1 will have a non-zero address. If it is unsuccessful, indicating that another context currently holds the counter, then it spins until the counter is obtained. This implementation of *malloc* is extremely fast, running in only four cycles when the code is present in the instruction cache.

```

malloc:
.          r1 = gcap _CAP_BIG | _CAP_ALL, g0
.          g0 = move 0                ;; obtain the counter
.          p0 = test r1x, r1x         ;; p0 indicates success
.          r2 = alloc r1, r0a         ;; allocate the memory
. (p0)    r1 = askip r1, r0a         ;; advance the counter
. (p0)    r0 = move r2                ;; new pointer in r0
. (p0)    g0 = move r1x              ;; replace the counter
. (p0)    r1x = move 0               ;; destroy the capability
. (p0)    return
.          branch malloc              ;; spin on failure

```

Figure 10-1: Assembly code for malloc, which atomically reads & modifies g0.

### 10.3 Register-Based Synchronization

Hamal supports register-based synchronization via the *join*, *jcap* and *busy* instructions. The *jcap* instruction creates a *join capability* which, when given to other threads, allows them to use the *join* instruction to write directly to a register in the thread that created the capability. The *busy* instruction marks a register as busy, which will cause a thread to stall when it attempts to access this register until another thread uses *join* to write to it. This is similar to register-based synchronization in the M-Machine [Keckler98], but differs in two important respects. First, the mechanism is protected via join capabilities, so mutually untrusting threads can run on the same machine without worrying about unsolicited writes to their register files. Second, while the M-Machine restricts register-based synchronization to active threads running on the same physical processor, the Hamal *join* instruction can be used to write to an arbitrary local or remote thread in the system, and the *reply* event allows the microkernel to handle joins to threads which are not currently active.

One of the most important uses of register-based synchronization is to implement parent-child synchronization. A parent thread can initialize a child thread with a join capability allowing the child to write directly to one or more of the parent's registers. This allows both synchronization and one-way communication of data. A two-way communication channel can be established if the child thread passes a join capability back to its parent.

As an example, consider the *procs\_doacross* and *procs\_doacross\_sync* library routines. *procs\_doacross* starts a family of threads, one thread on every processor within a given processor set. It takes as arguments a processor set, the code address at which the threads should be started, and a set of arguments with which to initialize the threads. A call to *procs\_doacross* does not return until all threads have exited. The *procs\_doacross\_sync* function provides barrier synchronization for these threads. A call to *procs\_doacross\_sync* does not return until all other threads in the family have either exited or also called *procs\_doacross\_sync*.

*procs\_doacross* recursively creates a binary tree of threads with one leaf on each processor in the processor set. This tree of threads is used for both barrier and exit synchronization. Each thread in the tree is initialized with a join capability for its parent. To request barrier synchronization, a thread passes a join capability to its parent. The parent uses this join capability to signal the child once the barrier has passed. To exit, a thread simply passes NULL to its parent.



```

void procs_doacross_thread (ProcSet p, Code *func,
                           JCap *j, <args>)
{
    if (|p| == 1)           // If there's only one processor
        func(j, <args>);   // call the supplied function
    else
    {
        ProcSet (p1, p2) = Split(p);
        JCap j0, j1, j2, sync0, sync1, sync2, temp;

        j1 = JCap(sync1);   // Left child
        sync1 = busy;
        fork(middle_node(p1), procs_doacross_thread,
             p1, func, j1, <args>);

        j2 = JCap(sync2);   // Right child
        sync2 = busy;
        fork(middle_node(p2), procs_doacross_thread,
             p2, func, j2, <args>);

        while (sync1 || sync2) // while (one of the
        {                       // children called sync)
            j0 = JCap(sync0);
            sync0 = busy;
            join(j, j0);       // Ask parent for barrier
            test(sync0);      // Wait for signal from parent

            if (sync1)        // If left child did not exit
            {                 // then signal it
                temp = sync1; // Need to mark sync1 as
                sync1 = busy; // busy before joining
                join(temp, 0); // to avoid race condition!
            }
            if (sync2)        // If right child did not exit
            {                 // then signal it
                temp = sync2;
                sync2 = busy;
                join(temp, 0);
            }
        }
    }
    join(j, NULL); // Tell parent that we're done
}

```

**Figure 10-2: Register-based synchronization in *procs\_doacross* thread.**

Figure 10-2 gives pseudo-code for the main *procs\_doacross* thread. If the thread is a leaf node, it simply calls the user-supplied function and then exits. Otherwise, it splits the processor set, initiates left and right child threads, then enters a loop to service barrier requests from its children. Each barrier request is passed on to its parent. Figure 10-3 gives pseudo-code for the top-level *procs\_doacross* function which ultimately handles all barrier requests as well as the *procs\_doacross\_sync* function which sends a barrier request to the parent thread.

```

void procs_doacross (ProcSet p, Code *func, <args>)
{
    JCap j, sync, temp;

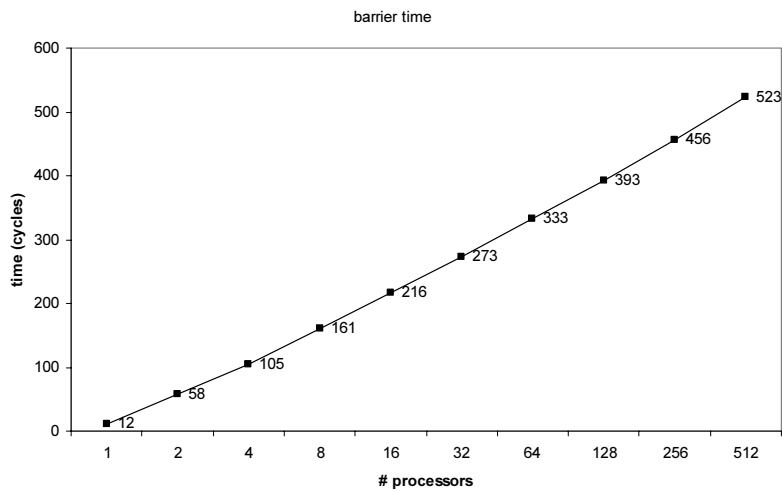
    j = JCap(sync);
    sync = busy;
    fork(middle_node(p), procs_doacross_thread,
        p, func, j, <args>);

    while (sync) // barrier request loop
    {
        temp = sync;
        sync = busy;
        join(temp, 0);
    }
}

void procs_doacross_sync (JCap *j)
{
    Word sync = busy;
    JCap j0 = JCap(sync);
    join(j, j0);
    test(sync);
}

```

**Figure 10-3: Register-based synchronization in top-level procs\_doacross and in barrier function.**



**Figure 10-4: Barrier time measured in machine cycles.**

The time required to perform a barrier synchronization using these library functions is plotted against machine size in Figure 10-4. These times were measured as the number of machine cycles between consecutive barriers with no intermediate computation. We see that register-based synchronization leads to an extremely efficient software implementation of barriers which outperforms even some previously reported hardware barriers (e.g. [Kranz93]). Furthermore, because no special hardware resources are required, multiple independent barrier operations may be performed simultaneously.

In a similar manner, the *ppadd* benchmark uses register-based synchronization to pass values between parent and child threads and to perform exit synchronization. Figure 10-5 shows a log-log plot of speedup versus machine size for *ppadd* on a  $2^{16}$  entry vector. Again, register-based synchronization permits efficient communication between threads which results in linear speedup over a wide range of machine sizes. Note that since the problem size is only  $2^{16}$ , the amount of work performed by each thread becomes quite small beyond 64 processor nodes.

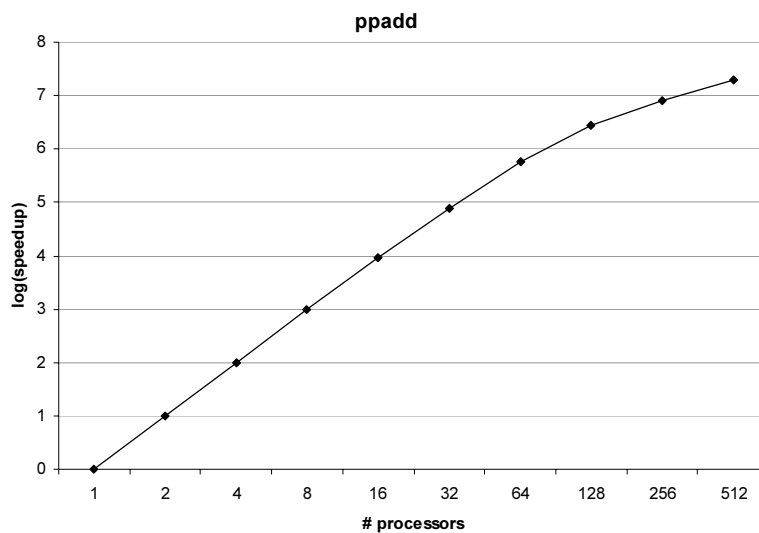


Figure 10-5: Speedup in parallel prefix addition benchmark.

## 10.4 UV Trap Bits

The fourth synchronization primitive provided in the Hamal architecture is user-controlled U and V trap bits associated with every 128-bit word of memory. Each memory operation may optionally specify both trapping

behaviour and how U and V should be modified if the operation succeeds. UV traps are a generalization of previous similar mechanisms ([Smith81], [Alverson90], [Kranz92], [Keckler98]). They differ in that a trap is not returned to the thread that issued the operation. Instead, an event is generated on, and handled by, the node containing the memory word being addressed. In this section we show how UV traps can be used to implement two common forms of synchronization: producer-consumer structures and locks.

#### 10.4.1 Producer-Consumer Synchronization

Producer-consumer synchronization is required when one thread passes data to another via a shared memory location. In the simple case where only one value is passed, the consumer must simply wait for the data to become available. In the more general case involving multiple values, the producer must also wait for the previous data to be consumed.

We can implement producer-consumer synchronization using the four states listed in Table 10-2. In the *empty* state the word contains no data. In the *full* state the word contains a single piece of data which is ready to be consumed. The *trap* state indicates either that the word is empty and the consumer is waiting, or that the word is full and the producer is waiting. Finally, the *busy* state indicates that a UV trap handler is currently operating on the word. The producer uses a store instruction that traps on U or V high and sets U. The consumer uses a load instruction that traps on U low or V high and clears U.

U	V	Meaning
0	0	empty
1	0	full
0	1	trap
1	1	busy

**Table 10-2: Producer-consumer states.**

Figure 10-6 gives pseudo-code for the producer-consumer trap handlers. Each handler begins by using the special *loaduv* instruction in a spin-wait loop to simultaneously lock the word and obtain its previous state (*empty*, *full* or *trap*). If the consumer attempts to read from an empty word, the load handler stores in the word a join capability which can be used to complete the load operation and sets the state to *trap*. The next time the producer attempts to write to the word the store handler will be invoked which will manually complete the consumer's load and set the state to *empty*. If the producer attempts to write to a full word, the store handler reads the previous value, replaces it with a join capability for one of its own registers, sets the state to *trap*, and uses register-based synchronization to

wait for a signal from the load handler. The next time the consumer attempts to read the word, the load handler will be invoked which will pass a join capability for the consumer to the store handler. Finally, the store handler uses this join capability and the old value to manually complete the consumer's load operation, then writes the new value to the word and sets the state to *full*.

```

trap_store:
    lock the word
    if (state == empty)
        complete store, clear V
    else if (state == full)
        swap old value with
        join capability
        wait for join capability
        from load handler
        complete load
        write new value, clear V
    else if (state == trap)
        read join capability,
        complete load, clear UV

trap_load:
    lock the word
    if (state == empty)
        write join capability,
        clear U
    else if (state == full)
        complete load, clear UV
    else if (state == trap)
        pass join capability to
        store handler

```

**Figure 10-6: Producer-consumer trap handlers.**

Producer-consumer synchronization is needed between the phases of an iteration in the *nbody* benchmark. Two versions of this benchmark were programmed: one using UV trap bits to implement fine-grained producer-consumer synchronization, and one using the global barrier synchronization described in Section 10.3. Table 10-3 compares the run times of the two versions. For small machine sizes in which the barrier overhead is extremely low the times are roughly the same, but as the machine size and barrier overhead increase the version using fine-grained synchronization begins to noticeably outperform the barrier version. For 256 nodes it runs nearly 9% faster; with this many nodes 2.6% of the loads and 1.7% of the stores caused UV traps. These results are very similar to those reported in [Kranz92].

# processors	1	4	16	64	256
barrier (cycles)	38555371	9690415	2479124	665263	212725
UV (cycles)	38583457	9703698	2476991	648438	195365
speedup	0.999272	0.998631	1.000861	1.025947	1.088859

**Table 10-3: Run times and speedup of UV synchronization vs. global barrier synchronization.**

## 10.4.2 Locks

Locks are one of the most fundamental and widely used synchronization primitives. They preserve the integrity of shared data structures by enforcing transactional semantics. Locks have traditionally been implemented as separately-allocated data structures. In the simplest case a single bit in memory indicates whether or not a lock is available; threads acquire a lock using an atomic memory operation that reads and sets the appropriate bit, and they release a lock by clearing the bit. This, however, is unsatisfactory for applications that need to maintain locks for a large number of small data structures (such as individual words). There are two specific problems. First, at least two extra memory references are required to access locked data: one to acquire the lock and one to release the lock. Second, extra storage is required for these locks. At minimum a single bit is needed for every lock, but this simple scheme only supports acquisition by spin-waiting. For more sophisticated waiting strategies involving thread blocking and wait queues, the lock must consist of at least an entire word.

In a tagged architecture with a *swap* instruction (such as Hamal), it is possible to finesse these problems by using a special tagged value to indicate that a word is locked. Spin-wait acquisition then consists of atomically swapping this LOCKED value with the desired word until it is obtained, and a lock is released simply by writing the value back to memory. This approach still requires the use of spin-waiting, the overhead of which consists of at least one test instruction, one branch, and possibly a number of network messages.

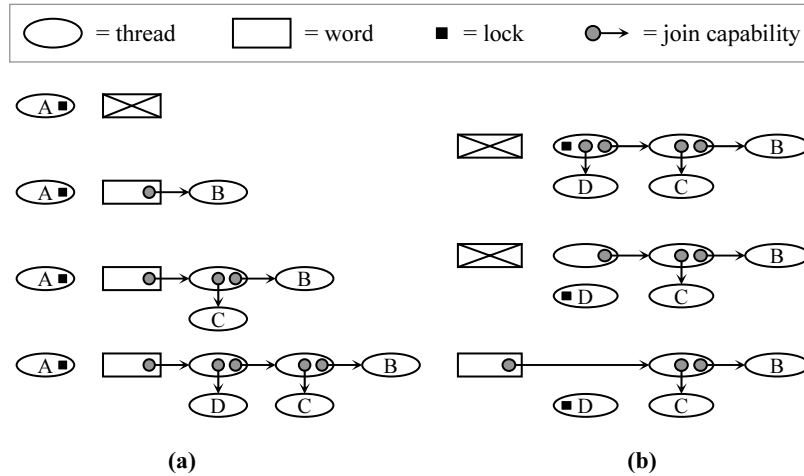
U and V trap bits can be used to implement word-level locking with minimal communication and no overhead in the absence of contention. We again make use of four states, shown in Table 10-4. A word is *available* if it is unlocked. When a word has been locked it is *unavailable* and its contents are undefined. The *trap* state indicates that at least one thread is waiting to acquire the lock; in this state the word contains a join capability for a thread or trap handler that has requested the lock. As before, the *busy* state indicates that a trap handler is currently operating on the word. A lock is acquired using a load operation that traps on U or V high and sets U. It is released using a store operation that traps on V high and clears U.

U	V	Meaning
0	0	available
1	0	unavailable
0	1	trap
1	1	busy

Table 10-4: Locked word states.

The first time that some thread attempts to acquire an unavailable lock, the trap handler simply stores a join capability for this thread in the word,

sets the state to *trap*, and exits. Trap handlers invoked by subsequent acquisition attempts swap this join capability with a join capability for one of their own registers, then use register-based synchronization to wait for the lock to be released. Thus, each waiting acquire handler stores two join capabilities: one for the thread that caused the acquire trap, and one that was previously stored in the memory word. When a thread attempts to release a lock which is in the *trap* state, the trap handler uses the join capability stored in the memory word to pass the lock on to the next requester and sets the state to *unavailable*. Finally, when a lock is passed to a waiting acquire handler, the handler uses its first join capability to pass on the lock. It then loops back to the start to re-handle the acquisition request corresponding to its second join capability. This is illustrated in Figure 10-7.



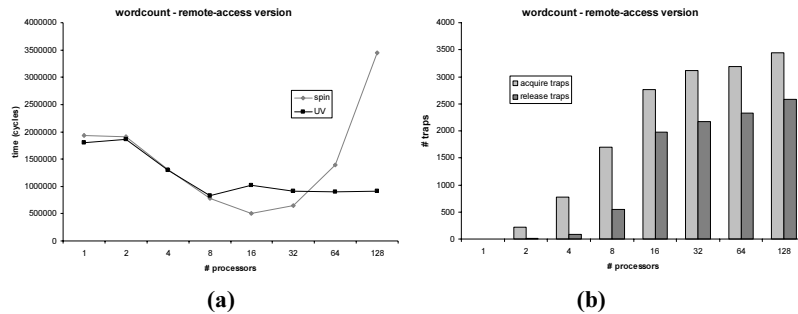
**Figure 10-7: (a) Threads A, B, C, D request a lock in that order. (b) Thread A releases the lock.**

In the wordcount benchmark, locks are required to preserve the integrity of the distributed hash table used to count words. In a *remote access* version of the benchmark, a single thread runs on each node and acquires these locks remotely. Two methods are used to acquire the locks: UV trap bits, as described above, and spin-waiting. The spin-wait version uses a special LOCKED value to acquire locks with a *swap* instruction, so the UV locking mechanism is being compared to the most efficient form of spin-waiting available.

Figure 10-8a gives execution time for both *remote access* versions of the wordcount benchmark as the number of processors is varied from 1 to 128. As the number of processors increases, so too does the contention for locks. This is shown in Figure 10-8b which gives the number of acquire and release traps for the UV version. There is a sequential bottleneck

caused by commonly occurring words such as ‘the’ (1775 occurrences) and ‘of’ (949).

With few processors (1-4) there is little contention, so the UV version marginally out-performs the spin-wait version due to the absence of test and branch instructions when a lock is acquired. For a medium number of processors (8-32) contention increases considerably, and the overhead of creating trap-handling threads in the UV version becomes a factor. Spin-waiting over a small network with few requestors is efficient enough to out-perform UV traps in this case. For a large number of processors (64+), the performance of spin-waiting becomes unacceptable as both the size of the network and the number of requestors increases. The performance of the UV version, by contrast, remains roughly constant even as the number of trap handler threads grows past 6000. This is due to a combination of fixed communication costs, which prevent performance degradation, and sequential bottlenecks, which eliminate the possibility of performance improvements.



**Figure 10-8: (a) Execution time for non-forking wordcount benchmark using both spin-waiting and UV traps. (b) Number of acquire and release traps for UV version.**

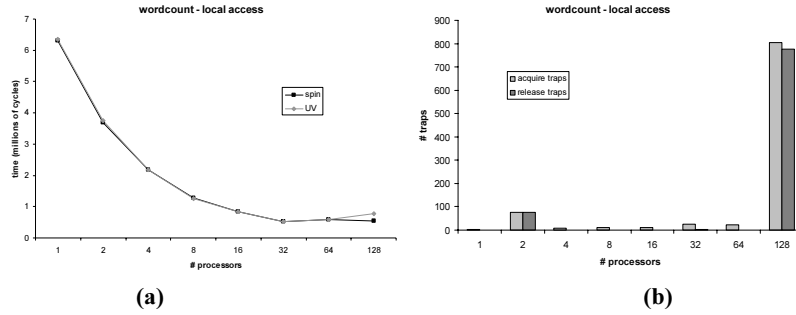
These results indicate that the primary benefit of the UV trapping mechanism is the automatic migration of the lock-requesting task from the source node to the destination node. This has two positive effects. First, it reduces network communication for remote lock acquisition to the absolute minimum: one message to request the lock, and another message when the lock is granted. The sequence is indistinguishable from a high-latency remote memory request. Second, when a lock is heavily requested (as in the wordcount benchmark), only the node on which the lock resides spends time managing the lock. The other nodes in the system do not have to waste cycles by spin-waiting.

To verify this conjecture, *local access* versions of the benchmark were programmed which create a thread for each word on the node containing the word’s hash table entry. These threads then acquire locks (which are



now always local) and update the hash table. With threads being manually migrated to the nodes containing the required locks, we would expect the performance advantages of the UV trapping mechanism to be lost.

Figure 10-9a plots execution times for the modified benchmark. Creating threads on the nodes containing the desired hash table entries dramatically reduces the amount of time that a given lock is held, which correspondingly lowers contention as shown in Figure 10-9b. With little contention there is no noticeable difference between the spin-wait and UV versions. For 128 processors when contention becomes significant, UV trap bits are indeed outperformed by spin-waiting.



**Figure 10-9: (a) Execution time for forking wordcount benchmark using both spin-waiting and UV traps. (b) Number of acquire and release traps for UV version.**

# Chapter 11

## The Hamal Processor

*I wish to God these calculations had been executed by steam.*

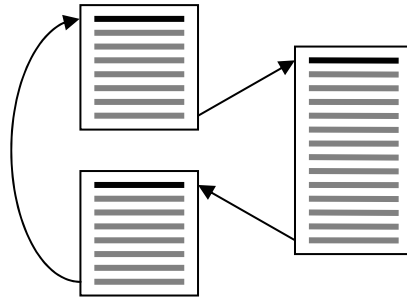
– Charles Babbage (1792-1871)

The Hamal processor combines a number of novel and existing mechanisms and is designed to provide high performance while minimizing complexity and silicon requirements. A full evaluation of its performance and features is unfortunately beyond this scope of this thesis; in this chapter we focus on the implementations of the instruction cache and hardware multithreading. Specifically, we investigate the extent to which instruction cache miss bits are able to reduce the instruction cache miss rate, and we evaluate the performance benefits of register dribbling as the number of hardware contexts is varied.

### 11.1 Instruction Cache Miss Bits

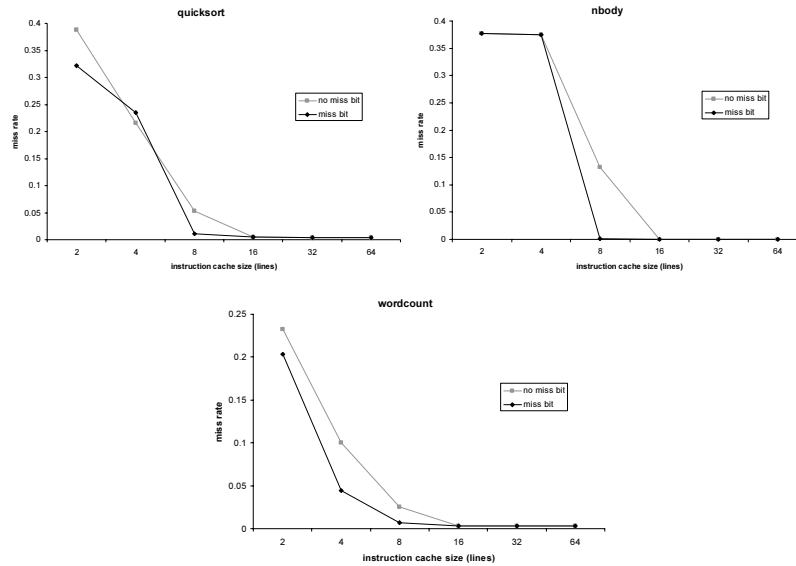
In the Hamal instruction cache, each cache line is tagged with a *miss bit* which indicates whether the cache line was prefetched or loaded in response to a cache miss. When the cache must select a line to replace, it preferentially selects lines with the miss bit clear. The motivation for this is that cache lines which were successfully prefetched in the past are likely to be successfully prefetched in the future.

As an example of the potential benefits of miss bits, consider the loop illustrated in Figure 11-1 which consists of 3 basic blocks. Suppose  $N$  cache lines are required to hold all the instructions in this loop. Without miss bits, a prefetching cache with fewer than  $N$  lines which uses LRU replacement will incur 3 cache misses on every pass through the loop: one miss at the start of each basic block. With miss bits, only 5 cache lines are required to avoid misses altogether: one for the start of each basic block, and 2 more to hold the current and next set of instructions.



**Figure 11-1: Loop containing 3 basic blocks. Grey instructions can be pre-fetched by the cache.**

To test the actual effectiveness of miss bits in reducing the number of cache misses, we ran the *quicksort*, *nbody* and *wordcount* benchmarks both with and without miss bits, varying the size of the instruction cache from 2 to 64 lines. We did not make use of the *ppadd* benchmark as the loops in this benchmark are extremely small and fit into a single instruction cache line. The *quicksort* benchmark was run on a  $2^{16}$  entry array. The remote access spin-waiting version of *wordcount* was used, and the barrier synchronization version of *nbody* was used. All benchmarks were run on 16 processors.



**Figure 11-2: Instruction cache miss rates for the quicksort, nbody and wordcount benchmarks.**

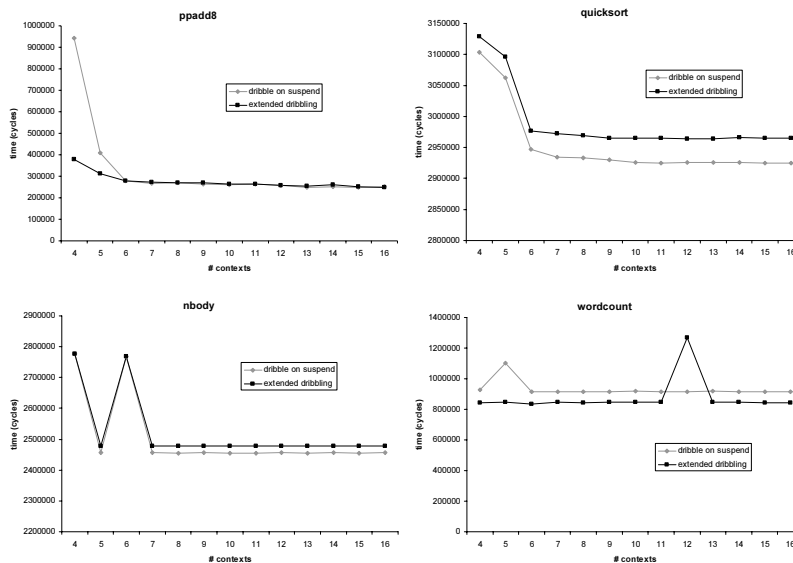
The results of these simulations are shown in Figure 11-2. As expected, miss bits are able to significantly reduce the miss rate for small cache sizes. Once the cache grows large enough to accommodate the inner loops of the benchmarks, the miss rates drops to nearly zero with or without miss bits. Miss bits are therefore a simple and effective mechanism for both improving the performance of small caches and reducing the miss rate in applications with large inner loops.

## 11.2 Register Dribbling

In a multithreaded architecture, *register dribbling* [Soundarar92] reduces the overhead of thread switching by allowing a context to be loaded or unloaded in the background while other contexts continue to perform useful computation. The Hamal processor extends this idea by maintaining a set of dirty bits for all registers and constantly dribbling the least recently issued (LRI) context to memory. Each time a dirty register is successfully dribbled (dribbling can only take place on cycles in which no thread is initiating a memory request), the register is marked as ‘clean’. We will refer to this strategy as *extended dribbling*.

By dribbling a context’s registers to memory in advance of the time at which the context is actually suspended, extended dribbling reduces the amount of time required to save the state of the context to memory. This in turn reduces the latency between the decision to suspend a thread and the activation of a new thread. The disadvantage of extended dribbling is that even though it makes use of cycles during which the processor is not accessing memory, a successful dribble will occupy a memory bank for the amount of time required to perform a write operation in the embedded DRAM (this is modeled as three machine cycles in the Hamal simulator). Thus, memory requests generated immediately after a dribble and targeted at the same memory bank will be delayed for two cycles.

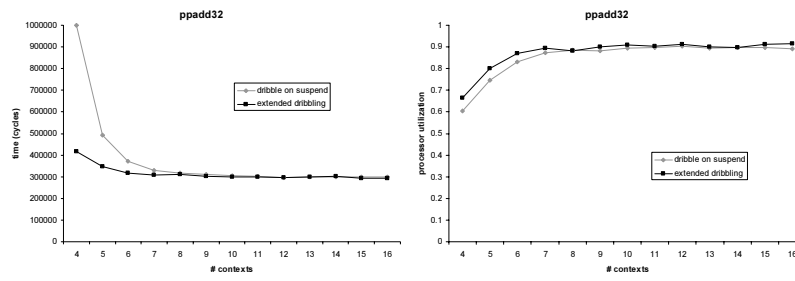
It is impossible to determine *a priori* whether or not the benefits of extended dribbling outweigh its costs, so as usual we resort to simulation. All four benchmarks were run both with and without extended dribbling with the number of hardware contexts varying from 4 to 16. With extended dribbling, a *stall* event is generated when there are less than two free contexts, no context can issue, and the LRI context is clean. Without extended dribbling this last condition is dropped, so *stall* events are generated sooner than they would be otherwise. Since the *ppadd* benchmark only creates two threads on each node (one internal node and one leaf node in the thread tree), 8 instances were run simultaneously. The *quicksort* benchmark was run on a  $2^{16}$  entry array. To maximize the number of threads, UV trap bit synchronization was used for both the *nbody* and *wordcount* benchmarks, and the local access version of *wordcount* was used. All benchmarks were again run on 16 processors.



**Figure 11-3: Execution time vs. number of contexts with and without extended dribbling.**

The resulting execution times are shown in Figure 11-3. The two exceptional data points in the *wordcount* benchmark resulted from a thread being swapped out while it held a lock that was in high demand. In *ppadd* and *wordcount*, which make heavy use of thread swapping, we see that extended register dribbling offers a performance advantage (~8% in *wordcount*). By contrast, both *quicksort* and *nbody* feature threads which run for long periods of time without being swapped out, so in these cases extended register dribbling actually degrades performance slightly (~1% in each case). On the whole, our initial conclusion is that extended dribbling helps more than it hurts.

We were surprised to find that increasing the number of contexts beyond 6 offers little or no performance gains in any of the benchmarks, even in *ppadd8* which creates many threads on each node. Running this benchmark again with 32 simultaneous instances produces similar results, shown in Figure 11-4, which graphs both execution time and processor utilization. In retrospect this result should not have been surprising; the simple explanation is that 6 or 7 concurrent *ppadd* threads are able to fully saturate the processor's interface to memory. This also explains why extended dribbling has almost no effect with 8 or more contexts: if the processor is generating a memory request on every cycle, then the LRI context will never dribble. In the other three benchmarks, the flat performance curves are due to a lack of sufficient parallelism.



**Figure 11-4: Execution time and processor utilization vs. number of contexts for ppadd32.**



# Chapter 12

## Squids

*"Its head," rejoined Conseil, "was it not crowned with eight tentacles, that beat the water like a nest of serpents?"*

– Jules Verne (1828-1905), “20,000 Leagues Under the Sea”

Squids (Short Quasi-Unique IDentifiers) were introduced in Chapter 3 as a way of mitigating the effects of forwarding pointer aliasing. The theoretical motivation for squids is that by assigning a short random tag to objects, pointers to different objects can be disambiguated with high probability. This avoids expensive dereferencing operations when performing pointer comparisons, and prevents the processor from having to wait for every split-phase memory operation to complete before initiating the next one. In this chapter we discuss experiments performed using the Hamal simulator to quantify the performance advantages of squids.

### 12.1 Benchmarks

Table 12-1 lists the eight benchmarks used to evaluate squids. The first five (*list*, *2cycle*, *kruskal*, *fibsort*, *sparsemat*) involve pointer comparisons and the primary overhead is traps taken to determine final addresses. The last three (*vector*, *filter*, *listrev*) involve rapid loads/stores and the primary overhead is memory stalls when addresses cannot be disambiguated.

It was necessary to carefully choose these benchmarks as most programs either do not make use of pointer comparisons, or compare them so infrequently that slow comparisons would have no impact on performance. Nonetheless, as exemplified by the benchmarks, there are some fundamental data structures for which pointer comparisons are frequently used. One common example is graphs, in which pointer comparisons can be used to determine whether two vertices are the same. Both *2cycle* and *kruskal* are graph algorithms. *2cycle* uses a brute force approach to detect 2-cycles in a directed graph by having each vertex look for itself in the connection lists of its neighbours. *kruskal* uses Kruskal’s minimum spanning tree algorithm [CLR90] in which edges are chosen greedily without creating cycles. To



avoid cycles, a representative vertex is maintained for every connected subtree during construction, and an edge may be selected only if the vertices it connects have different representatives.

Benchmark	Description	Parameters
list	Add/delete objects to/from a linked list	32 objects in list, 1024 iterations
2cycle	Detect 2-cycles in a directed graph	1024 vertices, 10,240 edges
kruskal	Kruskal's minimal spanning tree	512 vertices, 2048 edges
fibsort	Fibonacci heap sort	4096 keys
sparsemat	Sparse matrix multiplication	32x32 matrix with 64 entries; 5 iterations of $B = A * (B + A)$
vector	$a_i = x_i * y_i$ $b_i = x_i + y_i$ $c_i = x_i - y_i$	20,000 terms
filter	$y_i = .25 * x_{i-1} + .5 * x_i + .25 * x_{i+1}$	200,000 terms
listrev	Reverse the pointers in a linked list	30,000 nodes

**Table 12-1: Benchmark programs.**

Another important data structure which makes use of pointer comparisons is the cyclically linked list. Figure 2 gives C code for iterating over all elements of a non-empty cyclically linked list; a pointer comparison is used as the termination condition. This differs from a linear linked list in which termination is determined by comparing a pointer to NULL. Both *fibsort* and *sparsemat* make use of cyclically linked lists. *fibsort* sorts a set of integers using Fibonacci heaps [Fredman87]; in a Fibonacci heap the children of each node are stored in a cyclically linked list. *sparsemat* uses an efficient sparse matrix representation in which both the rows and columns are kept in cyclically linked lists.

```

Node *p = first;
do
{
    ...
    p = p->next;
} while (p != first);

```

**Figure 12-1: Iterating over a cyclically linked list.**

In the *list* benchmark, 32 objects are stored in both an array and a linked list. On each iteration, an object is randomly selected from the array and located in the linked list using pointer comparisons. The object is deleted, and a new object is created and added to both the array and the linked list. Every 64 iterations the list is linearized [Clark76]; this is one of the locality optimizations performed in [Luk99]. This benchmark is somewhat contrived; it was constructed to provide an example in which squids are unable to asymptotically reduce overhead to zero. Because the pointers in the array are not updated, subsequent to a linearization comparisons will be made between pointers having different levels of forwarding indirection. In particular, an object will be found by comparing two pointers to the same

object with different levels of indirection. This is one of the two cases in which squids fail. Previously it was argued that this may be a rare case in general, however it is a common occurrence in the *list* benchmark.

The overhead of forwarding pointer dereferencing is potentially quite large, especially if there is a deep chain of forwarding pointers, a remote memory reference is required, or, in the worst case, a word in the forwarding chain resides in a page that has been sent to disk. For the purposes of evaluation, we wish to minimize this overhead *before* introducing squids in order to avoid exaggerating their effectiveness. Accordingly, all benchmarks are run as a single thread on a single node and fit into main memory. Additionally, we emulate a scenario in which data has been migrated at least once by setting the migrated (M) bit in all capabilities.

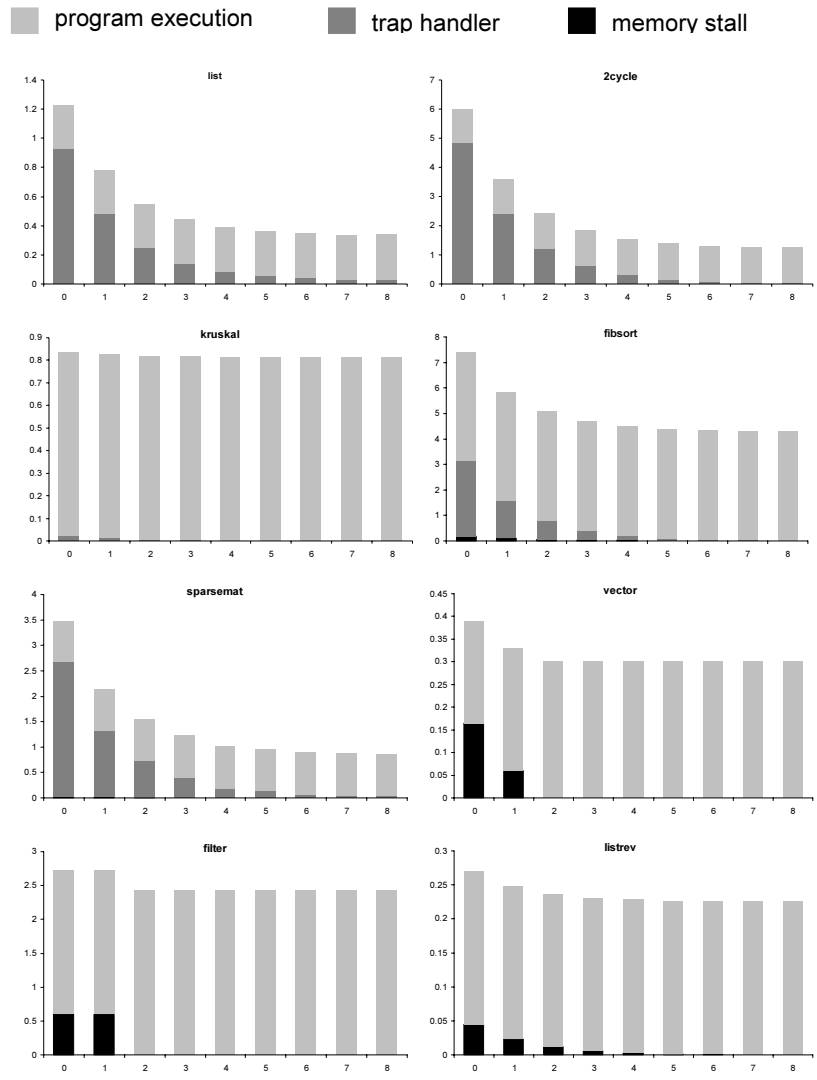
## 12.2 Simulation Results

Figure 12-2 shows the results of running all eight benchmark programs with the number of squid bits varying from 0 to 8. Execution time is broken down into program cycles, trap handler cycles, and memory stalls. A cycle is counted as a memory stall when the hardware is unable to disambiguate different addresses and as a result a memory operation is blocked. Table 12-2 lists the total speedup of the benchmarks over their execution time with zero squid bits.

As expected, in most cases the overhead due to traps and memory stalls drops exponentially to zero as the number of squid bits increases. The three exceptions are *list*, *vector* and *filter*. In *vector* and *filter* the lack of a smooth exponential curve is simply due to the small number of distinct objects (five in *vector*, two in *filter*), so in both cases the overhead steps down to zero once all objects have distinct squids. In *list* the overhead drops exponentially to a non-zero amount. This is because squids offer no assistance in comparisons of two pointers to the same object with different levels of indirection.

Squid bits:	1	2	3	4	5	6	7	8
list	1.57	2.22	2.76	3.16	3.41	3.55	3.62	3.65
2cycle	1.66	2.47	3.27	3.91	4.32	4.56	4.68	4.75
kruskal	1.01	1.02	1.02	1.02	1.02	1.03	1.03	1.03
fibsort	1.26	1.46	1.58	1.65	1.69	1.70	1.71	1.72
sparsemat	1.62	2.24	2.83	3.41	3.57	3.92	3.98	4.00
vector	1.18	1.30	1.30	1.30	1.30	1.30	1.30	1.30
filter	1.00	1.12	1.12	1.12	1.12	1.12	1.12	1.12
listrev	1.09	1.14	1.17	1.18	1.19	1.20	1.20	1.20

Table 12-2: Speedup over execution time with zero squid bits.



**Figure 12-2: Squid simulation results.** For each benchmark the horizontal axis indicates the number of squid bits used and the vertical axis gives the execution time in millions of cycles. Execution time is broken down into program cycles, trap handler cycles and memory stall cycles.

We note that squids are most effective in programs that compare pointers within the inner loop. This includes *list*, *2cycle*, *fibsort* and *sparsemat*, where the speedup with eight squid bits ranges from 1.72 for *fibsort* to 4.75 for *2cycle*. In *kruskal*, by contrast, the inner loop follows a chain of point-

ers to find a vertex's representative; only once the representatives for two vertices have been found is a pointer comparison performed. As a result, the improvement in performance due to squids is barely noticeable.

Squids are also helpful, albeit to a lesser extent, in the three memory-intensive benchmarks. With eight squid bits the speedup ranges from 1.12 in *filter* to 1.30 in *vector*. Note that in each of these benchmarks, as the number of squid bits is raised the decrease in overall execution time is slightly less than the decrease in the number of memory stalls. This is because programs are allowed to continue issuing arithmetic instructions while a memory request is stalled, so in some cases there is overlap between memory stalls and program execution. Overlap cycles have been graphed as memory stall cycles.

### 12.3 Extension to Other Architectures

The design space of capability architectures is quite large, so we must call into question the extent to which our results would generalize to other architectures. In particular, the execution time of the trap handler (which is roughly 48 cycles from start to finish in our simulations) may be significantly smaller in an architecture with data caches or extra registers available to the trap handler. However, we note that:

1. Any mechanism that speeds up the trap handler but is not specific to traps (e.g. data caches, out-of-order execution) will most likely reduce program execution time comparably, keeping the percentage of trap handler cycles the same.
2. Hardware improvements reduce the cost but not the number of traps. Squids reduce the number of traps exponentially independent of the architecture.

The number of memory operations that the hardware fails to reorder or issue simultaneously *is* architecture dependent since it is affected by such factors as memory latency and the size of the instruction reorder buffer (if there is one). If the overhead due to memory stalls in memory intensive applications is negligible to begin with, then the architecture will not benefit from adding squids to the memory controller logic. On the other hand if the overhead is noticeable, then squids will reduce it exponentially.

### 12.4 Alternate Approaches

We have focused our evaluations on the specific implementation of squids in the Hamal architecture, i.e. a hardware-recognized field within capabilities. A number of other approaches to the problem of pointer disambiguation can be used in place of or in addition to this technique.

### 12.4.1 Generation Counters

We can associate with each pointer an  $m$  bit saturating generation counter which indicates the number of times that the object has been migrated. If two pointers being compared have the same generation counter (and it has not saturated), then the hardware can simply compare the address fields directly.

The migrated (M) bit in Hamal capabilities is a single-bit generation counter that deals with the common case of objects that are never migrated. This completely eliminates aliasing overhead for applications that choose not to make use of forwarding pointers. Using two generation bits handles the additional case in which objects are migrated exactly once as a compaction operation after the program has initialized its data (this is one of the techniques used in [Luk99]). Again, overhead is completely eliminated in this case.

More generally, generation counters are effective in programs for which (1) objects are migrated a small number of times, and (2) at all times most working pointers to a given object have the same level of indirection. They lose their effectiveness in programs for which either of these statements is false.

### 12.4.2 Software Comparisons

Instead of relying on hardware to ensure the correctness of pointer comparisons, the compiler can insert code to explicitly determine the final addresses and then compare them directly, as in [Luk99]. Figure 12-3 shows the code that must be inserted; for each pointer a copy is created, and the copy is replaced with the final address by repeatedly checking for the presence of a forwarding pointer in the memory word being addressed. The outer loop is required in systems that support concurrent garbage collection or object migration to avoid a race condition when an object is migrated while the final addresses are being computed. In a complex superscalar processor, the cost of this code may only be a few cycles (and a few registers) if the memory words being addressed are present in the data cache. The overhead will be much larger if a cache miss occurs while either of the final addresses is being computed.

Making use of hardware traps, and placing this code in a trap handler rather than inlining it at every pointer comparison, has the advantages of reducing code size and eliminating overhead when the hardware is able to disambiguate the pointers. On the other hand, overhead is increased when a trap is taken due to the need to initialize the trap handler and clean up when it has finished. In our simulations, we found that 25% of the trap cycles were used to perform the actual comparisons. Thus, using software comparisons would give roughly the same performance as hardware comparisons with two squid bits.

```

temp1 = ptr1;
temp2 = ptr2;
flag = 0;
do
{
    while (check_forwarding_bit(temp1))
        temp1 = unforwarded_read(temp1);
    while (check_forwarding_bit(temp2))
    {
        temp2 = unforwarded_read(temp2);
        flag = 1;
    }
} while (flag);
compare(temp1, temp2);

```

**Figure 12-3: Using software only to ensure the correctness of pointer comparisons, the compiler must insert the above code wherever two pointers are compared.**

The cost of software comparisons can be reduced (but not eliminated) by incorporating squids, as shown in Figure 5. This combined approach features both exponential reduction in overhead and fast inline comparisons at the expense of increased code size and register requirements.

```

temp = ptr1 ^ ptr2;
if (temp & SQUID_MASK)
    <pointers are different>
else
    <compare by dereferencing>

```

**Figure 12-4: Using squids in conjunction with software comparison.**

### 12.4.3 Data Dependence Speculation

In [Luk99], the problem of memory operation reordering is addressed using *data dependence speculation* ([Moshovos97], [Chrysos98]). This is a technique that allows loads to speculatively execute before an earlier store when the address of the store is not yet known. In order to support forwarding pointers, the speculation mechanism must be altered so that it compares final addresses rather than the addresses initially generated by the instruction stream. This in turn requires that the mechanism is somehow informed each time a memory request is forwarded. The details of how this is accomplished would depend on whether forwarding is implemented directly by hardware or in software via exceptions.

Data dependence speculation does not allow stores to execute before earlier loads/stores, but this is unlikely to cause problems as a store does not produce data which is needed for program execution. A greater concern is the failure to reorder atomic read-and-modify memory operations, such as those supported by Tera [Alverson90], the Cray T3E [Scott96], or Hamal.

#### 12.4.4 Squids without Capabilities

It is possible to implement squids without capabilities by taking the upper  $n$  bits of a pointer to be that pointer's squid. This has the effect of subdividing the virtual address space into  $2^n$  domains. When an object is allocated, it is randomly assigned to one of the domains. Objects migration is then restricted to a single domain in order to preserve squids.

Using a large number of domains introduces fragmentation problems and makes data compaction difficult since, for example, objects from different domains cannot be placed in the same page. However, as seen in Section 12.2, noticeable performance improvements are achieved with only one or two squid bits (two or four domains).

Alternately, the hardware can cooperate to avoid the problems associated with multiple domains by simply ignoring the upper  $n$  address bits. In this case the architecture begins to resemble a capability machine since the pointer contains both an address and some additional information. The difference is that the pointers are unprotected, so user programs must take care to avoid mutating the squid bits or performing pointer arithmetic that causes a pointer to address a different object. Additionally, because the pointer contains no segment information, arrays of objects are still a problem since a single squid would be created for the entire array.

### 12.5 Discussion

Forwarding pointers facilitate safe data compaction, object migration, and efficient garbage collection. In order to address the aliasing problems that arise, the Hamal architecture implements squids, which allow the hardware to, with high probability, disambiguate pointers in the presence of aliasing without performing expensive dereferencing operations. Our experimental results show that squids provide significant performance improvements on the small but important set of applications that suffer from aliasing, speeding up some programs by over a factor of four.

The fact that the overhead associated with forwarding pointer support diminishes exponentially with the number of squid bits has two important consequences. First, very few squid bits are required to produce considerable performance improvements. Even a single squid bit provides noticeable speedups on the majority of the benchmarks, and as Figure 12-2 shows, most of the potential performance gains can be realized with four bits. Thus, squids remain appealing in architectures which have few capability bits to spare. Second, squids allow an architecture to tolerate slow traps and/or long memory latencies while determining final addresses. For most applications, three or four additional squid bits would compensate for an order of magnitude increase in the time required to execute the pointer comparison code of Figure 12-3.

# Chapter 13

## Analytically Modeling a Fault-Tolerant Messaging Protocol

*Models are to be used, not believed.*

– Henri Theil (1924-2000), “Principles of Econometrics”

Analytical models are an important tool for the study of network topologies, routing protocols and messaging protocols. They allow evaluations to be conducted without expensive simulations that can take hours or even days to complete. However, analytically modeling a fault-tolerant messaging protocol is challenging for several reasons:

- There are multiple packet types (at least two are required: ‘message’ and ‘acknowledge’)
- Many packets must be re-sent
- The future behaviour of the network depends on which packets have been successfully received

In this chapter we present a simple approach to the analysis of fault-tolerant protocols that accurately models these effects while hiding many of the other protocol details. We are able to solve for key performance parameters by considering only the rates at which the different types of packets are sent and the probabilities that they are dropped at various points in the network once the system has reached a steady state. Our method is quite general and can be applied to various topologies and routing strategies. We will demonstrate the accuracy of the models obtained by comparing them to simulated results for the idempotent messaging protocol described in Chapter 5 implemented using both circuit switching and worm-hole routing on three different network topologies.

The literature contains a myriad of analytical models for dynamic network behaviour. Models have been proposed for specific network topologies ([Dally90], [Stamoulis91], [Saleh96], [Greenberg97]), routing algorithms ([Draper94], [Sciedeler96], [Ould98]), and traffic patterns [Sar-



bazi00]. While the vast majority of this work has focused on non-discarding networks, discarding networks have also been considered ([Parviz79], [Rehrmann96], [Datta97]). However, in [Rehrmann96] and [Datta97] packet retransmission was not modeled. In [Parviz79] the model did take into account packet retransmission, but a magic protocol was used whereby the sending node was instantly and accurately informed as to the success or failure of a packet. Our work differs from previous research in that we present an accurate model for the higher-level messaging protocol required to ensure packet delivery across a faulty network.

### 13.1 Motivating Problem

Our work was motivated by an attempt to analytically answer the following question: Given a desire to implement the idempotent messaging protocol on a bisection-limited network, should one use wormhole routing or circuit switching? In a wormhole routed network, all three protocol packets are independently routed through the network; all three are subject to being discarded due to contention within the network. In a circuit switched network, only the MSG packet is routed through the network. A connection is maintained along the path that it takes, and the ACK and CONF packets are sent through this connection. They can still be lost due to corruption, but not due to contention. On one hand, wormhole routing generally makes more efficient use of network resources. On the other hand, circuit switching capitalizes on a successful MSG route through the network bisection by holding the channel open for the ACK and CONF packets. We will answer this question in Section 13.3.4 after deriving models for both wormhole routing and circuit switching on a bisection-limited network.

### 13.2 Crossbar Network

To introduce our technique, we begin with the simplest of networks: a crossbar. Specifically, we assume a pipelined crossbar of diameter  $d$  where the head of each packet takes  $d$  cycles to reach its destination and there is no contention within the network. Each node has one receive port. When a packet reaches its destination node it is delivered if the receive port is free and it is discarded otherwise.

In all that follows, we assume that each node generates messages independently at an average rate of  $\lambda$  messages per cycle, and that message destinations are chosen randomly. MSG packets are  $L$  flits long; ACK and CONF packets are each  $m$  flits long. For all networks that we consider, we assume that packets are lost due to contention only. We do not model network failures.

### 13.2.1 Circuit Switched Crossbar

To derive our models, we use the standard approach of assuming that the network reaches a steady state and then solving for the steady state parameters. For uniform traffic on a circuit switched crossbar, there are two parameters of interest: the rate  $\alpha$  at which each node attempts to send messages, and the probability  $p$  that a message is successfully delivered when it reaches its destination.

With only two parameters, we need only two equations. Our first equation comes from *conservation of messages*: messages must be successfully delivered at the same rate that they are generated, hence

$$\lambda = \alpha p \quad (1)$$

Our second equation comes from *port utilization*: the probability that a message is dropped at the receive node ( $1 - p$ ) is equal to the probability that the receive port is in use. When a message is dropped, it uses zero receive port cycles. Using circuit switching, when a message is successfully received it uses  $2d + L + 2m$  receive port cycles ( $L$  cycles to absorb the MSG packet,  $d$  cycles to send the ACK packet to the sender,  $m$  cycles for that packet to be absorbed,  $d$  cycles to send the CONF packet to the receiver, finally  $m$  cycles for that packet to be absorbed). Thus, each node causes receive port cycles to be used at a rate of  $\alpha p(2d + L + 2m)$ . Since the number of senders is equal to the number of receivers, this is the probability that a receive port will be in use, so

$$1 - p = \alpha p(2d + L + 2m) \quad (2)$$

Finally, we use (1) and (2) to solve for  $p$ :

$$p = 1 - \lambda(2d + L + 2m) \quad (3)$$

### 13.2.2 Wormhole Routed Crossbar

The wormhole model is more complicated as we must consider the various protocol packets separately. Let  $\alpha$ ,  $\beta$ ,  $\gamma$  be the rates at which a node sends MSG, ACK and CONF packets respectively in steady state. As before, let  $p$  be the probability that a packet is successfully delivered (this is independent of the packet type).

Our port utilization equation is similar to (2). When a MSG packet is successfully delivered it uses  $L$  receive port cycles. When an ACK or CONF packet is delivered it uses  $m$  receive port cycles. Hence, each node causes receive port cycles to be used at a rate of  $p(\alpha L + (\beta + \gamma)m)$ , so

$$1 - p = p(\alpha L + (\beta + \gamma)m) \quad (4)$$

Note that  $\alpha L + (\beta + \gamma)m$  is the fraction of cycles during which a node is injecting a packet into the network; it is therefore  $\leq 1$ . It follows from (4) that  $1 - p \leq p$ , or  $p \geq 0.5$ . This implies that the network *cannot* reach a steady state unless the probability of successful delivery is  $\geq 0.5$ .

Our next three equations are conservation equations: conservation of messages, acknowledgements and confirms. The rate  $\lambda$  at which messages are generated must be equal to the rate at which they are forgotten in response to ACK packets. ACK packets are received at a rate of  $p\beta$ , but in general multiple ACK's may be received for a single message, and only the first of these causes the message to be forgotten. A receiver will periodically send ACK's until it receives a CONF. Since the probability of receiving a CONF after sending an ACK is  $p^2$  (both packets must be delivered successfully), the expected number of ACK's sent before a conf is received is  $1/p^2$ . Of these, it is expected that  $1/p$  will be successfully delivered. Hence, if an ACK is received, the probability that it is the *first* ACK in response to the message is  $p$ , so our conservation of messages equation is:

$$\lambda = p^2\beta \quad (5)$$

Next, the rate at which ACK's are created must be equal to the rate at which they are destroyed. We consider an ACK to exist for the duration of time that a receiver remembers the corresponding message. The rate of destruction is simply  $p\gamma$  because every CONF that is successfully delivered destroys an ACK. The rate of creation is slightly trickier to compute as again it is only the *first* time a message is received that an ACK is created.

Let  $x$  be the expected number of times that a message is sent. With probability  $1 - p$  a message is not delivered, in which case we expect it to be sent  $x$  more times. With probability  $p$  it *is* delivered, and the receiver will begin sending ACK's. If we assume the approximation that the protocol retransmits MSG's and ACK's at the same rate, then in this case we expect the number of messages sent by the sender to be equal to the number of ACK's sent by the receiver before one is received. This in turn is  $1/p$  since the probability of a given ACK being received is  $p$ . It follows that:

$$x = p(1/p) + (1 - p)(x + 1) \quad (6)$$

Solving for  $x$ :

$$x = 2/p - 1 \quad (7)$$

The expected number of times a message is received is therefore  $px = 2 - p$ . Thus, when a message is received the probability that it is the *first* copy received (and hence creates an ACK) is  $1/(2 - p)$ , so our equation for conservation of ACK's is:

$$p\alpha / (2 - p) = p\gamma \quad (8)$$

which we rewrite as:

$$\alpha = (2 - p)\gamma \quad (8')$$

Finally, a CONF is created every time an ACK is received and it is forgotten as soon as it is sent, so our equation for conservation of CONF's is:

$$\gamma = p\beta \quad (9)$$

Let  $T = 1/\lambda$ , so  $T$  is the average amount of time in cycles between the generation of new messages on a node. Eliminating  $\alpha$ ,  $\beta$ ,  $\gamma$  from equations (4), (5), (8) and (9) leaves us with the following quadratic in  $p$ :

$$f(p) = (T - L)p^2 + (2L + m - T)p + m = 0 \quad (10)$$

Solving for  $p$ :

$$p = \frac{(T - L) - L - m \pm \sqrt{\Delta}}{2(T - L)} \quad (11)$$

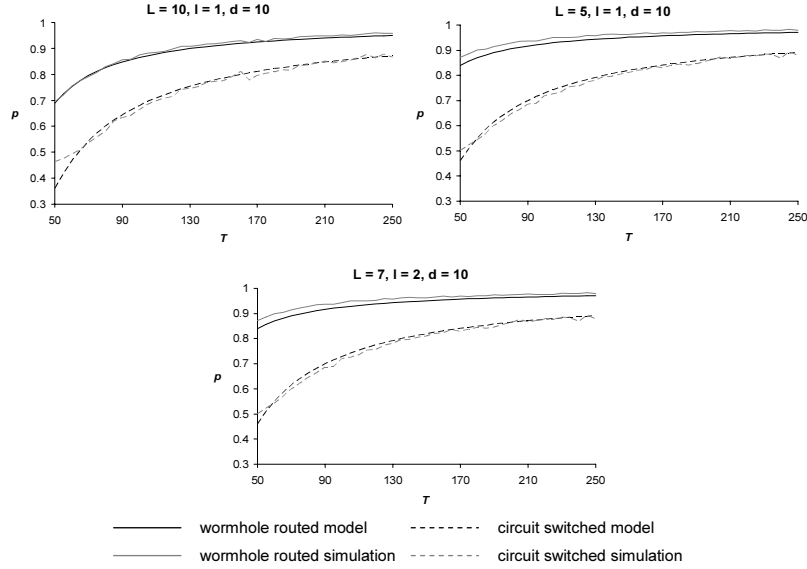
Where  $\Delta$  is the discriminant of  $f$ . Recall that for the solution to be meaningful we must have  $p \geq 0.5$ . But if  $f$  has real roots then we see from (11) that the smaller root is less than 0.5, so it is the larger root that we are interested in. Furthermore,  $f(1) = L + 2m > 0$ , so it follows that  $f$  has a real root in  $[0.5, 1)$  if and only if  $f(0.5) \leq 0$ . Substituting this into (9) gives us the following necessary and sufficient condition for a meaningful solution to exist:

$$T \geq 3(L + 2m) \quad (12)$$

### 13.2.3 Comparison with Simulation

Simulations were performed of the idempotent messaging protocol using both circuit switching and wormhole routing on a crossbar network with  $d = 10$ . On every simulated cycle a node generates a new message to send with probability  $\lambda$ . A node's send queue is allowed to grow arbitrarily long, and nodes are always able to accept packets from the network so long as their receive port is free. For the wormhole network, MSG and ACK packets are retransmitted at a fixed interval of twice the network round-trip latency. Additionally, if a node has more than one packet which is ready to be sent, preference is given to ACK and CONF packets.

In Figure 13-1 we compare the results of the simulations to the predictions of our models for three different values of  $L$  and  $m$ . The graphs plot  $p$ , the probability of successful delivery, versus  $T$ , the average time between message generation on a node. In all cases the model agrees closely with simulation results. Note that the graphs diverge slightly for small values of  $T$  on a circuit switched network. This is due to the fact that in simulation a steady state was never reached for these values of  $T$ ; the size of the send queues continued to increase for the duration of the simulation.



**Figure 13-1: Simulated and predicted values of  $p$  plotted against  $T$  for both circuit switched and wormhole routed crossbar networks.**

The probability  $p$  is all that is required to determine the performance characteristics of the network. For example, in the wormhole routed network the expected number of message transmissions is given by (7), and in both networks the expected latency from initial message transmission to message reception is

$$d + L + \frac{1-p}{p} R \quad (13)$$

where  $R$  is the retransmission interval for a message packet. Note that the value of  $p$  does not depend on  $R$ ; this is one of the ways in which our model hides the details of the protocol implementation. Our only assumption has been that the same retransmission interval is used for both MSG and ACK packets.

### 13.2.4 Improving the Model

Inspecting the graphs of Figure 13-1 reveals a small but consistent discrepancy between the model and simulation. This is most noticeable for wormhole routing with  $L = 5, 7$ . The source of this error is an inaccuracy in our port utilization equations (2) and (4). In deriving these equations, we made the assumption that in steady state a fixed fraction of receive ports are always in use, and that this fraction is the probability of a message being dropped. However, in a discrete time system this is not quite correct, because at the start of each cycle some fraction of receive ports will become available, then later in the same cycle the same expected number of ports will become occupied with new packets.

In the wormhole network, the expected fraction of busy receive ports that become available at the start of a cycle is  $1/(\text{expected packet length})$ , i.e.

$$\frac{\alpha + \beta + \gamma}{\alpha L + (\beta + \gamma)m} \quad (14)$$

so the actual fraction  $x$  of receive ports that are in use at the start of a cycle is:

$$\begin{aligned} x &= p(\alpha L + (\beta + \gamma)m) \left( 1 - \frac{\alpha + \beta + \gamma}{\alpha L + (\beta + \gamma)m} \right) \\ &= p(\alpha(L-1) + (\beta + \gamma)(m-1)) \end{aligned} \quad (15)$$

If we randomly order the new packets competing for receive ports and attempt to deliver them in that order, then  $x$  is the probability that the first of these packets will encounter a busy port. As more packets are delivered this probability increases, until finally the probability that the last packet encounters a busy port is very nearly

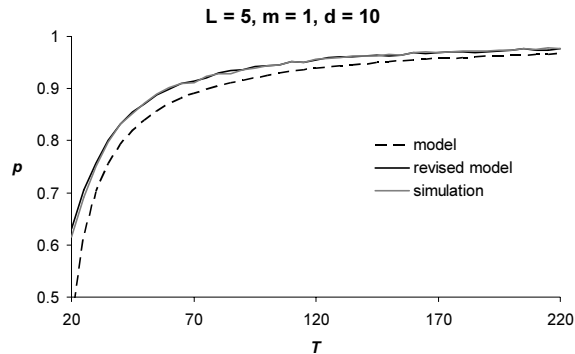
$$p(\alpha L + (\beta + \gamma)m) \quad (16)$$

A reasonable approximation is therefore to assume that all new packets encounter a busy receive port with probability midway between above two probabilities. This gives the following revised port utilization equation:

$$1 - p = p(\alpha(L - \frac{1}{2}) + (\beta + \gamma)(m - \frac{1}{2})) \quad (17)$$

Using equations (5), (8) and (9) once again to eliminate  $\alpha, \beta, \gamma$  gives us the same quadratic (10) and solution (11) as before but with  $L, m$  replaced by  $L - \frac{1}{2}, m - \frac{1}{2}$ . Figure 13-2 shows  $p$  plotted against  $T$  with  $d = 10$ ,  $L = 5$  and  $m = 1$  for the original model, the simulation, and the revised

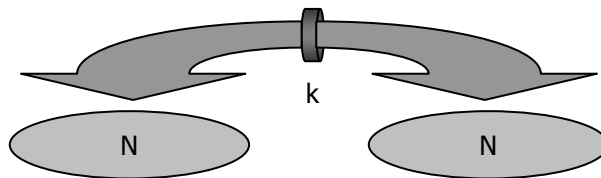
model. We see that the revised model gives a much closer match to the simulation results. For the remainder of the chapter we will use this improved model when considering wormhole routed networks; for circuit switched networks we will continue to use the original model as the inaccuracy is less pronounced.



**Figure 13-2:**  $p$  plotted against  $T$  in a wormhole routed network. Shown are the original model, the simulation results, and the revised model based on the corrected port utilization equation.

### 13.3 Bisection-Limited Network

We now shift our attention to the subject of our motivating problem: a network whose performance is limited by its bisection bandwidth. Figure 13-3 illustrates the network model that we use. There are  $N$  nodes in each half of the network, and the bisection consists of  $k$  ports in either direction. We model each half of the network as a crossbar, so that the nodes and bisection ports are fully connected. Both crossbars are again pipelined with diameter  $d$ . We will refer to a packet's destination as *remote* if it is on the other side of the bisection and *local* otherwise. A remotely destined packet is randomly routed to one of the bisection ports; if the port is free the packet passes through, otherwise it is dropped.



**Figure 13-3:** Bisection-limited network model.

### 13.3.1 Circuit Switched Network

Our circuit switched model now consists of four steady state parameters. Let  $\alpha_0$ ,  $\alpha_1$  be the rates at which a node attempts to send messages with local and remote destinations respectively. Let  $p_0$  be the probability of successful delivery once a packet reaches its destination; let  $p_1$  be the probability that a packet with a remote destination is able to cross the bisection.  $L$ ,  $m$ ,  $\lambda$  and  $T$  are as defined previously.

We now have two conservation of messages equations: one for local messages and one for remote messages. Since destinations are randomly chosen and, from a given node, exactly half of the destinations are remote, it follows that a node generates both local and remote messages at a rate of  $\lambda/2$ . The probability of successful delivery for a local message is  $p_0$ , and for a remote message it is  $p_0p_1$ . Our conservation equations are therefore:

$$\lambda/2 = p_0\alpha_0 \quad (18)$$

$$\lambda/2 = p_0p_1\alpha_1 \quad (19)$$

We also have two port utilization equations: one for receive ports and one for bisection ports. If a node successfully sends a local message it uses  $2d + L + 2m$  receive port cycles as in Section 13.2.1. Similarly, a successful remote message uses  $4d + L + 2m$  receive port cycles. Again, the probability that a receive port is in use is equal to the rate at which receive port cycles are used, so

$$\begin{aligned} 1 - p_0 &= p_0\alpha_0 (2d + L + 2m) + p_0p_1\alpha_1 (4d + L + 2m) \\ &= \lambda(3d + L + 2m) \quad (\text{using (18), (19)}) \\ \Rightarrow p_0 &= 1 - \lambda(3d + L + 2m) \quad (20) \end{aligned}$$

When a remote message passes through the bisection, the number of bisection port cycles used depends on whether or not the message is successfully delivered to its destination. If so (probability  $p_0$ ), then the port is used for  $4d + L + 2m$  cycles (the port is released as soon as the tail of the CONF packet passes through). Otherwise (probability  $1-p_0$ ) it is released after  $2d$  cycles when it is informed of the message's failure.

In a given direction, there are  $N$  nodes sending messages which pass through the bisection at a rate of  $p_1\alpha_1$ . Since there are  $k$  bisection ports in that direction, the rate at which each one is used (which is equal to the probability that a bisection port is in use) is:

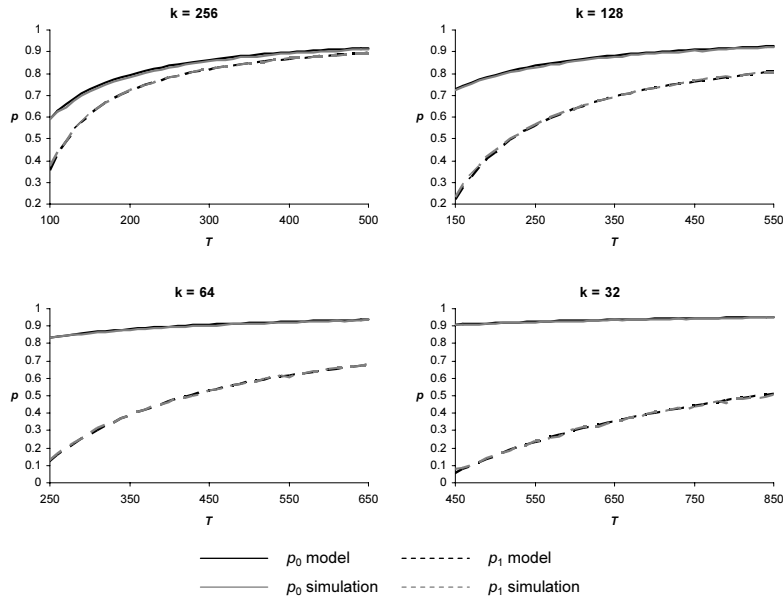


$$1 - p_1 = \frac{N}{k} \cdot p_1 \alpha_1 (2d + p_0(2d + L + 2m)) \quad (21)$$

Using (21), we can solve for  $p_1$  in terms of  $p_0$ :

$$p_1 = 1 - \frac{N\lambda(2d + p_0(2d + L + 2m))}{2kp_0} \quad (22)$$

Figure 13-4 plots  $p_0$  and  $p_1$  against  $T$  for the model and our simulations. We show results for four different bisection bandwidths  $k$  with  $N = 1024$ ,  $d = 10$ ,  $L = 7$  and  $m = 2$ . Again, the simulation results are closely matched by the model's predictions. The corresponding graphs for other values of  $L$  and  $m$  are very similar.



**Figure 13-4:** Simulated and predicted values of  $p_0$  and  $p_1$  plotted against  $T$  for a circuit-switched bisection-limited network with  $N = 1024$ ,  $d = 10$ ,  $L = 7$ ,  $m = 2$ .

### 13.3.2 Wormhole Routed Network

The number of steady-state parameters is also doubled in the wormhole-routed network. Let  $p_0, p_1$  be as defined in the previous section. For  $i = 0, 1$ , let  $\alpha_i, \beta_i, \gamma_i$  be the respective rates at which a node sends MSG, ACK and

CONF packets with local ( $i = 0$ ) and remote ( $i = 1$ ) destinations. Our receive port utilization equation is:

$$1 - p_0 = p_0(\alpha_0(L - \frac{1}{2}) + (\beta_0 + \gamma_0)(m - \frac{1}{2})) + p_0 p_1(\alpha_1(L - \frac{1}{2}) + (\beta_1 + \gamma_1)(m - \frac{1}{2})) \quad (23)$$

and our bisection port utilization equation is:

$$1 - p_1 = \frac{N}{k} \cdot p_1(\alpha_1(L - \frac{1}{2}) + (\beta_1 + \gamma_1)(m - \frac{1}{2})) \quad (24)$$

The six conservation equations are the same as equations (5), (8) and (9) with  $p = p_0$  for the local packets and  $p = p_0 p_1$  for the remote packets. Hence:

$$\lambda/2 = p_0^2 \beta_0 \quad (25)$$

$$\lambda/2 = p_0^2 p_1^2 \beta_1 \quad (26)$$

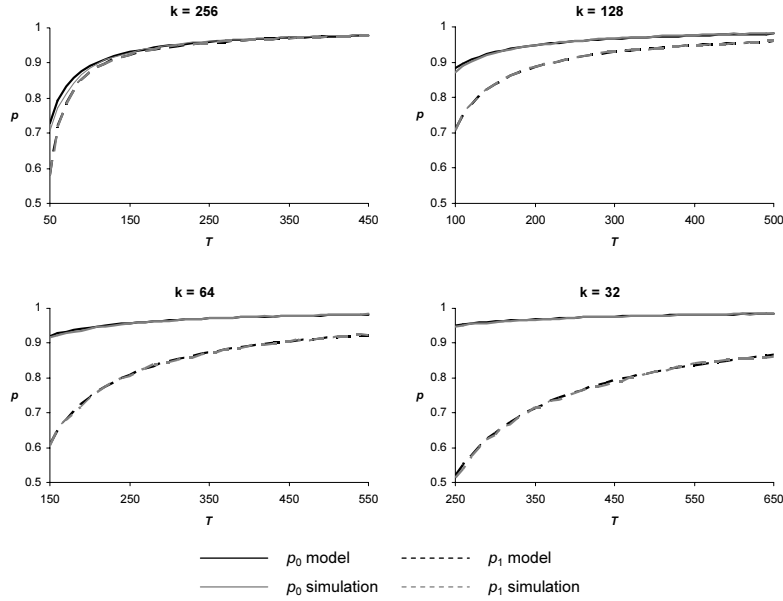
$$\alpha_0 = (2 - p_0) \gamma_0 \quad (27)$$

$$\alpha_1 = (2 - p_0 p_1) \gamma_1 \quad (28)$$

$$\gamma_0 = p_0 \beta_0 \quad (29)$$

$$\gamma_1 = p_0 p_1 \beta_1 \quad (30)$$

Eliminating  $\alpha_i$ ,  $\beta_i$ ,  $\gamma_i$  and  $p_1$  leaves a quartic in  $p_0$ , and  $p_1$  is expressed as a rational function of  $p_0$ . Figure 13-5 shows the resulting plots of  $p_0$  and  $p_1$  against  $T$ , again compared with simulation, using the same network parameters as the previous section ( $N = 1024$ ,  $d = 10$ ,  $L = 7$  and  $m = 2$ ). Once again, the model agrees closely with simulation results.



**Figure 13-5: Simulated and predicted values of  $p_0$  and  $p_1$  plotted against  $T$  for a wormhole routed bisection-limited network with  $N = 1024$ ,  $d = 10$ ,  $L = 7$ ,  $m = 2$ .**

### 13.3.3 Multiple Solutions

In the wormhole model, each of the four (complex) solutions to the quartic in  $p_0$  gives us values for  $\alpha_i$ ,  $\beta_i$ ,  $\gamma_i$  and  $p_1$ . In most cases only one of these solutions is meaningful, i.e.  $p_0$  is a real number,  $0 < p_0, p_1 < 1$ ,  $\alpha_i$ ,  $\beta_i$ ,  $\gamma_i$  are all positive, and the expected rate at which a node injects flits into the network is between 0 and 1:

$$0 < (\alpha_0 + \alpha_1)L + (\beta_0 + \beta_1 + \gamma_0 + \gamma_1)m < 1 \quad (31)$$

For some values of  $k$ ,  $T$ , however, we found two solutions to the equations that satisfied all of these constraints. Figure 13-6 plots both solutions of  $p_0, p_1$  against  $T$  for  $k = 32$  (again using  $L = 7$  and  $m = 2$ ). The extra solution behaves rather oddly; both  $p_0$  and  $p_1$  decrease with  $T$ , while at the same time  $\alpha_1$ ,  $\beta_1$  and  $\gamma_1$  increase (not shown). This indicates that the extra solution models a dynamically unstable state in which the bisection is bombarded with so many remotely destined packets that few packets can get through and as a result remote messages remain in the system for longer, compensating for their slower rate of generation.

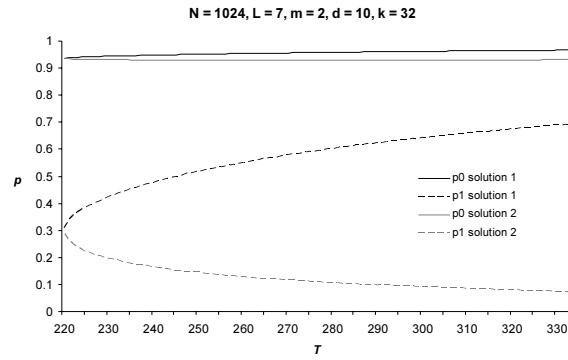


Figure 13-6: Multiple Solutions.

### 13.3.4 Comparing the Routing Protocols

We are now in a position to compare the two types of routing protocols that we have studied: circuit switched and wormhole routed. Recall our motivation for making this comparison; while wormhole routing generally provides better performance, circuit switching may offer an advantage on a bisection limited network by allowing the ACK and CONF packets to cross the bisection with probability 1 after the MSG packet is delivered.

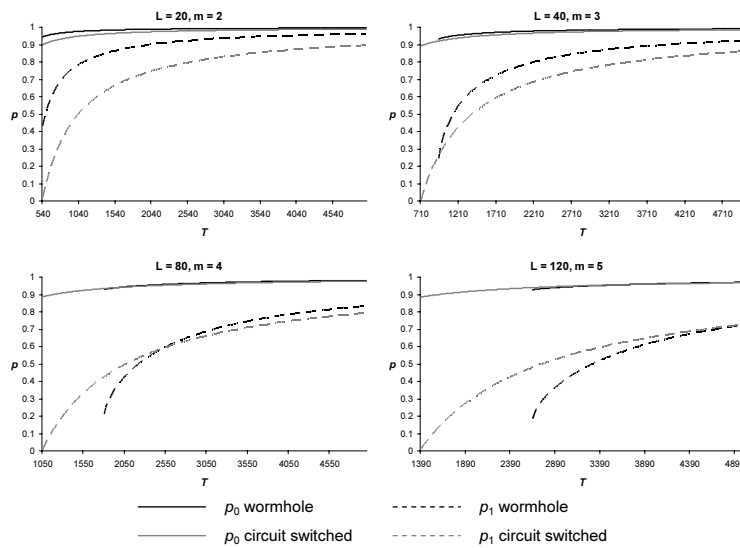
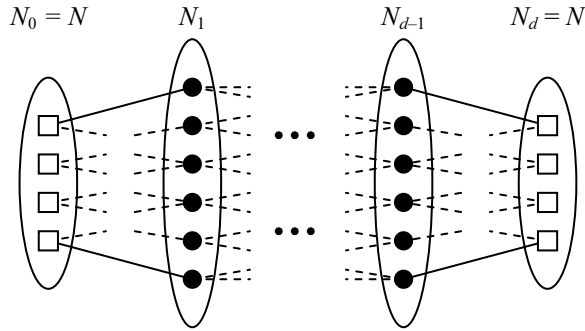


Figure 13-7: Analytic comparison of wormhole routing vs. circuit switching on a bisection-limited network for 4 values of  $L, m$  with  $N = 1024, k = 32, d = 10$ .

In Figure 13-7 we analytically compare the two protocols on a bisection-limited network with  $N = 1024$ ,  $k = 32$  and  $d = 10$ . We see that circuit switching can offer improved performance and greater network capacity, but only if the messages are extremely long (at least  $\sim 4$  times the network diameter) and the network is heavily loaded.

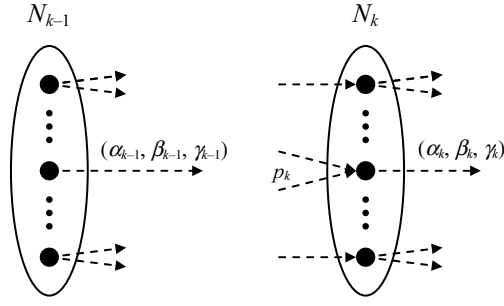
### 13.4 Multistage Interconnection Networks

The modeling technique we have presented is general and can be applied to arbitrary network topologies. In this section we will show how to model wormhole-routed multistage interconnection networks, using a butterfly network as a concrete example. Multistage interconnection networks are particularly well suited to this type of analysis as they can be modeled one stage at a time.



**Figure 13-8:**  $N$  processor nodes (squares) connected by a  $d$  stage interconnection network with  $N_k$  network nodes after the  $k^{\text{th}}$  stage.

Consider  $N$  processor nodes connected by a  $d$  stage wormhole-routed interconnection network. Let  $N_k$ ,  $k = 1, \dots, d - 1$ , be the number of network nodes at the end of the  $k^{\text{th}}$  stage, and for completeness let  $N_0 = N_d = N$  (Figure 13-8). Assume that network traffic is uniform and that all nodes at the same stage are indistinguishable. As before, let  $\alpha$ ,  $\beta$  and  $\gamma$  be the rates at which processor nodes send MSG, ACK and CONF packets respectively. Let  $\alpha_k$ ,  $\beta_k$ ,  $\gamma_k$  be the corresponding rates at which packets emerge from nodes at the end of the  $k^{\text{th}}$  stage, with  $(\alpha_0, \beta_0, \gamma_0) = (\alpha, \beta, \gamma)$ . Let  $p_k$  be the probability that a packet entering the  $k^{\text{th}}$  network stage passes through successfully to the next stage, or is delivered if  $k = d$  (Figure 13-9). Finally, let  $p = p_1 p_2 \dots p_d$  be the overall probability that a packet is successfully delivered to its destination.



**Figure 13-9:** Nodes at the end of stage  $k-1$  emit packets into stage  $k$  at rates  $(\alpha_{k-1}, \beta_{k-1}, \gamma_{k-1})$ . Each of these packets passes through to stage  $k+1$  with probability  $p_k$ .

In the  $k^{\text{th}}$  network stage, we derive our conservation equations from the following observation: the rate at which a given type of packet emerges from a node at the end of the  $k^{\text{th}}$  stage is equal to the rate at which packets are delivered to that node times the probability  $p_k$  of successfully passing through the node. Hence:

$$\begin{aligned}
 \alpha_k &= \frac{N_{k-1}}{N_k} \alpha_{k-1} p_k \\
 \beta_k &= \frac{N_{k-1}}{N_k} \beta_{k-1} p_k \\
 \gamma_k &= \frac{N_{k-1}}{N_k} \gamma_{k-1} p_k
 \end{aligned} \tag{32}$$

or equivalently,

$$\begin{aligned}
 \alpha_k &= p_1 p_2 \cdots p_k \frac{N}{N_k} \alpha \\
 \beta_k &= p_1 p_2 \cdots p_k \frac{N}{N_k} \beta \\
 \gamma_k &= p_1 p_2 \cdots p_k \frac{N}{N_k} \gamma
 \end{aligned} \tag{33}$$

The port utilization equation for the  $k^{\text{th}}$  stage depends on the specific topology of this stage. Regardless of the topology, the equation will provide a rational expression for  $p_k$  in terms of  $\alpha_{k-1}$ ,  $\beta_{k-1}$  and  $\gamma_{k-1}$ . Finally, the end-to-end conservation equations are the same as equations (5), (8) and (9). These equations give  $\alpha$ ,  $\beta$ ,  $\gamma$  in terms of  $p$  and  $\lambda$ . Using (33) and the

port utilization equations we can inductively find rational expressions for  $\alpha_k$ ,  $\beta_k$ ,  $\gamma_k$  and  $p_k$  in terms of  $p$  and  $\lambda$ . Finally, we can use the end-to-end probability equation  $p = p_1 p_2 \dots p_d$  to solve numerically for  $p$  given  $\lambda$ .

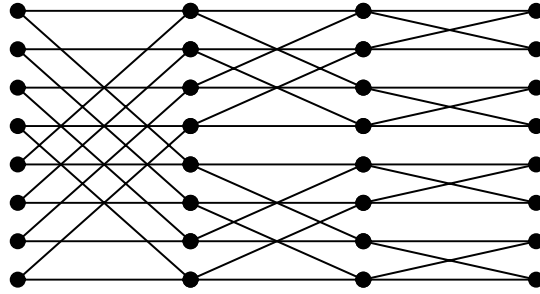


Figure 13-10: 3-state butterfly network.

### 13.5 Butterfly Network

We now apply the results of the previous section to the butterfly network. A  $d$  stage butterfly network connects  $N = 2^d$  processor nodes; Figure 13-10 shows a 3-stage butterfly network. Two features of the butterfly network are relevant to our analysis. First, each stage contains the same number of nodes, so we can drop the fraction  $N / N_k$  from equations (33). Second, the topology of each stage consists of pairs of nodes at the beginning of the stage which are cross-connected to the corresponding nodes at the end of the stage. It follows that when a packet is emitted into a stage, it will be competing with packets from only one other node, but packets are sent to one of two receive ports at the end of the stage depending on their ultimate destination. We therefore must divide the probability of encountering a busy port by 2, so our port utilization equation for the  $k^{th}$  stage is

$$\begin{aligned}
 1 - p_k &= \frac{1}{2} p_k (\alpha_{k-1} (L - \frac{1}{2}) + (\beta_{k-1} + \gamma_{k-1}) (m - \frac{1}{2})) \\
 &= \frac{1}{2} p_1 p_2 \dots p_k (\alpha (L - \frac{1}{2}) + (\beta + \gamma) (m - \frac{1}{2})) \quad (34)
 \end{aligned}$$

Dividing the  $k^{th}$  stage equation by the  $(k-1)^{th}$  stage equation allows us to solve for  $p_k$  in terms of  $p_{k-1}$ :

$$\frac{1 - p_k}{1 - p_{k-1}} = p_k \Rightarrow p_k = \frac{1}{2 - p_{k-1}} \quad (35)$$

If we let  $p_k = a_k / b_k$  (where we have a degree of freedom in choosing  $a_k$ ,  $b_k$ ), then equation (35) becomes:

$$\frac{a_k}{b_k} = \frac{b_{k-1}}{2b_{k-1} - a_{k-1}} \quad (36)$$

At this point we can use our degree of freedom to assume that the numerators and denominators of (36) are exactly equal. Thus  $b_{k-1} = a_k$  and

$$a_{k+1} = 2a_k - a_{k-1} \quad (37)$$

so  $\{a_k\}$  is an arithmetic sequence. Since  $a_d / a_{d+1} = p_d$ , we can again use the degree of freedom to assume that  $a_d = p_d$  and  $a_{d+1} = 1$ . It follows that:

$$a_k = p_d + (d-k)(p_d - 1) \quad (38)$$

Now the port utilization equation for the  $d^{\text{th}}$  stage is:

$$1 - p_d = \frac{1}{2} p (\alpha(L - \frac{1}{2}) + (\beta + \gamma)(m - \frac{1}{2})) \quad (39)$$

Using equations (5), (8) and (9) to eliminate  $\alpha$ ,  $\beta$  and  $\gamma$ , this becomes:

$$p - p \cdot p_d = \frac{1}{2} p (2 - p) \lambda (L - \frac{1}{2}) + (1 + p) \lambda (m - \frac{1}{2}) \quad (40)$$

Next, we have

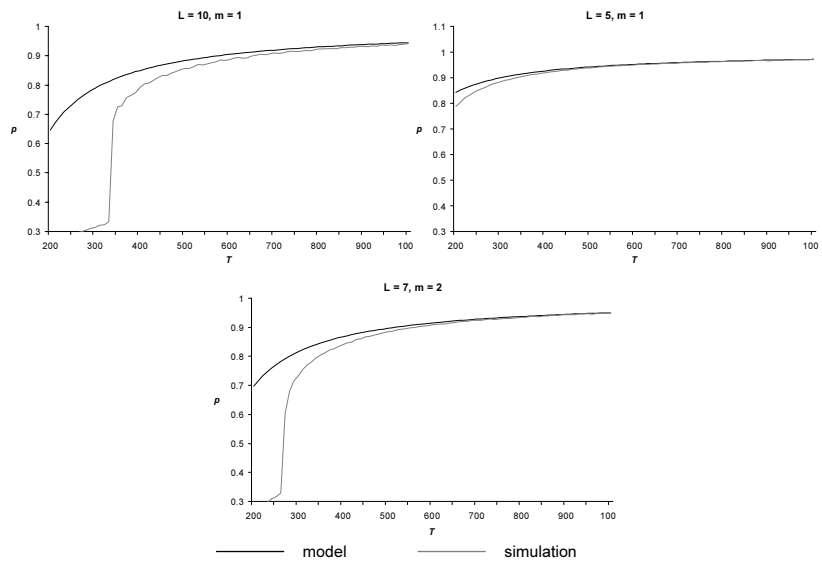
$$\begin{aligned} p &= p_1 p_2 \cdots p_d = \frac{a_1}{a_2} \frac{a_2}{a_3} \cdots \frac{a_d}{a_{d+1}} \\ &= \frac{a_1}{a_{d+1}} = \frac{p_d + (d-1)(p_d - 1)}{1} \\ \Rightarrow p_d &= 1 + \frac{p-1}{d} \end{aligned} \quad (41)$$

Using (41) to eliminate  $p_d$  in (40) and substituting  $\lambda = 1/T$  leaves us with a quadratic in  $p$ :

$$\left( \frac{2T}{d} - L \right) p^2 + \left( 2L + m - \frac{2T}{d} \right) p + m = 0 \quad (42)$$

Surprisingly, this is exactly the same quadratic that we obtained for the crossbar network (10) but with  $T$  replaced by  $2T/d$ . Figure 13-11 shows  $p$  plotted against  $T$  on a 10-stage butterfly network for the model and simulations. Three different choices of  $(L, m)$  are shown. We see that the accuracy of the model increases with  $T$ ; for small values of  $T$  the model is optimistic and in particular it overestimates the capacity of the network.





**Figure 13-11: Simulated and predicted values of  $p$  versus  $T$  for a 10-stage butterfly network.**

# Chapter 14

## Evaluation of the Idempotent Messaging Protocol

*The more we elaborate our means of communication, the less we communicate.*

– Joseph Priestley (1733-1804), “Thoughts in the Wilderness”

In this chapter we evaluate the idempotent messaging protocol in simulation. Our simulations are directed by two specific goals. First, we wish to determine the implementation parameters that optimize overall performance. Second, we would like to quantify the performance impact of the messaging protocol compared to wormhole routing on a non-discarding network.

### 14.1 Simulation Environment

Our evaluations were conducted using a trace-driven network simulator. In this section we describe the machine model, the format of the traces, how they were obtained, the four micro-benchmarks that were used, and the parameters of the trace-driven simulator.

#### 14.1.1 Hardware Model

Our hardware model, based on the Hamal architecture, is a distributed shared memory machine with explicitly split-phase memory operations, hardware multithreading, and register-based synchronization via join capabilities. New threads are created with a *fork* instruction which specifies the node on which the new thread should run and the set of registers to copy from parent to child. Memory consistency is enforced in software using a *wait* instruction. Pointers contain *node* and *offset* fields; distributed objects are implemented by allocating the same range of offsets on each node. There are no data caches, which does not affect our results as all micro-benchmarks explicitly migrate data to where it is needed.

### 14.1.2 Block Structured Traces

Typically, the input to a trace-driven simulator is simply a set of network messages where each message specifies a source node, a destination node, the size of the message, and the time at which the message should be sent. These traces may be obtained by instrumenting actual parallel programs running on multiple real or simulated processor nodes.

There are two problems with this straightforward approach. First, in an actual program the time at which a given message is sent generally depends on the time that one or more previous messages were received. It is therefore inaccurate to specify this time a priori in a trace. Second, a large parallel computer may not be readily available, and the number of threads required to run a parallel program on thousands of simulated nodes can easily overwhelm the operating system.

We address the first problem by organizing the trace into *blocks* of timed messages. Each block represents a portion of a thread in the parallel program which can execute from start to finish without waiting for any network messages. When a block is activated, each of its messages is scheduled to be sent at a specified number of cycles in the future. Each message optionally specifies a target block to signal when the message is successfully delivered; a block is activated when it has been signaled by all messages having that block as a target. This block-structured trace captures the dependency graph of messages within an application, and allows the simulation to more accurately reflect the pattern of messages that would arise from running the parallel program with a given network configuration.

Block-structured traces are similar to *intrinsic traces* [Holliday92], used in trace-driven memory simulators to model programs whose address traces depend on the execution environment. It has been observed that trace-driven parallel program simulations can produce unreliable results if the traces are of timing-dependent code ([Holliday92], [Goldschmidt93]); our micro-benchmarks and synchronization mechanisms were therefore chosen to ensure deterministic program execution.

### 14.1.3 Obtaining the Traces

The second problem – the difficulty of simulating thousands of nodes on a single processor – is addressed by our method of obtaining traces. We provide a small library of routines that implement the hardware model described in Section 14.1.1; these functions are listed in Table 14-1. The routines are instrumented to transparently manage threads, blocks, messages, and the passage of time. Most importantly, they are designed to allow the program to run as a *single thread*. This is primarily accomplished by implementing the Fork routine using a function call rather than actually creating a new thread. Figure 14-1 gives a very simple program written with this library.

Function	Description
Load	Load data from a (possibly remote) location
Store	Store data to a (possibly remote) location
Wait	Wait for all outstanding stores to complete
Fork	Start a new thread of execution
Join	Write data to another thread's registers
Sync	Register synchronization: wait for a join

**Table 14-1: Simulation library functions.**

```

void Fork (_thread t,    /* thread entry point */
          int node,    /* destination node */
          ...);        /* other arguments */

int ComputeSum (Pointer data)
{
    JCap *j = new JCap;
    Fork(SumThread, 0, numNodes, data, j);
    return Sync(j);
}

void SumThread (int cNodes, Pointer data, JCap *j)
{
    if (cNodes > 1)
    {
        int n = cNodes / 2;
        JCap *j1 = new JCap;
        JCap *j2 = new JCap;
        Fork(SumThread, node, n, data, j1);
        Fork(SumThread, node + n, cNodes - n, data, j2);
        Join(j, Sync(j1) + Sync(j2));
    }
    else
    {
        data.node = node;
        Join(j, Load(data));
    }
}

```

**Figure 14-1: Sample program to compute the sum of a distributed object with one word on each node. `node` and `numNodes` are global variables.**

As an example of how the library routines are implemented, Figure 14-2 gives simplified code for `Load`. `thread` is a global variable managed by the library routines which points to the current thread of execution. The `Load` routine begins by creating a new block representing the continuation of the current thread once the value of the load has been received (it is assumed that the current thread must wait for this value – we are not taking prefetching into account). Then a message of type ‘load’ is added to the current block which targets this continuation (the trace driven simulator automatically generates load reply messages; the target block becomes the

target of the reply). Finally, the thread block pointer is updated to the new block and the contents of the memory word are returned.

The actual Load routine is slightly more complicated as it also checks for address conflicts with outstanding stores. The Wait routine is provided to enforce memory consistency by explicitly waiting for all stores to complete before execution continues.

While the library routines automatically manage the passage of time for the parallel primitives that they implement, it is the programmer's job to manage the passage of time for normal computation. A macro is provided for adding time to the current block. The programmer is responsible for making use of this macro and providing a reasonable estimate of the number of cycles required to perform a given computation.

```
void Block::AddMessage (int type,          /* message type */
                       int dst,          /* destination */
                       Block *target); /* target block */

Word Load (Pointer p)
{
    Block *newBlock = new Block;

    thread->block->AddMessage(TYPE_LOAD, p.node, newBlock);
    thread->block = newBlock;

    return memory[p.address];
}
```

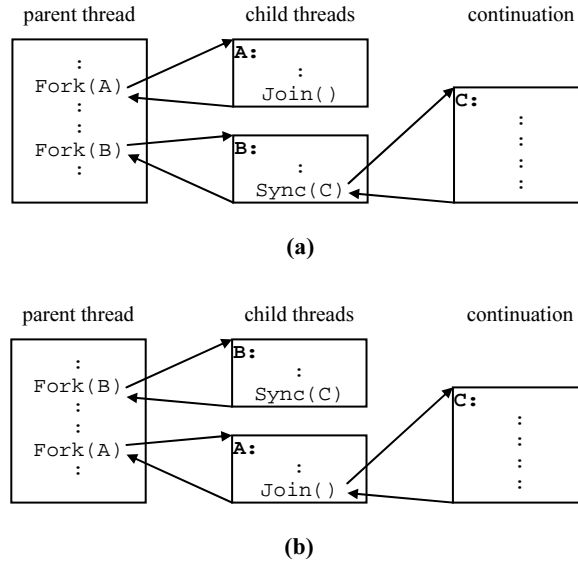
**Figure 14-2: Load routine (simplified). `thread` is a global variable.**

#### 14.1.4 Synchronization

In the simulation environment, register-based synchronization is accomplished using the Sync and Join library routines. There are no actual registers in the simulation, so Join is implemented by storing a word of data in the join capability data structure (and adding a message to the current block); Sync retrieves the word from the data structure (and creates a new block).

Because the simulation is run as a single thread, the straightforward implementation of Sync will only work if the data is already available, i.e. if the corresponding Join has already been called. If all synchronization is from child to parent then this will always be the case because implementing Fork using a function call causes the “threads” to run to completion in a depth-first manner. Figure 14-1 gives an example of child to parent synchronization. While each Fork conceptually creates a new thread, the single-threaded implementation simply calls SumThread as a subroutine and then returns, so Join will already have been called by the time the parent thread calls the corresponding Sync.

To allow for more complicated synchronization wherein Sync may be called before the corresponding Join, a version of Sync is provided in which the programmer explicitly provides a continuation. If the data is ready when Sync is called, then the continuation is invoked immediately. Otherwise the continuation is stored in the join capability data structure and invoked when the corresponding Join is called (Figure 14-3). This sacrifices some of the transparency of the simulation environment in order to retain the benefits of being able to run the simulation using a single thread.



**Figure 14-3: (a) Join called before Sync; continuation invoked by Sync. (b) Sync called before Join; continuation invoked by Join.**

#### 14.1.5 Micro-Benchmarks

Four micro-benchmarks were chosen to provide a range of network usage patterns. Each one was coded as described in the previous sections. The four resulting block-structured traces were used to drive our simulations. The micro-benchmarks are as follows:

- add:** Parallel prefix addition on 4096 nodes with one word per node. Light network usage. Network is used for synchronization and thread creation.
- reverse:** Reverse the data of a 16K entry vector distributed across 1024 nodes. Very heavy network usage with almost all messages crossing the bisection.

- quicksort:** Parallel quicksort of a 32K entry random vector on 1024 nodes. Medium, irregular network usage (lighter than *reverse* or *nbody* due to a higher computation to communication ratio).
- nbody:** N-body simulation on 256 nodes with one body per node. Computation is structured for  $O(\sqrt{N})$  communication by conceptually organizing the nodes in a square array and broadcasting the location of each body to all nodes in the same row and column. Heavy network usage; network is used in bursts.

#### 14.1.6 Trace-Driven Simulator

The trace driven simulator keeps track of active blocks and memory requests on all nodes in the system. Blocks are serviced in a round-robin fashion; on each cycle every node picks an active block and advances it by one time step, possibly generating a new message. This models a multi-threaded processor which is able to issue from a different thread on each cycle. Memory requests are processed on a first-come first-served basis. Each request takes 6 cycles to process, after which the reply message is automatically generated and the next request can be serviced.

In an attempt to ensure that our results are independent of the network topology, four different topologies are used in all simulations: a 2D grid, a 3D grid, a radix-2 dilation-2 multibutterfly, and a radix-4 (down) dilation-2 (up) fat tree. For the grid networks dimension-ordered routing is preferred, but any productive channel may be used to route packets. In all cases wormhole routing is used, with packet heads advancing one step per cycle. Each network link contains a small flit buffer; if a packet cannot be advanced due to congestion it may be buffered for as many cycles as there are flits in the buffer, after which it is discarded. The maximum packet transit time  $T$  is therefore the size of these buffers multiplied by the diameter of the network. When a node receives an ACK packet it has 32 cycles to respond with a CONF, after which the ACK is discarded. Receivers must therefore remember messages for  $2T + 32$  cycles after receiving a CONF, as explained in Chapter 5.

The size of a packet is determined by the fields that it contains, which in turn is determined by the packet type. Table 14-2 lists the sizes of the various fields. All fields are fixed-size except for the type field which uses a variable length encoding to identify the packet as a CONF, an ACK, or one of four message types. Table 14-3 lists the sizes of the various packets. In this table “MSG header” refers to the four fields present in every message packet which are required to route the packet and implement the idempotent messaging protocol: *type*, *dest*, *source* and *message ID*. The size of the fork packet depends on the number of registers being copied to the new

thread; this number is denoted by  $N$  in the table. Flits are 25 bits each. This size was chosen both so that CONF packets would fit into a single flit and so that the number of physical bits required to transmit a flit with double error correction is  $\leq 32$  (five ECC bits are required for 25 bit flits).

Field	Size in Bits
type	1 (CONF), 2(ACK), 4(MSG)
source	16
destination	16
address	32
data	32
message ID	32
secondary ID	8

**Table 14-2: Packet field sizes.**

Packet Type	Fields	Size in Bits
CONF	type + dest + secondary ID	25
ACK	type + dest + source + messageID + secondary ID	74
LOAD	MSG header + address + return address	132
STORE	MSG header + address + data + return address	164
FORK	MSG header + address + $N$ x data	$100 + 32N$
JOIN	MSG header + address + data	132

**Table 14-3: Packet sizes. MSG header = type + dest + source + message ID.**

## 14.2 Packet Retransmission

The first important implementation parameter for the idempotent messaging protocol is the strategy used for packet retransmission. In order for the protocol to function correctly, it is necessary to periodically retransmit MSG and ACK packets. When such a packet is sent, it should be scheduled for retransmission at

$$size + 2 \times distance + constant + backoff$$

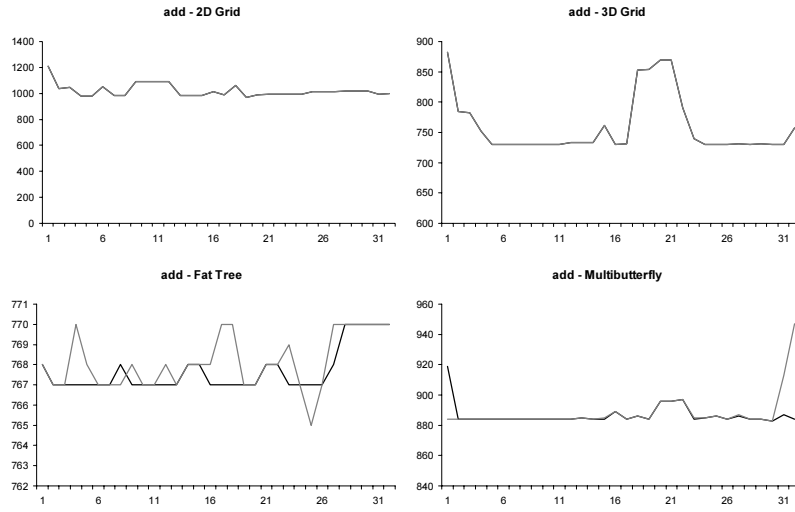
cycles in the future. The first three terms in this sum represent the amount of time it takes to receive an ACK/CONF packet if the receiving node is able to reply immediately and if neither packet is dropped by the network, where *size* is the size of the packet in flits, *distance* is the number of hops to the destination node, and *constant* is a small constant to account for processing time. The *backoff* term is a function of the number of transmit attempts for the packet ( $n$ ), and represents the strategy being used to manage network congestion.

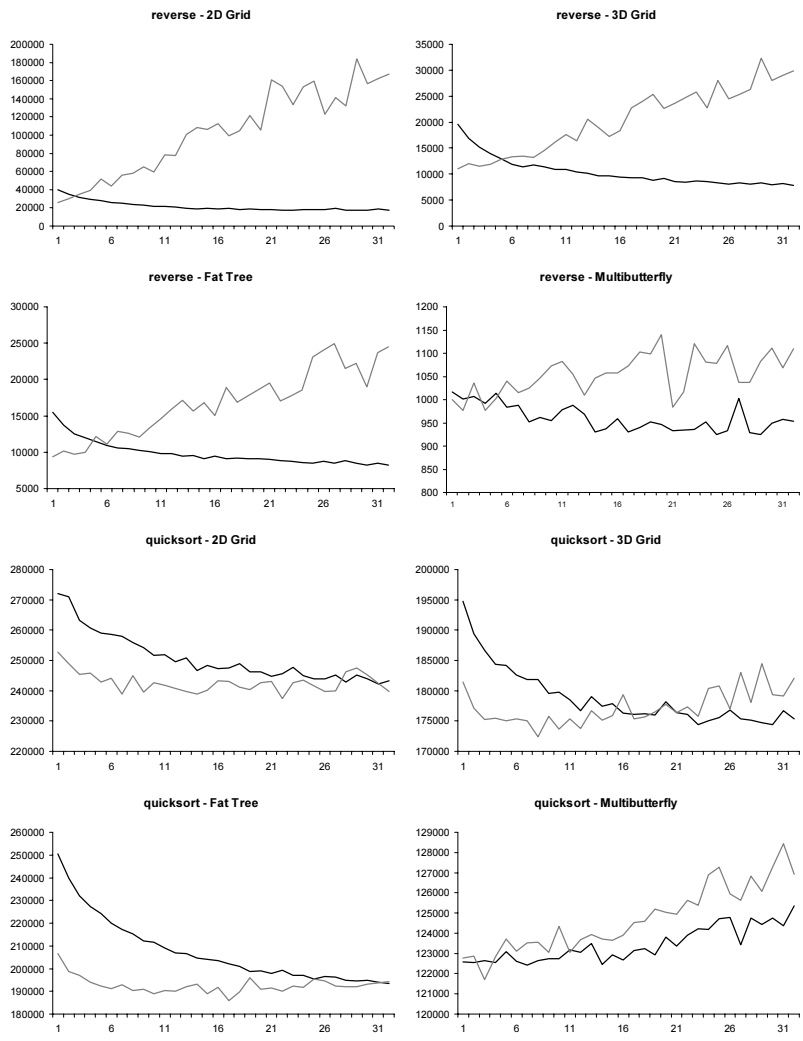
Four backoff terms were considered: constant ( $C$ ), linear ( $Cn$ ), quadratic ( $Cn^2$ ) and exponential ( $C \cdot 2^n$ ). We do not present results for constant or

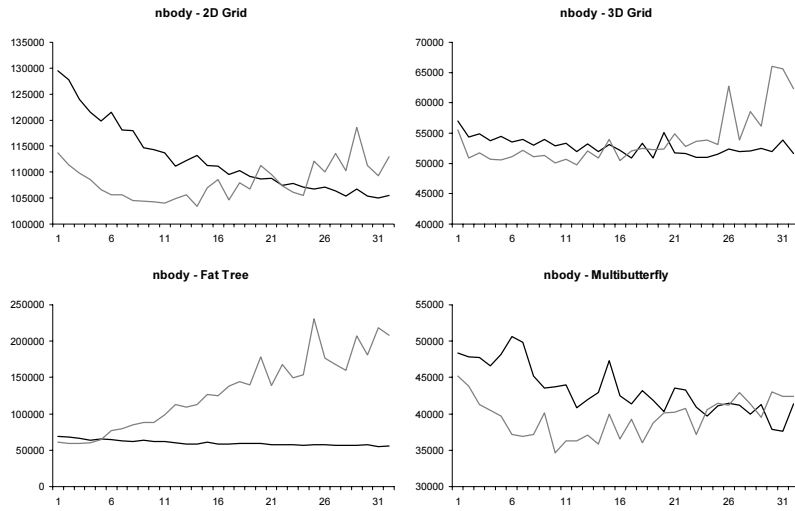


exponential backoff as their performance was unacceptable. A constant backoff is intuitively bad as it makes no attempt to manage congestion, and indeed in simulation it often caused livelock when the network became congested. Exponential backoff was found to be overkill; in a congested network packets were often rescheduled with excessively large delays and as a result performance suffered.

Figure 14-4 shows plots of execution time for all four micro-benchmarks on all four topologies with both linear and quadratic backoff as the retransmission constant  $C$  is varied from 1 to 32. We see that quadratic backoff performs well with small  $C$ , but performance quickly degrades as  $C$  becomes larger. By contrast, in almost all cases the performance of linear backoff improves with  $C$ , the one exception being quicksort on a multibutterfly. Intuitively this indicates that even quadratic backoff is overkill, so that linear backoff with a large constant is to be preferred. However, it is difficult to say with any certainty from simply inspecting the graphs which retransmission strategy is best. Resorting to numerical analysis, we asked the question of which strategies provided closest-to-optimal performance in the worst and average cases (where “optimal” refers to the best observed performance for a given benchmark/topology combination). We found linear backoff with  $C = 30$  to be superior under both metrics, performing within 9.3% of optimal in the worst case and within 2.8% of optimal in the average case.







**Figure 14-4: Execution time in cycles plotted against retransmission constant  $C$  for linear (—) and quadratic (---) backoff.**

Table 14-4 list the best backoff strategy according to both metrics for each benchmark, each network, and overall. So, for example, in the quicksort benchmark a quadratic backoff with  $C = 15$  performed at worst within 1.020 of optimal across all four topologies, and on a 2D grid network linear backoff with  $C = 28$  performed on average within 1.026 of optimal across all four benchmarks. This table is much easier to read than the previous graphs, and clearly indicates that a linear backoff with a large constant is to be preferred. We therefore use linear backoff with  $C = 32$  (since this is easy to compute in hardware) for the remainder of the evaluations.

	slowdown over optimal			
	worst case		average case	
<b>add</b>	1.009	L5	1.003	L5
<b>reverse</b>	1.028	L30	1.016	L32
<b>quicksort</b>	1.020	Q15	1.015	Q12
<b>nbody</b>	1.085	L31	1.045	L31
<b>2D grid</b>	1.033	L32	1.026	L28
<b>3D grid</b>	1.039	L32	1.018	L30
<b>fat tree</b>	1.085	L31	1.036	L30
<b>multibutterfly</b>	1.041	L32	1.015	L32
<b>overall</b>	1.093	L30	1.028	L30

**Table 14-4: Best backoff strategy as measured by worst case and average case slowdown over optimal for each benchmark, each network, and overall.**

It is worth noting that our results differ from those obtained in [Brown02b]. Our simulations and analyses have changed in three respects. First, the simulator has been improved to more accurately model threads and memory references. Second, flit buffering has been added to the network nodes. Third, the multibutterfly network has been included in the simulations. The graphs of Figure 14-4 are qualitatively similar to those in [Brown02b], but numerical analysis has yielded different results.

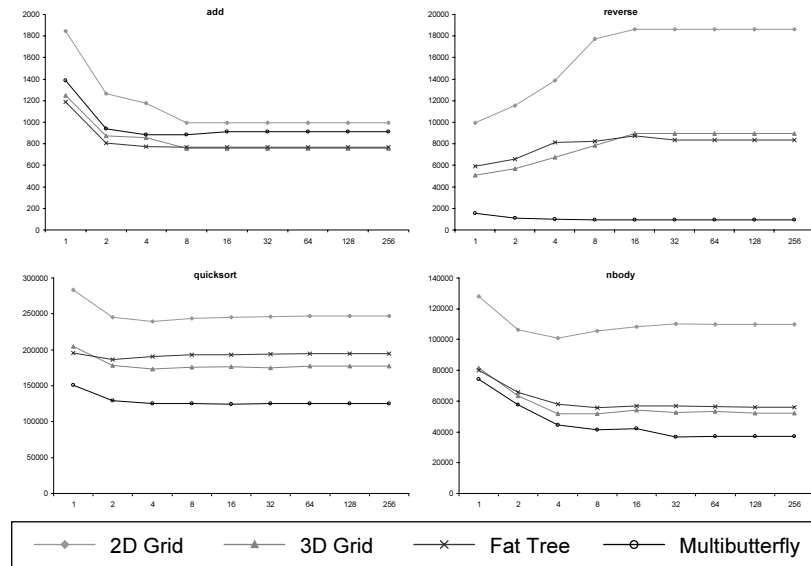


Figure 14-5: Execution time vs. send table size.

### 14.3 Send Table Size

The next important implementation parameter is the size of the send tables. There is a tradeoff between performance and implementation cost since if a table fills up it will temporarily prevent new messages from being sent, but increasing the size of the table requires additional resources to remember more message packets. In Figure 14-5 execution time is graphed for all micro-benchmarks and topologies as the send table size is varied from  $2^0$  to  $2^8$ . In most cases execution time quickly drops to a minimum, and we can achieve near-optimal performance with as few as 8 send table entries. The notable exception is *reverse*, where execution time actually increases with larger table sizes. This is due to the increased network congestion that results when nodes are able to send more messages. The remainder of the simulations will assume 8-entry send tables.

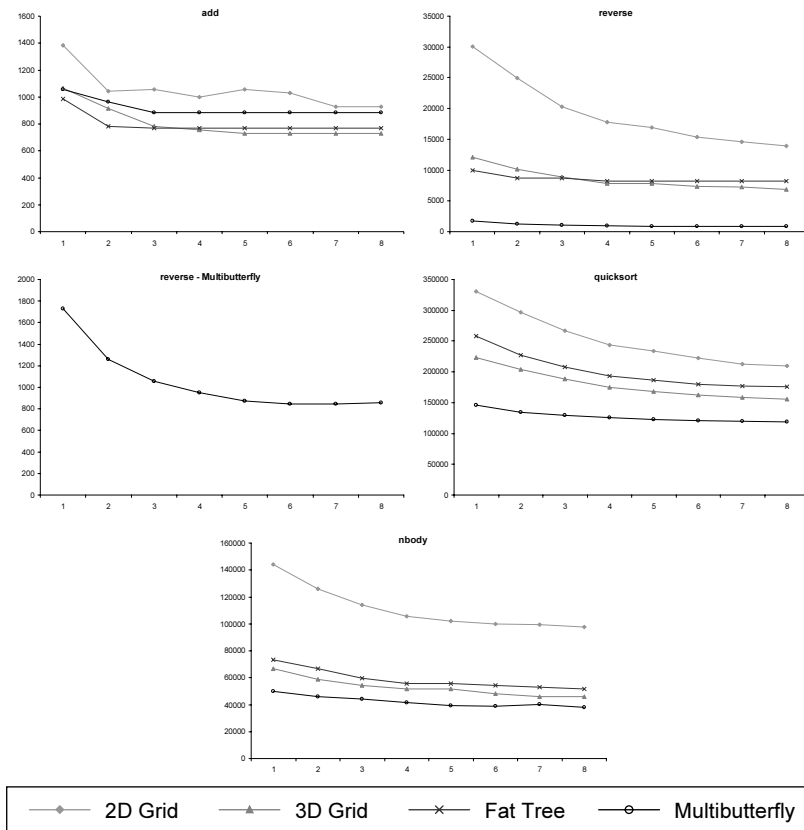


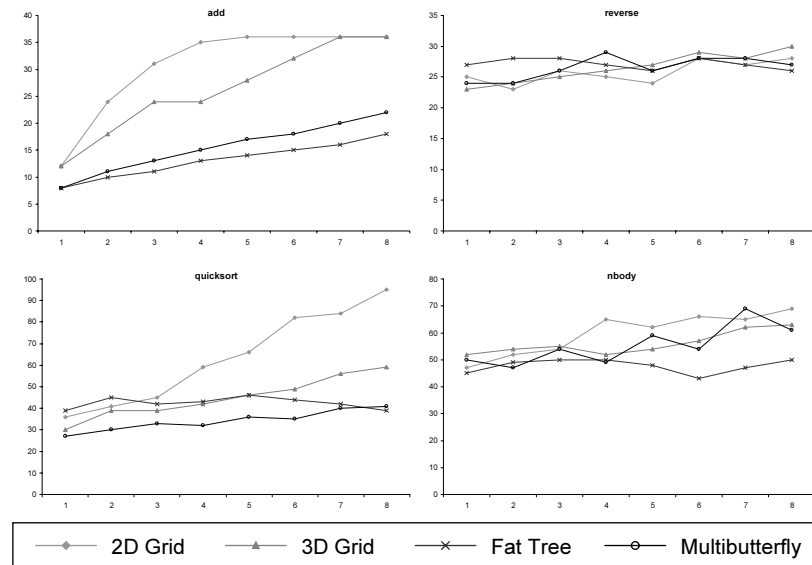
Figure 14-6: Execution time vs. network node flit buffer size.

## 14.4 Network Buffering

A single flit buffer along every routing path within a network node is both necessary and sufficient for correct network operation. It is necessary because the network is assumed to be synchronous so that flits must be buffered before being advanced to the next node; it is sufficient because a discarding network can simply drop packets when there is contention for an output port. However, we may be able to improve performance by allowing a small number of flits to be buffered instead of immediately discarding the packets. In Figure 14-6 we plot execution time against flit buffer size as the buffers are varied from 1 to 8 flits. The graphs show that the improvement is significant – over 2x for reverse on a 2D grid or multibutterfly.

There are two costs associated with these buffers. The obvious cost is the additional hardware within the network nodes. The less obvious cost is an increase in the number of receive table entries. Recall that a receive

table entry must be remembered for  $2T + R$  cycles after a CONF is received, where  $T$  is the maximum transit time for a packet and  $R$  is the maximum time allowed to process an ACK (32 cycles in our simulations). If the diameter of the network is  $d$  and the size of the buffers is  $k$  flits, then  $2T + R = 2kd + 32$ . In the worst case, then, it would not be unreasonable to expect the receive table requirements to increase almost linearly with  $k$ . However, this may be partially or wholly compensated for by the fact that larger buffers reduce the probability of ACK's and CONF's being dropped, reducing in turn the expected amount of time from sending the first ACK to receiving a CONF. Resorting again to simulation, Figure 14-7 plots the maximum number of active receive table entries at any time on any node as the buffer sizes range from 1 to 8 flits. We see that in most cases the effect of the buffer sizes on the receive tables is minimal. It is therefore reasonable to choose the size of the buffers based solely on the tradeoff between performance and network hardware complexity. For the remainder of our simulations we will use 8 flit buffers.



**Figure 14-7: Maximum number of receive table entries vs. network node flit buffer size.**

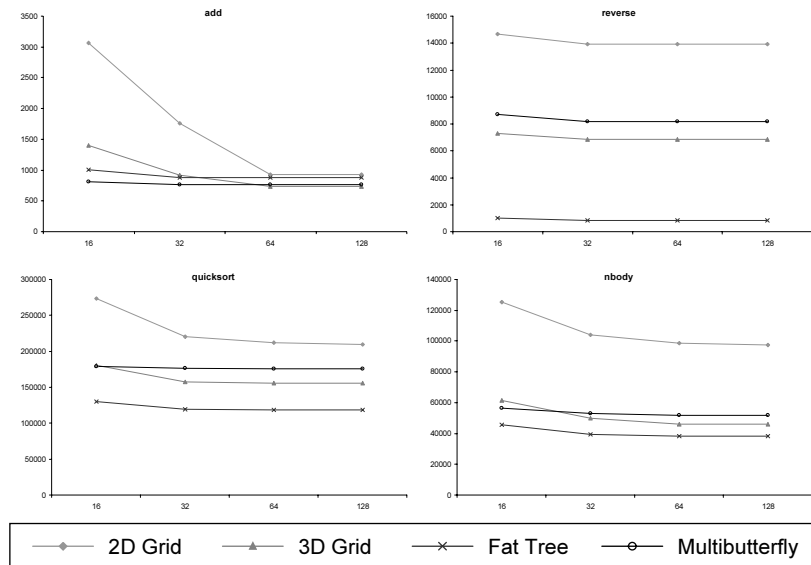


Figure 14-8: Execution time vs. receive table size.

## 14.5 Receive Table Size

If a receive table fills, new message packets which arrive over the network must be dropped. This wastes network bandwidth since these packets have already traversed the network, so it is important to ensure that the receive tables are not too small. At the same time there are two costs associated with the receive tables. First, the tables themselves require expensive content-addressable memory. Second, the size of the secondary ID's is the base 2 logarithm of the receive table size (recall that a secondary ID is a direct index into the receive table). Thus, increasing the size of the receive tables beyond a power of two increases the size of both ACK and CONF packets.

In Figure 14-8 execution time is plotted against four different receive table sizes (16, 32, 64, 128). We see a significant improvement in performance from 16 to 32 entries, moderate improvement from 32 to 64 entries, and negligible improvement from 64 to 128 entries. As can be seen from Figure 14-7, this is largely due to the fact that most benchmark/topology combinations never use more than 64 receive table entries in the worst case. Figure 14-8 shows that in the cases where more than 64 entries are required, performance is barely affected by limiting the size of the receive table to 64. We therefore use 64-entry receive tables for the remainder of the simulations. Note that this reduces the size of CONF packets to 23 bits and the size of ACK packets to 72 bits.

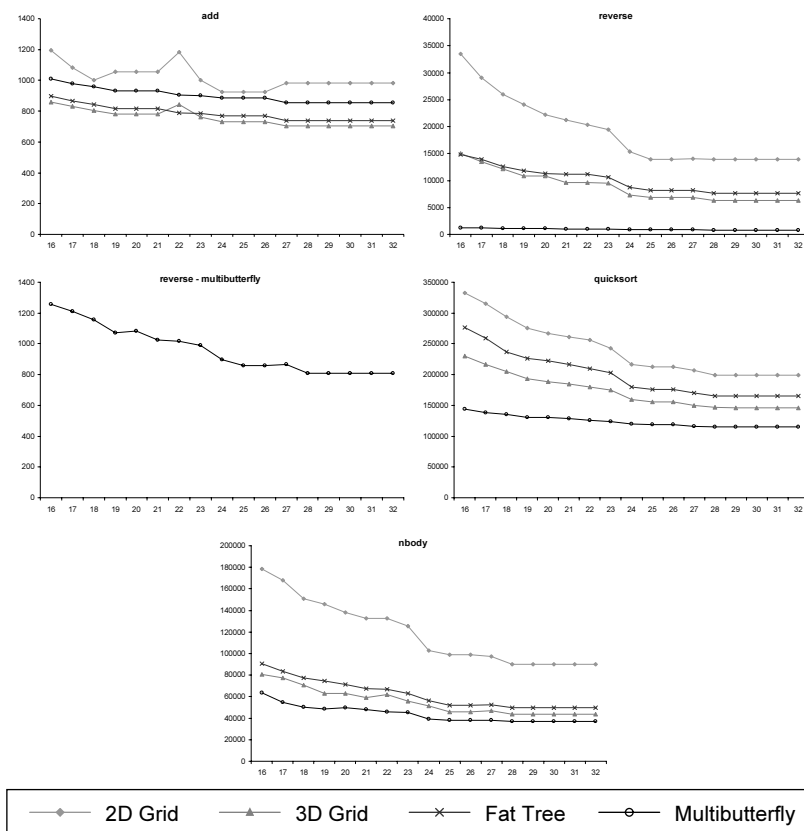


Figure 14-9: Execution time vs. channel width.

## 14.6 Channel Width

Different network implementations will make use of different flit sizes. In Figure 14-9 we show execution time plotted against flit size as the number of bits in a flit varies from 16 to 32. We see that our choice of 25 bit flits was fortuitous; there is a significant improvement in performance from 16 to 25 bits, but little improvement beyond that point. Figure 14-10 provides some intuition for these graphs by showing packet size vs. flit size for five different packet types. Fork (3) refers to a fork packet where 3 registers are copied into the child thread. Note that for many benchmark/topology combinations there is a noticeable improvement in performance from 23 bits to 24 bits as the size of the ACK packets drops from 4 flits to 3 flits (e.g. reverse on a 2D grid).



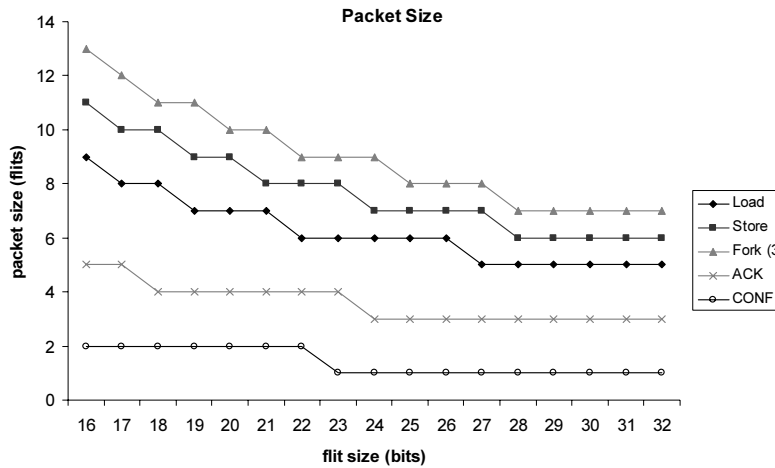


Figure 14-10: Packet size in flits vs. flit size in bits.

### 14.7 Performance Comparison: Discarding vs. Non-Discarding

For small systems it is probably worth constructing a reliable network, whereas for extremely large systems it is almost certainly necessary to implement a fault-tolerant messaging protocol. In between these extremes, however, it may be difficult to determine which approach is more appropriate, and it becomes useful to know the performance impact of the fault-tolerant messaging protocol.

To compare the two approaches, we simulated a perfect network with both the discarding protocol and non-discarding buffered wormhole routing. In both cases network nodes have 8-entry flit buffers and each communication link consists of 30 physical bits. In the discarding network 25 of these bits contain data and 5 are ECC bits required to detect up to two bit errors. In the non-discarding network, errors must be *corrected*, not simply detected, which requires 9 bits. Additionally, a single backpressure bit is required to prevent buffer overruns. Thus, the non-discarding network uses 20 bit flits. For the non-discarding grid networks, strict dimension-ordered routing is used to avoid deadlocks [Dally87].

The results of the comparison are shown in Table 14-5. We see that the actual slowdown, which ranges from as little as 0.99 to as much as 3.36, depends on both the application and the network topology. In general, a more congested network leads to greater slowdowns. Note that in our simulations we are assuming that the cycle times of the two networks are the same. In practice this would likely not be the case for two reasons. First,

the control logic of the discarding network is much simpler than that of the non-discarding network; as a result it will be possible to clock the discarding network nodes at a higher speed ([DeHon94], [Chien98]). Second, with a fault-tolerant messaging protocol it is possible to boost the clock speed even further since one does not need to worry about introducing the occasional signaling error so long as it can be detected.

topology:	2D Grid			3D Grid		
	discarding?		slowdown	discarding?		slowdown
	no	yes		no	yes	
<b>add</b>	934	926	<b>0.99</b>	741	730	<b>0.99</b>
<b>reverse</b>	4711	13924	<b>2.96</b>	2372	6829	<b>2.88</b>
<b>quicksort</b>	165368	212296	<b>1.28</b>	128526	155849	<b>1.21</b>
<b>nbody</b>	44200	98708	<b>2.23</b>	33576	45838	<b>1.37</b>

topology:	Fat Tree			Multibutterfly		
	discarding?		slowdown	discarding?		slowdown
	no	yes		no	yes	
<b>add</b>	773	768	<b>0.99</b>	893	884	<b>0.99</b>
<b>reverse</b>	2432	8183	<b>3.36</b>	640	859	<b>1.34</b>
<b>quicksort</b>	119382	176369	<b>1.48</b>	110543	118979	<b>1.08</b>
<b>nbody</b>	36115	51930	<b>1.44</b>	34369	38146	<b>1.11</b>

**Table 14-5: Slowdown of messaging protocol compared to wormhole routing on a perfect network.**

We can attempt to quantify the amount by which clock speed may be increased by “normalizing for reliability”, that is, choosing network parameters so that both the discarding and the non-discarding networks have the same mean time between failures (MTBF). Suppose we wish the network as a whole to have a MTBF of  $10^{10}$  seconds. Assuming a 1GHz network, this is  $10^{19}$  cycles. If  $\sim 10^5$  flits are transferred on each cycle, then the probability of failure for a single flit should be  $10^{-24}$ .

In the non-discarding network, each flit consists of 29 bits, including ECC bits. A failure occurs whenever a flit contains 3 or more single bit errors. If the probability of error for a single bit is  $p$ , then to first order the probability of failure for the entire flit is

$$\binom{29}{3} p^3 = 3654 p^3 \quad (1)$$

$\Rightarrow 3654 p^3 = 10^{-24} \Rightarrow p \approx 6.492 \times 10^{-10}$ . Next we must relate  $p$  to the clock speed. We will consider the case in which sampling jitter is the dominant source of error, where by “sampling jitter” we mean the combination of signal jitter and receiver clock jitter. Assume that signal setup time  $t$



In the discarding network, a failure is an undetected error. Thus, a failure occurs whenever a flit contains 4 or more single bit errors *and* the modified flit is a valid code word. Since we are using a linear code, this is the case if and only if the error vector itself is a valid code word. It can be shown using a simple counting argument (or by brute force if one is not inclined to count) that the given code contains 945 code words of weight 4. Thus, if the probability of error for a single bit is  $p$ , then to first order the probability of failure for an entire flit is  $945 p^4 \Rightarrow 945 p^4 = 10^{-24} \Rightarrow p \approx 1.804 \times 10^{-7}$ . If the clock period in the discarding network is  $T'$ , then in this case we find  $\frac{1}{2}(T' - t) \approx 5.089\delta$ .

Finally, to relate the clock speeds of the two networks we must make an additional assumption regarding the size of the sampling window relative to the clock period. Assuming that  $t = T/3$ , we have

$$\frac{T - T/3}{6.068} = \frac{T' - T/3}{5.089} \Rightarrow T' = \frac{5.089}{6.068} 2T/3 + T/3 \approx 0.892T \quad (3)$$

If we again compare the two approaches under the assumption that the non-discarding network has 24 bit flits and a clock that runs 11% faster, we obtain the results shown in Table 14-6. In this case the slowdowns are slightly less severe.

topology:	2D Grid			3D Grid		
	discarding?		slowdown	discarding?		slowdown
	no	yes		no	yes	
<b>add</b>	934	862	<b>0.92</b>	741	690	<b>0.93</b>
<b>reverse</b>	4711	13765	<b>2.92</b>	2372	7007	<b>2.95</b>
<b>quicksort</b>	165368	200076	<b>1.21</b>	128526	148210	<b>1.15</b>
<b>nbody</b>	44200	91019	<b>2.06</b>	33576	43378	<b>1.29</b>

topology:	Fat Tree			Multibutterfly		
	discarding?		slowdown	discarding?		slowdown
	no	yes		no	yes	
<b>add</b>	773	722	<b>0.93</b>	893	825	<b>0.92</b>
<b>reverse</b>	2432	7809	<b>3.21</b>	640	845	<b>1.32</b>
<b>quicksort</b>	119382	165556	<b>1.39</b>	110543	112669	<b>1.02</b>
<b>nbody</b>	36115	49989	<b>1.38</b>	34369	35319	<b>1.03</b>

**Table 14-6: Slowdown when discarding network uses 24 bit flits and runs 11% faster.**



# Chapter 15

## System Evaluation

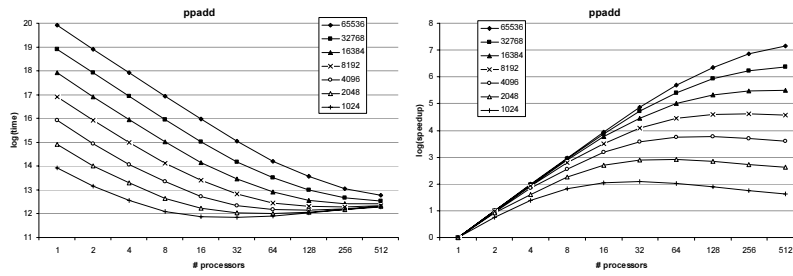
*The whole is more than the sum of its parts.*

– Aristotle (ca. 330 BC), “Metaphysica”

Ultimately, the question of interest regarding any parallel architecture is: How well does it perform? In a scalable system, performance is eventually limited by the costs of synchronization, communication and thread management. As the number of processors increases, so too do these overheads. For every application, there comes a point at which increasing the number of processors offers no further performance gains. The goal, then, is to minimize these overheads so that programs can take full advantage of the large number of available processors. The extent to which an architecture meets this goal can be measured by inspecting performance curves of parallel applications. In this chapter we use the four benchmarks presented in Chapter 9 as case studies in our evaluation of the Hamal parallel computer.

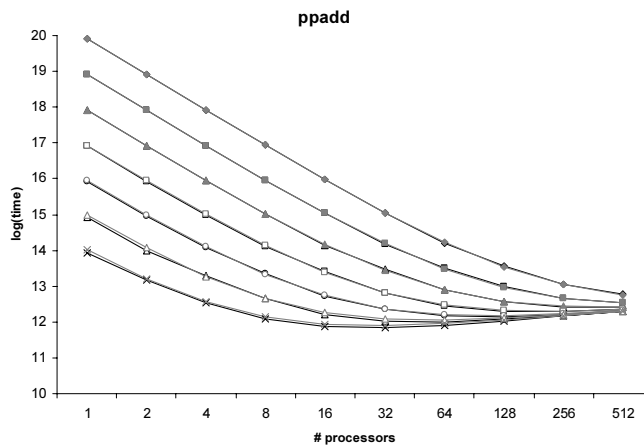
### 15.1 Parallel Prefix Addition

*ppadd* is a simple benchmark in which there is a clean separation between the linear-time vector processing and the log-time overheads of thread creation, communication and synchronization. The running time for a vector of length  $m$  on  $N$  processors is  $C_0 + C_1m/N + C_2\log(N)$ . Figure 15-1 shows log-log plots of execution time and speedup for several different problem sizes as the number of processors is increased from 1 to 512. The larger the problem size, the greater the range of machine sizes over which linear speedup is achieved.



**Figure 15-1: Execution time and speedup for the *ppadd* benchmark.**

Fitting the model for run-time to the observed data using least-squares analysis yields constants  $C_0 = 1386$ ,  $C_1 = 15$  and  $C_2 = 398$ . The accuracy of the resulting model can be seen in Figure 15-2 which superimposes graphs of predicted and observed run-times.  $C_2$  represents the overhead of adding another level to the binary tree of threads used to perform the parallel prefix computation. This overhead, which includes the costs of thread creation, upward communication of partial sums, downward communication of left sums, and exit synchronization, is less than 400 cycles. As a result, the benchmark scales extremely well and benefits from increasing the number of processors even when there are fewer than 32 vector entries on each node.



**Figure 15-2: Actual (black) and modeled (grey) run times for the *ppadd* benchmark.**

## 15.2 Quicksort

The *quicksort* benchmark is qualitatively similar to *ppadd* in that a log-depth binary tree of threads is created to perform the computation. It is quantitatively different, however, because the cost of adding a level to the tree is much higher. Each step in the recursion involves splitting one vector into two and then redistributing these vectors over two disjoint sets of processors. Thus, the dominant overhead is communication and not thread creation or synchronization.

Figure 15-3 shows log-log plots of execution time and speedup for several different problem sizes. Again, the larger the problem size, the greater the range over which linear speedup is achieved. Note that in this case we generally do not see linear speedup with few (1-4) processors; this is due to the fact that quicksort is a randomized algorithm so each recursion does not subdivide the problem into two equal parts. As the number of processors grows it becomes easier to subdivide them according to the ratio of the expected work in the sub-problems, resulting in closer-to-linear speedups.

Inspecting the curves for problem sizes 4096-65536, we find that optimal performance is achieved when the average number of vector entries per node is 128. It follows that the communication overhead of each recursion step is on the same order of magnitude as the time required to quicksort a 128-entry vector on a single node, which we measured to be 19536 cycles. This is nearly two orders of magnitude larger than the overhead in the *ppadd* benchmark, indicating that while the Hamal architecture provides extremely efficient thread management and synchronization, communication is an area of weakness.

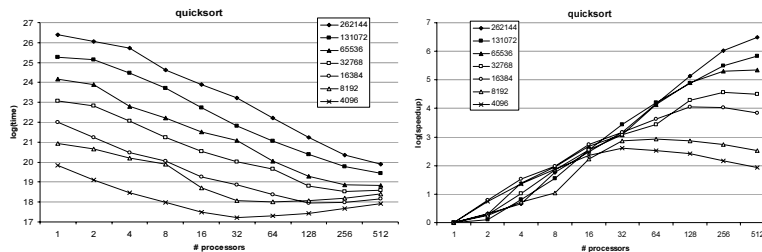


Figure 15-3: Execution time and speedup for the *quicksort* benchmark.

## 15.3 N-body Simulation

The *nbody* benchmark has been optimized for communication by conceptually arranging the processor nodes in a square array; processors communicate only with other processors in the same row or column. With  $m$  bodies distributed across  $N$  processors, each processor maintains  $m/N$  bodies and



must send them to  $(2\sqrt{N} - 1)$  other processors, and each processor computes and communicates a partial force for each of the  $m/\sqrt{N}$  bodies in its row, so the communication overhead is proportional to  $m/\sqrt{N}$ . Each processor must then compute the force interactions between the  $m/\sqrt{N}$  bodies in its row and the  $m/\sqrt{N}$  in its column, so the work for each processor is proportional to  $m^2/N$ . Furthermore, the constant for this work is fairly high since each force interaction requires performing the computation

$$\frac{m(x_2 - x_1, y_2 - y_1, z_2 - z_1)}{\left((x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2\right)^{\frac{3}{2}}}$$

We measured this constant to be approximately 70 cycles. Roughly speaking, we expect performance to improve as the number of nodes is increased as long as the communication overhead is less than the single-threaded workload, i.e.  $Cm/\sqrt{N} < 70m^2/N$  where  $C$  is the constant for the communication overhead. Simplifying, this condition becomes  $N < (70m/C)^2$ . From this we see that *nbody* is extremely scalable and, indeed, the execution time and speedup curves for 256 bodies on 1-256 processors (Figure 15-4) are almost perfectly linear. This is an indication that  $256 \ll (70 \cdot 256/C)^2$ , so  $C \ll 1120$ . Thus, the average cost of communicating 2 bodies and 1 force (a total of 88 bytes, using double-precision floating point numbers) in a 256 node machine is much less than 1120 cycles. This is not terribly informative and merely serves to reassure us that while the performance of communication in the Hamal architecture is not optimal, neither is it unacceptable.

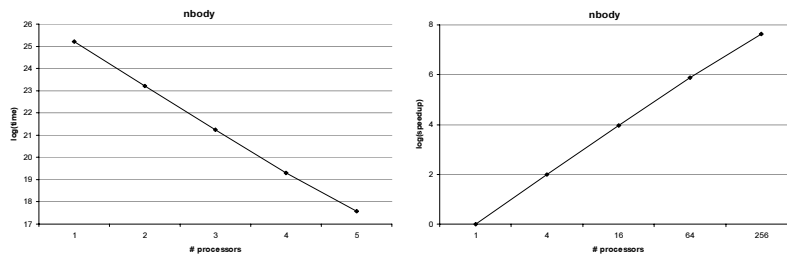


Figure 15-4: Execution time and speedup for the *nbody* benchmark.

## 15.4 Wordcount

The *wordcount* benchmark differs from the other three in that commonly occurring words (such as ‘a’ and ‘the’) introduce sequential bottlenecks which constrain performance as the number of processors is increased. Figure 15-5 shows execution time and speedup for the best-performing ver-

sion of the program, which is a spin-waiting local-access version in which each parent thread creates at most one child thread at a time. For  $\leq 16$  processors there is no lock contention, and as a result good speedups are observed. The speedup is slightly less than linear due primarily to load imbalance (each child thread is essentially created on a random node depending on the hash value of the current word). At 32 processors we see the emergence of contention which noticeably impacts performance. Additionally, the sequential bottlenecks start to become significant. Thereafter, performance improves at a much reduced rate.

From an evaluation standpoint, the most significant aspect of the *wordcount* benchmark is the large number of threads that it generates (over 30,000 – one for every word in [Brown02b]). This demonstrates the effectiveness of the thread management mechanisms in the Hamal processor and microkernel. In particular, the low cost of remote thread creation gives rise to the speedups observed with  $\leq 16$  processors.

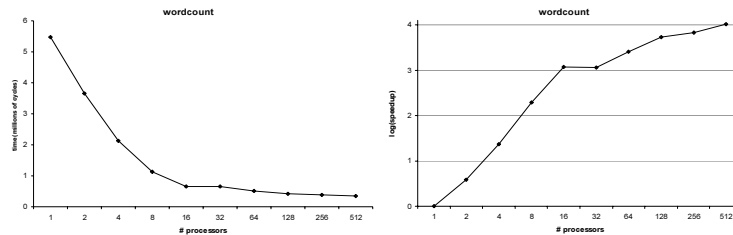


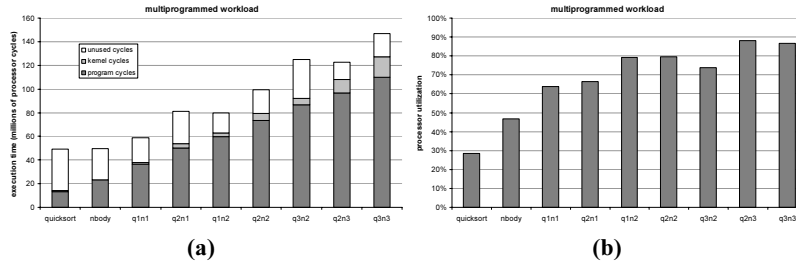
Figure 15-5: Execution time and speedup for the *wordcount* benchmark.

## 15.5 Multiprogramming

Hamal is a general purpose architecture and is designed to provide efficient support for running multiple independent programs via hardware multi-threading and low-overhead thread management. Processor utilization is maximized by dynamically choosing a context to issue on every cycle, allowing concurrent threads to fill each other's pipeline bubbles and memory stalls. Figure 15-6 shows execution times and processor utilization for various combinations of the *quicksort* and *nbody* benchmarks run concurrently on 16 processors. *quicksort* was run on a  $2^{16}$  entry vector, and *nbody* was run for 10 iterations; these parameters were chosen to roughly equalize the run-times of the individual benchmarks. Figure 15-6 graphs total numbers of processor cycles (there are 16 processor cycles on each machine cycle) and breaks them down into three categories. On a given processor, a cycle is a *program* cycle if a user thread issues, a *kernel* cycle if the kernel running in context 0 issues, and an *unused* cycle if no context can issue. The first two bars of Figure 15-6a give execution times for *quicksort* and *nbody* run on their own. The remaining bars given execution times for con-

current execution of copies of these benchmarks, using the nomenclature  $qXnY$  for  $X$  copies of *quicksort* and  $Y$  copies of *nbody*. Data is collected from the time the machine boots to the time the last user thread exits.

Both graphs clearly illustrate the benefits of cycle-by-cycle multi-threading which results in sub-additive run-times (Figure 15-6a) and increased processor utilization (Figure 15-6b). The execution time of *q1b1* is only slightly greater than that of the benchmarks run alone; in general program cycles are almost exactly additive whereas the number of unused cycles decreases. Note that as the number of threads increases, so too does the number of kernel cycles as more work is required to manage these threads. However, the kernel is largely able to take advantage of otherwise unused cycles so this has little effect on the overall run time (compare the number of kernel and unused cycles for *q3n2* and *q3n3*).



**Figure 15-6: (a) Execution time and (b) processor utilization for concurrent execution of the *quicksort* and *nbody* benchmarks.**

## 15.6 Discussion

Without question, the main strength of the Hamal architecture lies in its broad support for massive fine-grained parallelism. The low overheads of thread creation, concurrent execution, context swapping, event-driven thread management and register-based synchronization allow parallel applications to obtain high speedups as the number of processors is increased. The efficiency of thread management permits the use of a large number of threads without overwhelming the system (there are over 30,000 threads in *wordcount* and over 50,000 in *quicksort* on 512 nodes). Communication, on the other hand, is an area of weakness. In particular, possibly the most serious design flaw in the Hamal architecture is the lack of hardware support for data streaming. In order to move data from one node to another an application must write it to remote memory 128 bits at a time. Each write is placed in a separate network packet, incurring an overhead of at least 300%. This simple method of communication is sufficient for processor-intensive applications such as *nbody*, but noticeably impacts both the performance and potential scalability of communication-intensive applications such as *quicksort*.

# Chapter 16

## Conclusions and Future Work

*Great is the art of beginning, but greater is the art of ending.*

– Henry Wadsworth Longfellow (1807-82)

The goal of building a general-purpose shared-memory machine with millions or even billions of nodes gives rise to a number of design challenges and requires fundamental changes to the models currently used to construct systems with hundreds or thousands of processors. Ultimately, success will depend on advances in fabrication technology, computer architecture, fault management, compilers, programming languages, and development environments. This thesis has focused on hardware design, and we have presented **Hamal**: a shared-memory architecture with efficient support for massive parallelism which is directly scalable to one million nodes. In this chapter we summarize the key features of Hamal as well as our major findings, and we suggest directions for further research.

### 16.1 Memory System

A memory system is the canvas on which a parallel architecture is painted. A properly designed memory system facilitates the creation of a flexible and easily programmable machine, whereas a poor design inhibits performance and limits scalability. The Hamal memory system addresses the needs of future architectures by tightly integrating processors with memory and by making use of mechanisms which support arbitrary scaling.

The basic building block of the Hamal memory system is the *capability*, a tagged, unforgeable pointer containing hardware-enforced permissions and segment bounds. The use of capabilities has two important consequences. First, they allow the use of a single shared virtual address space. This greatly reduces the amount of state associated with a process and allows data to be shared simply by communicating a pointer. Second, capabilities ensure that all memory references are valid. Page faults no longer require the operating system to validate the faulting address, and they can be used to implement lazy allocation of physical pages. Additionally, we

have seen that it can be useful to place auxiliary information within the capability: we presented *squids*, which allow an architecture to support forwarding pointers without the overhead normally associated with aliasing problems.

All memory operations are explicitly split-phased, and a thread may continue to perform computation while it is waiting for replies from one or more memory requests. The hardware does not enforce any consistency model and makes no guarantee regarding the order in which memory operations with different addresses complete; weak consistency is supported via a *wait* instruction which allows software to wait for all outstanding memory operations to complete.

Virtual memory is implemented using a fixed mapping from virtual addresses to physical nodes and with associative hardware page tables, located at the memory, to perform virtual→ physical address translation. This completely eliminates the need for translation lookaside buffers, simplifying processor design and removing an obstacle to scalability.

We have presented *extended address partitioning* as well as an implementation of *sparsely faceted arrays* [Brown02b]. Each of these mechanisms allows distributed objects to be atomically allocated by a single node without any global communication or synchronization. Physical storage for distributed objects is lazily allocated on demand in response to page faults. A hardware *swizzle* instruction is provided to allow applications to map a continuous range of indices to addresses within a distributed object in a flexible manner.

## 16.2 Fault-Tolerant Messaging Protocol

In a machine with millions of discrete network components, it is extremely difficult to prevent electrical or mechanical failures from corrupting packets within the network. In the future, systems will need to rely on end-to-end messaging protocols in order to guarantee packet delivery. We have presented an implementation of a lightweight fault-tolerant messaging protocol [Brown02a] which ensures both message delivery and message idempotence. Each communication is broken down into three parts: a *message*, an *acknowledgement* which indicates message reception, and a *confirmation* which indicates that the message will not be re-sent. The protocol does not require global information to be stored at each node and is therefore inherently scalable. We have shown how the overhead of this protocol can be reduced by using receiver-generated *secondary ID's*.

We have developed an analytical model using a technique that can be applied to any fault-tolerant messaging protocol. The accuracy of the model was verified by simulation. An evaluation of the messaging protocol was conducted using *block-structured* trace driven simulations. We found that performance is optimized with small send tables (~8 entries), slightly

larger receive tables (~64 entries), and with linear backoff used for packet retransmission.

### 16.3 Thread Management

Massive parallelism implies massive multithreading; a scalable machine must be able to effectively manage a large number of threads. Hamal contains a number of mechanisms to minimize the overhead of thread management. A multithreaded processor allows multiple threads to execute concurrently. New threads are created using a single *fork* instruction which specifies a starting address for the new thread, the node on which the thread is to be created, and the set of general-purpose registers which are to be copied into the thread. Nodes contain 8-entry *fork queues* from which new threads can be loaded directly into a context or stored to memory for later activation. Each thread is associated with a hardware-recognized swap page in memory; this provides a uniform naming mechanism for threads and enables the use of *register-dribbling* to load and unload contexts in the background. Finally, *stall* events inform the microkernel that a context is unable to issue, allowing rapid replacement of blocked threads.

The effectiveness of these mechanisms was experimentally confirmed by simulating a number of parallel benchmark programs. Good speedups were observed, and benchmarks were able to make use of a large number of threads (over 50,000 in quicksort) without overwhelming the system. Additionally, cycle-by-cycle hardware multithreading was found to provide efficient support for multiprogrammed workloads by significantly increasing processor utilization.

### 16.4 Synchronization

Typically, the threads of a parallel program do not run in isolation; they collaborate to perform a larger task. Synchronization is required to ensure correctness by enforcing data dependencies and protecting the integrity of shared data structures. Hamal provides four different synchronization primitives. *Atomic memory operations* are the atomic read-and-modify operations found in all modern architectures. *Shared registers* provide efficient support for brief periods of mutual exclusion while accessing heavily-used shared data such as the *malloc* counter. *Register-based synchronization* allows one thread to write directly to another thread's registers, giving synchronization the same semantics and overheads as a high-latency memory operation. Register-based synchronization can be used to implement fast barrier and exit synchronization; the latency of a software barrier on 512 nodes is only 523 cycles. Finally, *UV trap bits* extend the semantics of memory operations in a flexible manner and can be used to implement a number of high-level synchronization primitives including locks and producer-consumer structures. Our experiments confirmed the results reported

in [Kranz92] regarding the performance advantages of using trap bits in memory to implement fine-grained synchronization. Additionally, we found the primary advantage of Hamal's UV trapping mechanism over previous similar mechanisms to be the handling of traps on the node containing the memory word rather than on the node which initiated the memory request.

## 16.5 Improving the Design

Our experience with the current design of the Hamal architecture has suggested a myriad of potential improvements. Many of these are trivial hardware modifications such as adding a status register or prioritizing events. In this section we outline some of the more challenging directions for future work.

### 16.5.1 Memory Streaming

The most significant limitation of the Hamal architecture is the lack of hardware support for streaming data transfers. Conceptually, a memory streaming mechanism is easy to implement by adding a small state machine to either the processor-memory node controllers or the individual memory banks. The difficulty is that this then becomes a hardware resource which must be carefully managed so that it does not introduce the possibility of deadlock. Additionally, the thread which initiates the streaming request must somehow be informed of the operation's completion for the purpose of memory consistency.

### 16.5.2 Security Issues with Register-Based Synchronization

Any general-purpose implementation of register-based synchronization must address the obvious security concern: threads must not be allowed to arbitrarily write to other threads' registers. Hamal deals with this issue by using unforgeable *join capabilities* which are generated by the thread containing the register(s) to be used for synchronization and which are required to perform writes to these registers. However, there is a more subtle security hole which has not yet been completely closed that involves trusted privileged subroutines.

The kernel exposes privileged functions to user programs via the kernel table which contains code capabilities with the *execute*, *privileged*, *increment-only* and *decrement-only* bits set. These functions are trusted black boxes; user programs may call them but should not be able to tamper with them. However, register-based synchronization introduces exactly this possibility. Consider a malicious program which spawns a child thread and gives the child a join capability for one of its own registers. The program then calls a trusted kernel routine while the colluding child thread uses the

join capability, interfering with the privileged routine and producing unpredictable results.

The obvious “solution” to this problem, which is to simply discard joins to registers which are not marked as busy, is insufficient as registers may be busy due to a memory read. Keeping track of registers which have been explicitly marked as busy using the *busy* instruction, and only allowing joins to these registers, solves the problem if trusted subroutines do not themselves make use of register-based synchronization, but this is a somewhat unfair and unsatisfying restriction.

### 16.5.3 Thread Scheduling and Synchronization

Locking and mutual exclusion synchronization is, as a rule, efficient when successful and costly when unsuccessful due to the need to spin-wait and/or block. It is therefore desirable for threads with one or more locks to complete their protected operations and release the locks as quickly as possible. However, there is currently no way for the kernel to know which threads have locks, and there is nothing preventing the kernel from swapping out a thread which is in a critical section in response to a *stall* or *timer* event. When this occurs it can seriously affect performance, as was shown by the two outstanding data points in the *wordcount* graph of Figure 11-3. An interesting direction for future research is to investigate ways of temporarily granting threads higher priority or immunity from being swapped out without introducing the possibility of deadlock or allowing dishonest applications to raise their own priority without cause.

## 16.6 Summary

When ENIAC – the world’s first large-scale general-purpose electronic computer – was completed in 1945, it filled an entire room and weighed over 30 tons. The engineers who designed it were visionaries, and yet even to them the concept of one million such processing automata integrated into a single machine would have been unfathomable. Just think of how many punch card operators would be required! Over half a century later, this fantasy of science fiction is close to becoming a reality. The first million node shared-memory machine will likely be built within the next decade. Equally likely is that it will fill an entire room and weigh over 30 tons.

The realization of this dream will have been made possible by the incredible advances of circuit integration and process technology. Yet Moore’s law alone is insufficient to carry shared-memory architectures past the million node mark. In this thesis we have presented design principles for a scalable memory system, a fault-tolerant network, low-overhead thread management and efficient synchronization, all of which are essential ingredients for the success of tomorrow’s massively parallel systems.





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*Pereant qui ante nos nostra dixerunt.*  
(To the devil with those who published before us.)

– Aelius Donatus (4<sup>th</sup> Century), Quoted by St. Jerome, his pupil

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